

Long-distance correlations of rhinovirus capsid dynamics contribute to uncoating and antiviral activity

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Human rhinovirus (HRV) and other members of the enterovirus genus bind small-molecule antiviral compounds in a cavity buried within the viral capsid protein VP1. These compounds block the release of the viral protein VP4 and RNA from inside the capsid during the uncoating process. In addition, the antiviral compounds prevent “breathing” motions, the transient externalization of the N-terminal regions of VP1 and VP4 from the inside of intact viral capsid. The site for externalization of VP1/VP4 or release of RNA is likely between protomers, distant to the binding cavity for antiviral compounds. Molecular dynamics simulations were conducted to explore how the antiviral compound, WIN 52084, alters properties of the HRV 14 capsid through long-distance effect. We developed an approach to analyze capsid dynamics in terms of correlated radial motion and the shortest paths of correlated motions. In the absence of WIN, correlated radial motion is observed between residues separated by as much as 85 Å, a remarkably long distance. The most frequently populated path segments of the network were localized near the fivefold symmetry axis and included those connecting the N termini of VP1 and VP4 with other regions, in particular near twofold symmetry axes, of the capsid. The results provide evidence that the virus capsid exhibits concerted long-range dynamics, which have not been previously recognized. Moreover, the presence of WIN destroys this radial correlation network, suggesting that the underlying motions contribute to a mechanistic basis for the initial steps of VP1 and VP4 externalization and uncoating.

long-range correlation | picornavirus | protein network | virus capsid MD simulations | functional protein dynamics

Human rhinovirus (HRV) infection is the most common cause of respiratory infection in humans (1) and incurs considerable economic expense (2). HRV replication is often restricted to the upper respiratory tract, and the resulting illness is of short duration, but HRV can also invade the lower respiratory tract and cause more serious infections (3, 4). Aided by the structure determination of HRV 14 in 1985 (5), much effort has been made to develop antiviral compounds such as disoxaril (WIN 51711) (6), WIN 52084 (7), WIN 54954 (8), and pleconaril (9). Pleconaril advanced to phase II clinical trials (10); however, no drug against HRV has been approved for distribution. These WIN compounds act primarily by inhibiting the “uncoating” process (11, 12) or release of genomic RNA from inside the host cell. Here we report results that elucidate this antiviral activity.

HRV, a member of the *Picornaviridae* family and the enterovirus genus, has an icosahedral capsid (Fig. 1A) with 60 copies of the protomer, which comprises four structural proteins—VP1, VP2, VP3, and VP4. A pentameric unit with five protomers is shown in Fig. 1B. The three larger proteins, VP1, VP2, and VP3, shown in blue, green, and red, respectively, in Fig. 1B and C, share a common structural motif, the eight-stranded, anti-parallel β barrel (5). A deep “canyon” on the capsid surface, indicated with a yellow ring in Fig. 1B and C, circumscribes the fivefold symmetry axis. WIN compounds, including WIN 52084

(Fig. 1B and C, gold space-filled spheres), bind below this canyon in a hydrophobic cavity, or pocket, in the interior of VP1.

Along with release of RNA, the uncoating process is also associated with the loss of VP4 from the viral capsid (13) as well as externalization of the N terminus of VP1 (14). Antibody recognition (15) and results from limited proteolysis of isolated virus (16) provide evidence that the N termini of VP1 and VP4, which are regions located inside the viral capsid (Fig. 1C), are reversibly exposed in the mature capsid, and suggest this externalization is part of the initial stages of uncoating. Notably, in the presence of WIN compounds these regions are not proteolyzed, and thus the motions leading to the exposure of these N termini are dampened, consistent with the activity of WIN compounds being to inhibit uncoating.

The reversible externalization of interior regions of VP1 and VP4, viral uncoating, and the inhibition of these processes by WIN together infer large-scale, concerted motions of the capsid. Further, RNA, VP4, and the N terminus of VP1 are suggested to exit the capsid at the fivefold symmetry axis (17–21) or an interface near the twofold axis (22–24), so that WIN binding in a pocket distant to these sites indicates a long-range activity. These observations motivated MD studies of the solvated HRV 14 capsid, with and without WIN 52084 bound, to probe functional protein dynamics that might underlie the initial stages of the externalization process and uncoating and to further elucidate the physical basis of the long-distance antiviral activity. The atomic fluctuations observed from MD studies were analyzed for radially correlated motions between capsid residues. Radial cross-correlation was examined rather than the more commonly used displacement vector cross-correlation (DCC) to overcome the dependence of the later on directionality (25) (see *SI Appendix*). We introduce a framework to analyze long-distance, concerted motions using a network based on radial cross-correlation coefficients. Potential pathways underlying the motions were traced in the radial correlation network by using a modification of Dijkstra’s graph searching algorithm (26). The resulting important paths involve residues at spontaneous drug-resistant mutation sites and were sensitive to the presence of the WIN compound. This framework based on a radial correlation network has allowed the previously undescribed identification of correlated motion over a long distance from an MD simulation, and allowed insights into the molecular mechanism of antiviral activity.

Results and Discussion

To investigate large scale, concerted motions of the HRV 14 capsid, trajectories were computed using rotational boundary

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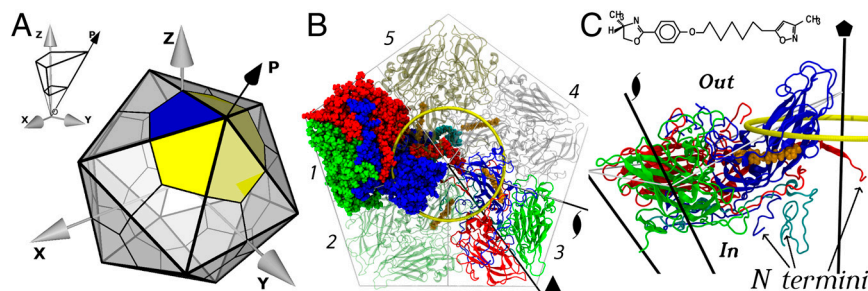


Figure 1. (A) Schematic of an icosahedron with 20 triangular tiles. Each tile has three asymmetric units corresponding to the protomer of the HRV 14 capsid (blue area). The Z axis is coincident with one of the twofold symmetry axis. In this study the pentamer, or five protomers centered around a fivefold symmetry axis, is the unit cell (blue and yellow areas). Inset shows orientation of one protomer in the unit cell. Neighboring protomers are generated using symmetry operators. (B) Top view of five protomers in the primary unit of simulation. Protomer 1 is shown in space-filling spheres, and protomer 2–5 are shown as ribbon drawings. In protomer 1 and 3 VP1 is shown in blue, VP2 in green, VP3 in red, and VP4 in cyan. WIN 52084 is shown in volume representation in gold. (C) Side view of protomer 1. N termini of VP1 and VP4 are the innermost residues and lie on the inside of the capsid. The N termini from five VP3 molecules together form a β -annulus (not shown) at the fivefold symmetry axis. The fivefold, threefold, and twofold symmetry axes are indicated by the usual symbols. The yellow circle, 35 Å from the fivefold symmetry axis, represents the approximate position of the canyon. Chemical structure of WIN 52084 is shown.

symmetry conditions (27–31) with a solvated viral pentamer as the asymmetric unit for simulation. Five copies of the protomer centered at the fivefold axis (Fig. 1 *A* and *B*) accurately models microscopic dynamics of not only the WIN-binding pocket but also the region around the fivefold symmetry axis. Trajectories were calculated starting from the crystallographic coordinates of either HRV 14 (32) or HRV 14 with WIN 52084 bound (33) (see *SI Appendix*). The last 2 ns of 10 3-ns trajectories were used for analysis, for a total time equal to 20 ns for HRV 14 trajectories, referred to as T_{nowin} , and 20 ns for HRV 14-WIN 52084 trajectories, referred to as T_{win} . Confidence intervals, CI, of time-averaged quantities were obtained from the bootstrapping method (see *SI Appendix*).

Long-Range Correlations. Reasoning that protein externalization and uncoating involve motions with a radial directionality, we examined the correlations in the distance from the capsid center among pairs of C_α atoms. A breathing motion is reflected in such a radial correlation coefficient in contrast to the DCC, which is generally diminished by angular averaging (25) (see [SI Appendix](#)). The absolute radial correlation coefficient, or absolute normalized radial covariance, $C_R(i, j)$ (see *Materials and Methods*), and the associated 95% CI were determined for pairs of C_α atoms from T_{nowin} and T_{win} .

To identify concerted motions over large spatial scales, we consider $C_R(i, j)$ values for C_α atoms of noninteracting residue pairs—i.e., those with a minimum distance between residues greater than the nonbond cutoff distance 14 Å. The distributions for the $C_R(i, j)$ values with 95% CI greater than 0.6 from T_{nowin} and T_{win} are shown in Fig. 2, blue and red curves, respectively, as a function of the distance between the two C_α atoms. The time-average values for $C_R(i, j)$ are well converged within 1 ns, and only a small fraction of the total C_α - C_α radial correlations are greater than 0.6 (see [SI Appendix](#)). We find that a large number of radially correlated C_α - C_α pairs exist for HRV 14 in T_{nowin} with the majority from pairs separated by 14 to 30 Å. In striking contrast, the corresponding $C_R(i, j)$ distribution for HRV 14-WIN from T_{win} is overall greatly reduced. Moreover, many of the T_{nowin} pairs with large radial correlation were separated by distances greater than 45 Å and some with distances as large as 85 to 90 Å. $C_R(i, j)$ values ≥ 0.8 were observed for C_α - C_α pairs at distances greater than 55 Å. This was not the case for T_{win} ; many fewer C_α - C_α pairs separated by long distances have a 95% CI for $C_R(i, j)$ greater than 0.6. In addition, the radially correlated C_α - C_α pairs separated by distances greater than 45 Å are largely nonoverlapping sets for T_{nowin} and T_{win} , as shown by the dotted black line in Fig. 2. This dotted line is the distribution of C_α - C_α

pairs present in the T_{nowin} distribution of Fig. 2 (blue curve) and have a 95% CI for $C_R(i, j)$ that is less than 0.6 in T_{win} . The dotted black curve nearly overlaps the blue curve, demonstrating that these correlated C_α - C_α pairs in T_{nowin} are not as correlated in T_{win} .

It has long been suggested that RNA, VP4, and the N terminus of VP1 exit the capsid at the fivefold symmetry axis (17–21), although recent cryoelectron microscopy results on the closely related poliovirus, another member of the enterovirus genus, suggest RNA exits at an interface near the twofold symmetry axes (22–24) and the N terminus of VP1 exits through an opening at the base of the canyon (26). To ask if the long-distance radial correlations shown in Fig. 2 might reflect dynamics associated with breathing, uncoating, and WIN-binding effects, we identify radially correlated pairs that have one C_α atom in the region of the WIN-binding pocket or within 35 Å of the fivefold axis (yellow ring in Fig. 1 *B* and *C*). This distribution is shown in Fig. 3*A* for T_{nowin} and T_{win} . While the T_{win} distribution (red curve) is overall reduced and shows little structure beyond 40 Å, the long-distance radially correlated pairs from T_{nowin} (blue curve) fall into three groups centered at 46 Å, 64 Å, and 84 Å, designated *i*, *ii*, and *iii*, respectively. These groups are mapped onto the structure in Fig. 3*B* and *C*; for each pair in the group, the C_α near the fivefold axis is indicated with a blue sphere drawn on one of the five protomers, and the second C_α is a sphere colored green for group *i*, gold for group *ii*, and red for group *iii*. Residues surrounding the fivefold axis are highly correlated with residues near the fivefold but in the neighboring protomer (green spheres). Also observed are radial correlation with residues in the vicinity of the closest twofold axis (green spheres) and all other twofold

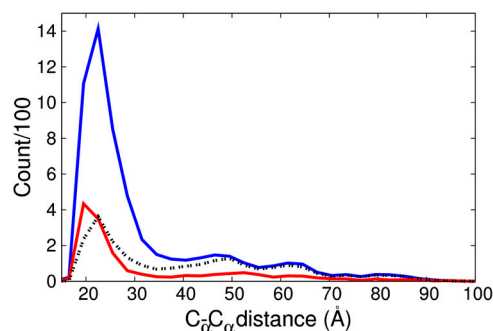


Figure 2. Distribution of all nonneighbor C_α pairs with 95% CI of $C_R(i, j) > 0.6$ from T_{nowin} (blue) and T_{win} (red) (see text for explanation of T_{nowin} and T_{win}) as a function of intrapair C_α distance.

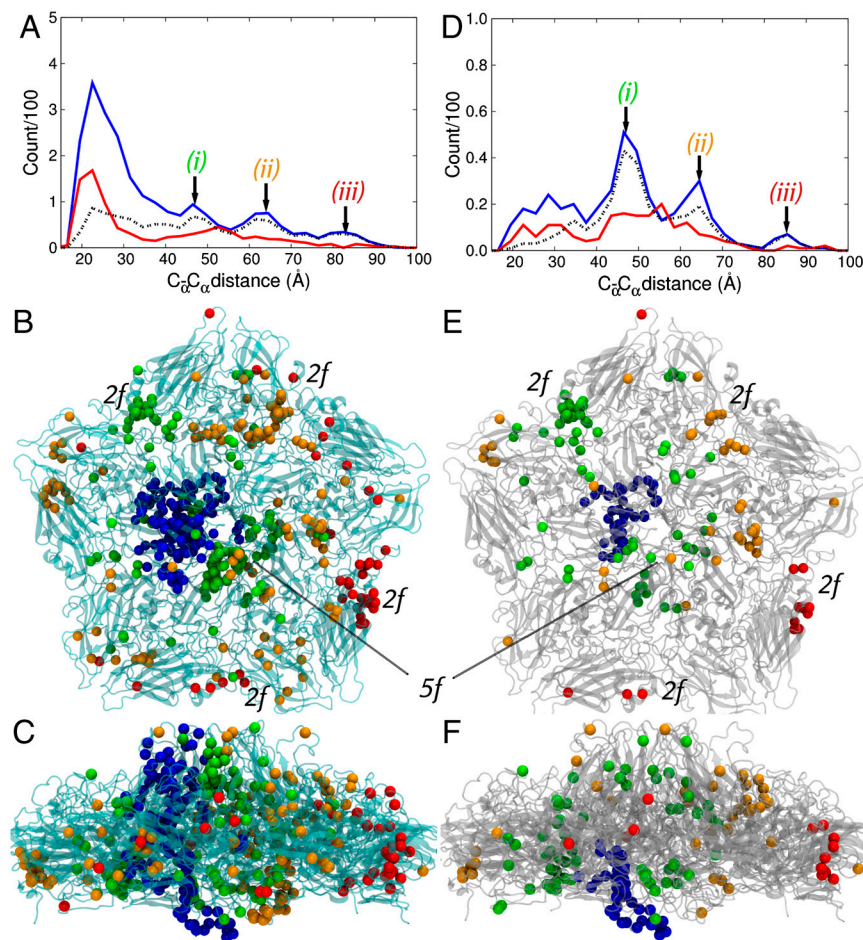


Figure 3. (A) Distribution of nonneighbor C_α pairs from Fig. 2 with at least one C_α within 35 Å of the fivefold symmetry axis (the yellow circle in Fig. 1). (D) C_α pairs present in A with at least one C_α from N termini of VP1 (residues 1001–1015) or VP4 (residues 4001–4040) are included. Long-distance radially correlated pairs in A fall into three groups centered at 46 Å, 64 Å, and 84 Å, designated *i*, *ii*, and *iii*, respectively. These groups are mapped onto the structure in B and C. For each pair in the group, the C_α near the fivefold axis is represented by a blue sphere drawn on one of the five protomers, and the second C_α is a sphere colored green for group *i*, gold for group *ii*, and red for group *iii*. D–F are similarly formatted for regions *i*, *ii*, and *iii* in B. Long-distance radial correlation for residues surrounding the fivefold axis with residues near fivefold but in other protomers and with residues in the vicinity of twofold axes as marked with 5f and 2f, respectively.

axes across the pentamer (gold and red spheres). The higher densities of long-range radially correlated motions in T_{nowin} are therefore between residues in the WIN pocket and residues in regions near the fivefold and twofold symmetry axes. Moreover, as noted above, these correlations are lost in the presence of WIN, so that the behavior is suggestive of functional motions related to externalization and uncoating at the fivefold axis as long proposed (17–21) as well as near the twofold axes as more recently reported (22–24).

The radial correlation in groups *i*, *ii*, and *iii* in T_{nowin} largely involve residues from the reversibly externalized N-terminal regions of VP1 or VP4; however, these radial correlations are not present in T_{win} . Fig. 3D displays the subset of the distribution in Fig. 3A corresponding to C_α - C_α pairs with one C_α from either VP1 (residues 1001–1015) or VP4 (residues 4001–4040). The curves are colored as in Fig. 3A. Because the dotted black curve in Fig. 3D closely follows the blue curve from T_{nowin} for distances >40 Å, most of these long-distance C_α - C_α pairs with large radial correlation coefficients in T_{nowin} are not radially correlated in T_{win} . As visualized in Fig. 3E and F, these VP1 or VP4 residues with long-distance radial correlations in T_{nowin} but not in T_{win} are primarily correlated with residues near the neighboring twofold axis (green spheres) or more distant twofold axes (gold and red spheres). These radial correlations are indicative of concerted motions of these innermost regions of VP1 and VP4 spanning distances of 85 Å.

Identification of Correlation Paths. What are the underlying origins of the radial correlations occurring over distances as large as 90 Å? That these correlations exist in free HRV 14 but are largely dampened in the presence of WIN 52084 suggests that identifying

the origin of the radial correlations could provide information toward the mechanism for transient externalization, or breathing, and perhaps the uncoating process.

To answer the question, we developed a method for detecting the link between two C_α atoms based on a modified version of

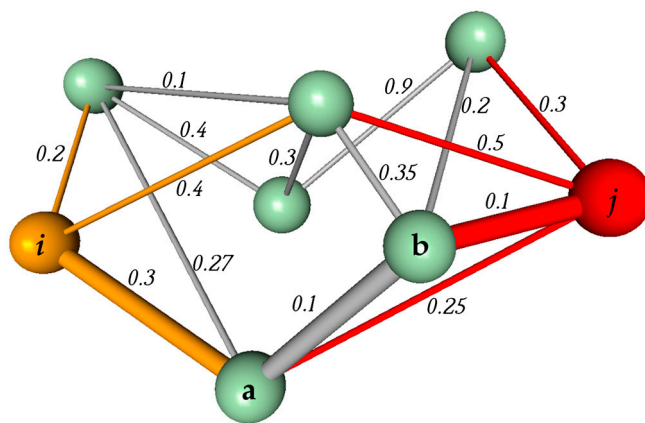


Figure 4. A simplified network. Each node in the network corresponds to a C_α atom of a residue. Two nodes are connected by an edge if atoms in the corresponding residues are within 14 Å during the simulation. Node *i* is connected with its neighbors through orange color edges and node *j* through red color edges. All other edges are shown in gray. Weight of an edge $\bar{i}a$, $W_{ia} = 1 - C_R(i, a)$, is written next to the edge. Weight of path $\bar{i}ab$, $W_{iab} \equiv W_{ia} \otimes W_{ab} \equiv 1 - C_R(i, a) \cdot C_R(a, b)$. Shortest path between two nodes *i* and *j* is $\bar{i}abj$, the path with minimum $W_{i,j}$.

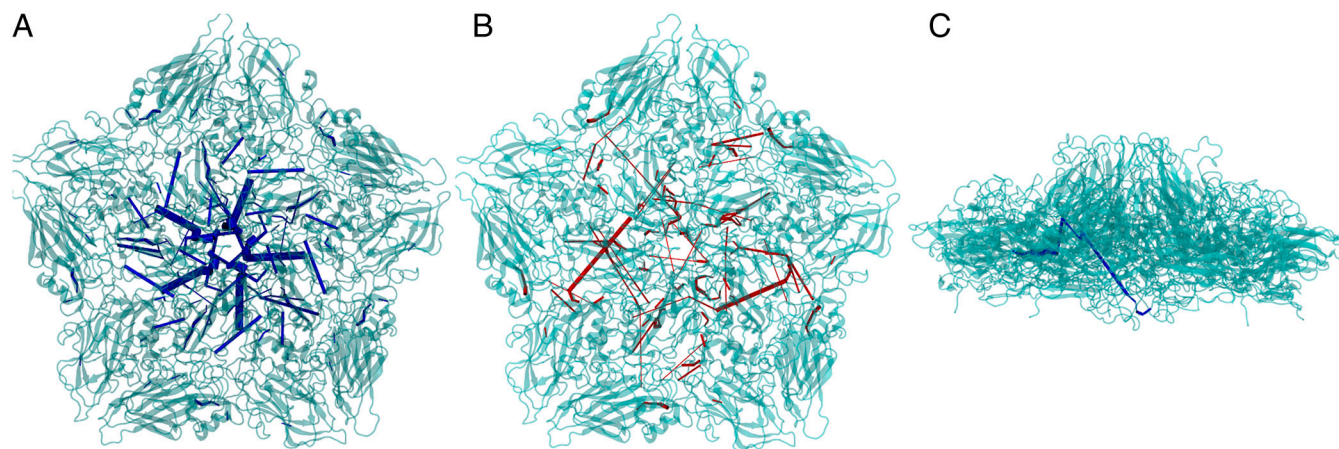


Figure 5. Edges with 95% confidence interval of betweenness >0.0005 are shown with their thickness proportional to their betweenness for T_{nowin} in A and for T_{win} in B. Betweenness is the number of occurrences of an edge relative to the total number of paths. Highest betweenness through any C_{α} pair are 0.0056 and 0.0027 in T_{nowin} and in T_{win} , respectively. (C) A sequence of edges with high betweenness connecting N terminus of VP4 (residue 4008 of protomer 1) near fivefold symmetry axis to a residue across canyon (residue 1254 of protomer 3).

Dijkstra's graph searching algorithm (26). The nodes of the network correspond to C_{α} atoms and edges connecting all C_{α} atoms belonging to residues within the nonbonded distance of 14 Å (Fig. 4). To capture the radial correlation behavior, an edge between $C_{\alpha i}$ and $C_{\alpha j}$ was assigned a value equal to $1 - C_R(i, j)$. The path between any two nodes of the network, l and m , was determined from the minimum value of the weight $W_{l \rightarrow a_1 \dots a_n \rightarrow m}$ (see *Materials and Methods*). The weight of a path is specified as one minus the product of the radial correlation coefficients for all edges of the path so that the path with the minimum weight is the optimal path in terms of high radial correlation and fewest number of edges. This path is named hereafter the "shortest path." The shortest path was determined for all C_{α} - C_{α} pairs of the pentamer, or approximately 8×10^6 paths. The second step of the method to identify the origin of the radial correlations was to determine which path segments had the highest betweenness (34). Betweenness of an edge is the probability with which the edge occurred in all shortest paths, or the number of occurrences of the edge relative to the total number of paths. From the distribution of betweenness values, shown in *SI Appendix*, a small number of edges are observed to lie at the far edge of the distri-

bution for T_{nowin} by having considerably higher betweenness than other edges. In contrast, the betweenness through these edges is substantially reduced in T_{win} .

The component of the radial correlation network with highest betweenness is visualized by mapping the edges with the largest betweenness values onto the structure in Fig. 5A. The edges having a betweenness with a 95% CI >0.0005 are shown with blue lines of thickness proportional to betweenness. It is noted that all edges within the pentamer asymmetric unit are treated independently so that the near fivefold symmetry apparent in the blue segments of Fig. 5A is evolved from microscopic sampling. High-betweenness edges from T_{win} using the same cutoff value of 0.0005 are shown with red lines in Fig. 5B. The presence of WIN 52084 very clearly alters the observed patterns of betweenness; fewer red lines are observed and the overall thinner widths indicate smaller betweenness in general for T_{win} .

The patterns in Fig. 5 are striking. Each node of the network has close to a hundred or more edges so that the number of possible paths between two C_{α} atoms is large and increases dramatically as the distance of separation increases. Thus, an edge with highest betweenness, and more importantly, sequential edges of high betweenness are definite outliers. Sequential edges of highest betweenness are a linked set of radially correlated C_{α} atoms and suggest a mechanism for the long-range connectivity in Fig. 3. Numerous blue path segments are observed from T_{nowin} (Fig. 5A) and found to be concentrated around the canyon and the fivefold axis. The set of blue lines encircling the fivefold axis corresponds to the N-terminal region of VP3, which forms a well-ordered β -annulus through interprotomer interactions. This annulus is absent from the pattern of highest betweenness paths calculated from T_{win} when WIN is bound (Fig. 5B).

The paths connect radially correlated C_{α} - C_{α} pairs separated by long distances (Fig. 3) and are a likely origin for these radial correlations. An example of one such path is given in Fig. 5C, which shows sequential edges connecting VP4 residue 4008 near the fivefold symmetry axis with the VP1 residue 1254 across the canyon. As such, this path provides a linkage between residues of C_{α} - C_{α} pairs in group i Fig. 3C (green with blue spheres Fig. 3E and F). Moreover, this path does not exist in the presence of WIN 52084.

The 10 edges with the highest betweenness from T_{nowin} are listed in Table 1 by the residue numbers of the nodes delimiting the edge. These edges have a 95% CI of betweenness greater than 0.001. In contrast, their values from T_{win} are approximately two orders of magnitude smaller. All the residues in Table 1,

Table 1. Top 10 unique edges with lower and upper 95% CI of betweenness in T_{nowin} and corresponding betweenness in T_{win}

Res # ^{1*}	Res #*	Betweenness ^{2†} ($\times 100$)	
		T_{nowin} ^{3‡}	T_{win} ⁴
4026	4027	0.33 ^{0.56} 0.82	0.01 ^{0.09} 0.19
3006	3007	0.43 ^{0.55} 0.71	0.00 ^{0.01} 0.05
1012	4026	0.33 ^{0.49} 0.66	<0.001
3005	3006	0.25 ^{0.37} 0.49	0.00 ^{0.02} 0.04
1173	1219	0.22 ^{0.22} 0.23	<0.001
1249	1250	0.14 ^{0.21} 0.32	0.08 ^{0.10} 0.13
3005	3019	0.18 ^{0.20} 0.22	<0.001
1199	4015	0.19 ^{0.19} 0.22	<0.001
2241	2242	0.10 ^{0.18} 0.33	0.00 ^{0.02} 0.04
1071	3100	0.16 ^{0.17} 0.18	0.00 ^{0.00} 0.00

*Italicized residues are within nonbond cutoff distance of drug in T_{win} . All the residues, except 2241, 2242, 3005, and 3006, are conserved or vary by one residue in HRV-B. Underlined residues are conserved or vary by one residue in HRV-A. Bold faced residues are drug resistant mutants.

†Betweenness is the number of occurrences of an edge relative to the total number of paths. Variability in betweenness was calculated using bootstrap method.

‡The 95% CI is shown in superscript.

other than 2241, 2242, 3005, and 3006, are conserved or vary by one amino-acid type substitution among HRV-B serotypes, of which HRV 14 is a member. The underlined residues in Table 1 are similarly conserved in HRV-A. Of the 15 residues in Table 1, two (1199 and 1219) are in the WIN-binding pocket of the capsid, and an additional eight (1071, 1173, 1249, 1250, 3005, 3006, and 3007) are within 14 Å of WIN 52084 bound in the cavity.

Conclusion

The uncoating process, a critical part of enveloped picornaviral infection, requires large changes in the capsid conformation. WIN antiviral compounds disrupt uncoating and protect virus particles against thermal loss of VP4 (7) and thus are presumed to prevent these conformational changes. Several experimental observations of the native-state capsid detect large-scale reversible fluctuations that are likely relevant to this uncoating process (16, 19). Antibody epitope sites (15) and limited proteolysis (16) indicate that the N-terminal regions of VP1 and VP4 are reversibly exposed from inside the viral capsid and provide evidence that the mature intact viral capsid undergoes large spatial-scale dynamics. The uncoating process involves the externalization of these same protein regions; the small VP4 protein is lost in its entirety during infection (13, 20), and the N terminus of VP1 becomes exposed (14). The exposed peptides are thought to facilitate membrane permeability (14), and the N terminus of VP1 was shown to insert into membranes and considered important for tethering the virus particle during endocytosis (35). Further the WIN antiviral compound diminish the large-scale motions of the capsid detected by proteolysis, which also links the breathing motion to uncoating. Together, these results argue that the reversible large-scale, breathing motions of the intact native virus particle are relevant to the uncoating process and that WIN compounds can be used to interrogate these dynamics.

Here, an analysis of MD simulations of HRV 14, without and with WIN 52084 bound, revealed large-scale concerted motions of the capsid that reasonably contribute to the initial events that lead to breathing and potentially uncoating. Radial motions of residues of HRV 14 without WIN separated by distances as large as 90 Å were found to be highly correlated (Fig. 2). Many of these radial correlations occur between residues within 35 Å of the fivefold axis, including the canyon region, and either a residue in the vicinity of the fivefold axis or a residue near a twofold axis that is nearby or across the pentameric unit. Sequential edges of the correlation paths with highest betweenness were found to connect these distant regions in HRV 14 (blue lines in Fig. 5A). These pathways are concentrated around the fivefold axis and the canyon region and extend to regions near the twofold symmetry axes regions where the RNA and VP4 are considered likely to exit the capsid (17–24).

Importantly, the presence of WIN 52084 dampens the radial correlations and destroys many of the highest-betweenness paths surrounding the fivefold axis (red lines, Fig. 5B), as would be predicted from the antiviral activity of inhibiting the uncoating process and blocking the breathing motion. The results therefore suggest the long-range basis for the WIN antiviral activity is to interrupt local interactions that are necessary for the highest-betweenness correlation paths. This effect of WIN on the large-scale capsid dynamics could act in concert with an entropic effect on the virus capsid predicted previously (36) from MD simulation studies of the HRV capsid. That is, binding the hydrophobic WIN compound in the buried pocket of VP1 was predicted to entropically stabilize the capsid, a prediction later supported by experiment (37). With the reasoning that long-range concerted motions are lower entropy and that disruption of the correlation paths by WIN could lead to an increase in entropy, the possibility of an entropic effect upon WIN binding was examined using a quasi-harmonic analysis of the configurational entropy (38) of T_{nowin} and T_{win} . Although the error from such an estimate is large, we

find that the HRV14 capsid with WIN bound is higher entropy (SI Appendix, Fig. G1). Thus, WIN binding could both stabilize the intact capsid by increasing the configurational entropy and also disrupt capsid interactions essential for the concerted dynamics leading to uncoating.

The paths of sequential edges with highest betweenness illustrated by the blue lines in Fig. 5A encompass a number of conserved residues (Table 1). Two of these, 1199 and 1219, are associated with antiviral activity and uncoating (39) as well as known to alter breathing (16). Together, the pattern of radial correlations and highest-betweenness paths composed of conserved residues, and the loss of this pattern when WIN is bound strongly suggest these paths are the origins of the radial correlations and part of the functional motion leading to uncoating.

Long-distance, correlated motions are a candidate mechanism for allostery in proteins. Nonetheless, such motions are often elusive in simulation studies (40); DCC are a function of the angle between centered vector variables (25) and insensitive to orthogonal displacements (41) (see SI Appendix A). Cross-correlation coefficients derived from dihedral angles are even less sensitive for detecting correlated motion (42). To circumvent this problem, we used radial cross-correlation coefficients, which defined numerous very long-distance correlations in capsid protein dynamics.

The insensitivity of displacement vector cross-correlation to identify long-distance effects motivated the development of network based approaches. Networks built from protein structures alone provide topological analysis that can give information on structural stability and binding sites (43). Another approach that has been used to investigate allostery and long-distance communication is a network using low-frequency fluctuations from elastic network normal mode analysis (ENMA) (44, 45). However ENMA is most useful for such analysis of binding effects in the presence of large structural changes (46). This is not the case with WIN binding HRV 14; the root mean square deviation between C_{α} atoms of average structures from T_{nowin} and T_{win} is only 1.32 Å. Indeed, our efforts to use elastic network normal mode calculations were not fruitful and found no significant difference in low-frequency modes of HRV and HRV-WIN 52084. Finally, a network derived from interaction energy correlations was reported to identify coupling over long-distance in signaling proteins (47, 48). Correlations in energy reflect interactions that reasonably lead to concerted motion but do not provide any direct information on that motion. The radial correlation network approach reported here offers an alternative method to query long-distance correlation paths from concerted motions.

Materials and Methods

Initial coordinates were from crystallography (PDB ID code 4RHV for HRV 14 and 1RUD for HRV 14-WIN). Modeling of missing coordinates and protocol of MD simulation are detailed in SI Appendix.

Each C_{α} atom was represented by a node in the network. WIN 52084 was represented by the first carbon atom on the right of the benzene ring in Fig. 1C. Two nodes are connected by an edge if any atom of the corresponding residues are within 14 Å in at least one frame of the 10 trajectories. An edge is assigned a weight calculated from the radial correlation of the C_{α} atoms, $C_R(i, j)$,

$$C_R(i, j) = \frac{|c_R(i, j)|}{\sqrt{\langle (R_i - \langle R_i \rangle)^2 \rangle \langle (R_j - \langle R_j \rangle)^2 \rangle}}$$

where

$$c_R(i, j) = \langle (R_i - \langle R_i \rangle)(R_j - \langle R_j \rangle) \rangle. \quad [1]$$

where, R_i is the distance of the C_{α} atom of the i th residue from the origin at an instance and $\langle \dots \rangle$ denotes the ensemble average. The weight of an edge connecting two neighboring nodes i and j , W_{ij} , is $1 - C_R(i, j)$.

A path in the network between two C_α atoms, or nodes, consists of one or more edges (Fig. 4). If nodes i and j are not neighbors and there exists a path $\bar{ia}_1...a_nj$, where $a_1...a_n$ are nodes between i and j and $n \geq 1$, then the weight of the path $\bar{ia}_1...a_nj$ is

$$W_{\bar{ia}_1...a_nj} \equiv 1 - C_R(i, a_1) \cdot \dots \cdot C_R(a_{n-1}, a_n) \cdot C_R(a_n, j). \quad [2]$$

The shortest path or path with least weight, between all nonneighbor pairs of nodes is found using an algorithm developed by Dijkstra (26) with edge

weights modified to include the radial correlation defined by Eq. 2. The betweenness of an edge is the fraction of all possible shortest-paths that include the edge.

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Supporting information: Long-distance correlations of rhinovirus capsid dynamics contribute to uncoating and antiviral activity.

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Appendix A: Cross-correlation

Angular dependence of displacement vector cross-correlation

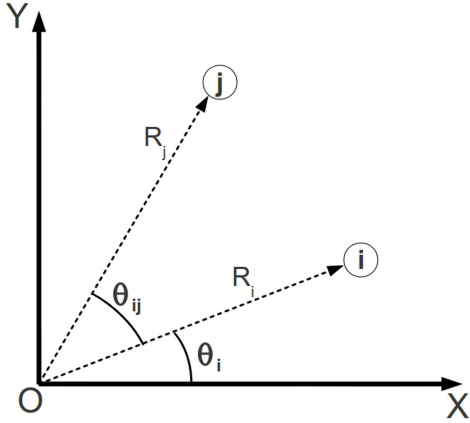


Figure A1: Two particles, i and j , are fluctuating in a two dimensional space. \mathbf{R}_i and \mathbf{R}_j are their position vectors at an instance. R_i makes an angle θ_i with X axis and \mathbf{R}_j makes an angle θ_{ij} with \mathbf{R}_i .

Covariance is a measure of how much two variables change together. Cross-correlation coefficient between two variables is defined as the covariance of the two variables divided by the product of their standard deviations. Cross-correlation is mainly sensitive to a linear relationship between two variables. Hence cross-correlation of vector quantities depends on the angle between the vectors.

Let two particles, i and j , are fluctuating in a two dimensional space as shown in Fig. A1 and $\{\mathbf{R}_i\}$ and $\{\mathbf{R}_j\}$ are ensemble of their position vectors. Let $\{\theta_i\}$ is the ensemble of angles $\{\mathbf{R}_i\}$ makes with X axis and $\{\theta_{ij}\}$ is the ensemble of angle between $\{\mathbf{R}_i\}$ and $\{\mathbf{R}_j\}$. Position vector \mathbf{R}_i and \mathbf{R}_j at an instance can be written as

$$\begin{aligned}\mathbf{R}_i &= X_i\hat{x} + Y_i\hat{y} \\ &= R_i\cos\theta_i\hat{x} + R_i\sin\theta_i\hat{y}\end{aligned}\tag{a1}$$

similarly,

$$\mathbf{R}_j = R_j\cos(\theta_{ij} + \theta_i)\hat{x} + R_j\sin(\theta_{ij} + \theta_i)\hat{y}$$

where \hat{x} and \hat{y} are unit vectors along X and Y axes respectively and X_i and Y_i are projections of \mathbf{R}_i along X and Y axes respectively. Similarly X_j and Y_j are projections of \mathbf{R}_j along X and Y axes respectively. Then covariance of displacement $c(i, j)$ between i and j is

$$\begin{aligned}
c(i, j) &= \langle (\mathbf{R}_i - \langle \mathbf{R}_i \rangle) \cdot (\mathbf{R}_j - \langle \mathbf{R}_j \rangle) \rangle \\
&= \langle X_i X_j \rangle + \langle Y_i Y_j \rangle - \langle X_i \rangle \langle X_j \rangle - \langle Y_i \rangle \langle Y_j \rangle \\
&= \langle R_i \cos \theta_i R_j \cos(\theta_{ij} + \theta_i) \rangle + \langle R_i \sin \theta_i R_j \sin(\theta_{ij} + \theta_i) \rangle - \\
&\quad \langle R_i \cos \theta_i \rangle \langle R_j \cos(\theta_{ij} + \theta_i) \rangle - \langle R_i \sin \theta_i \rangle \langle R_j \sin(\theta_{ij} + \theta_i) \rangle
\end{aligned} \tag{a2}$$

and cross-correlation coefficient of displacement, $C(i, j)$, is

$$C(i, j) = \frac{c(i, j)}{\sqrt{\langle (\mathbf{R}_i - \langle \mathbf{R}_i \rangle)^2 \rangle \langle (\mathbf{R}_j - \langle \mathbf{R}_j \rangle)^2 \rangle}} \tag{a3}$$

where $\langle \dots \rangle$ denotes ensemble average. If R_i and R_j are statistically independent of θ_i and θ_{ij} then we can rewrite eqn a2 as

$$\begin{aligned}
c(i, j) &= \langle R_i R_j \rangle \langle \cos \theta_i \cos(\theta_{ij} + \theta_i) + \sin \theta_i \sin(\theta_{ij} + \theta_i) \rangle - \\
&\quad \langle R_i \rangle \langle R_j \rangle \{ \langle \cos \theta_i \rangle \langle \cos(\theta_{ij} + \theta_i) \rangle + \langle \sin \theta_i \rangle \langle \sin(\theta_{ij} + \theta_i) \rangle \} \\
&= \langle R_i R_j \rangle \langle \cos \theta_{ij} \rangle - \\
&\quad \langle R_i \rangle \langle R_j \rangle \{ \langle \cos \theta_i \rangle \langle \cos(\theta_{ij} + \theta_i) \rangle + \langle \sin \theta_i \rangle \langle \sin(\theta_{ij} + \theta_i) \rangle \}
\end{aligned} \tag{a4}$$

From eqn a2 it is clear that $c(i, j)$ vanishes if we fix θ_{ij} to 90° . Furthermore if θ_{ij} and θ_i are statistically independent then

$$\begin{aligned}
c(i, j) &= \langle R_i R_j \rangle \langle \cos \theta_{ij} \rangle - \\
&\quad \langle R_i \rangle \langle R_j \rangle \{ \langle \cos \theta_i \rangle [\langle \cos \theta_i \rangle \langle \cos \theta_{ij} \rangle - \langle \sin \theta_i \rangle \langle \sin \theta_{ij} \rangle] + \\
&\quad \langle \sin \theta_i \rangle [\langle \sin \theta_i \rangle \langle \cos \theta_{ij} \rangle + \langle \cos \theta_i \rangle \langle \sin \theta_{ij} \rangle] \} \\
&= \{ \langle R_i R_j \rangle - \langle R_i \rangle \langle R_j \rangle [\langle \cos \theta_i \rangle^2 + \langle \sin \theta_i \rangle^2] \} \langle \cos \theta_{ij} \rangle
\end{aligned} \tag{a5}$$

Covariance, hence cross-correlation coefficient, of displacement depends on θ_{ij} , the angle between two displacement vectors.

Radial correlation

Cross-correlation of displacement in Cartesian coordinate (DCC) is most sensitive when θ_{ij} is around 0° or 180° and not suitable to describe correlation in fluctuation of a spherically symmetric assembly of particles. In a spherically symmetric assembly of particles $C(i, j)$ will fail to capture correlation between perpendicular fluctuations and overemphasize correlation between linear fluctuations. To overcome insensitivity of $C(i, j)$ to radial fluctuation we define radial correlation, $C_R(i, j)$, as

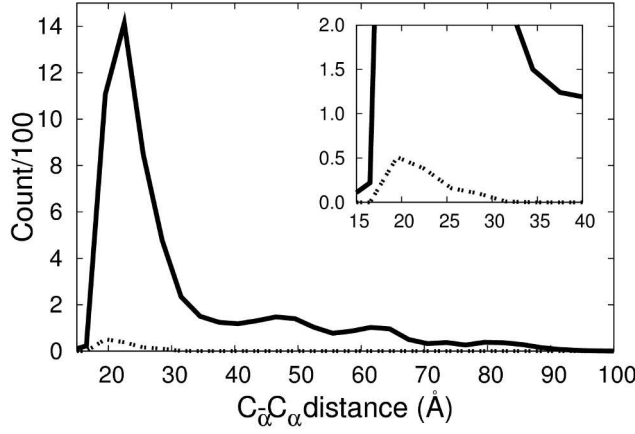


Figure A2: Distribution of non-neighbor C_α pairs with 95% confidence interval (CI) of radial correlation coefficient, $C_R(i, j)$, > 0.6 as a function of intra-pair C_α distance in T_{nowin} (solid). Distribution of same pairs with cross correlation of displacement > 0.6 for T_{nowin} is shown with dotted line. Cross-correlation of displacement fails to catch long-distance correlation.

$$C_R(i, j) = \frac{|c_R(i, j)|}{\sqrt{\langle (R_i - \langle R_i \rangle)^2 \rangle \langle (R_j - \langle R_j \rangle)^2 \rangle}}$$

where

$$c_R(i, j) = \langle (R_i - \langle R_i \rangle)(R_j - \langle R_j \rangle) \rangle$$

$$= \langle R_i R_j \rangle - \langle R_i \rangle \langle R_j \rangle. \quad (\text{a6})$$

$C_R(i, j)$ is most sensitive to radial as well as linear fluctuations but insensitive to tangential fluctuations. Distribution of DCCs of displacement and C_{RS} of non-neighboring C_α pairs in T_{nowin} , 20 ns trajectories each of HRV 14, against intra pair distance are shown in Fig A2 in dotted and solid lines respectively. Non-neighboring C_α pairs are from residues outside nonbond distance of 14 Å of each other. DCCs fail to capture long distance correlations.

Appendix B: Homology modeling of missing HRV 14 coordinates

The crystal structure of human rhinovirus (HRV) 14, PDBID: 4RHV [1], has missing coordinates for residues 1001 to 1016 of VP1, 2001 to 2007 of VP2 and 4001 to 4028 of VP4. the missing coordinates were modeled from HRV 16 (PDBID 1AYM [2]) and poliovirus (PDBID 1HXS [3]). VP1 residues were modeled from HRV 16 which has 43% sequence identity and 60% sequence similarity with VP1 of HRV 14. Secondary structure prediction of the missing coordinates of VP1 of HRV 14 matches exactly with the determined secondary structure of HRV 16. The crystal structure of polio virus, has no missing coordinates in VP4. It has 57% sequence identity and 75% sequence similarity with VP4 of HRV 14. Coordinates of residue 4001 to 4029 of VP4 of 4RHV were transferred from poliovirus. Missing coordinates of VP2 were not modeled as we could not find any template with known coordinates for the modeling.

The energy of the modeled residues was minimized while maintaining the known 4RHV crystallographic coordinates fixed. While still keeping the known atomic positions fixed, in vacuum NVE molecular dynamics (MD) simulations were performed to raise the temperature of the modeled regions over a 490 ps period from 100 K to 5000 K, the system was annealed at 5000 K for a 50 ps period, and then cooled to 300 K over a 980 ps period. Twenty modeled structures, ten each for viral capsid with and without drug, generated from twenty independent annealing and subsequent cooling MD calculations were used as initial coordinates for MD trajectory calculations.

Appendix C: Molecular dynamics

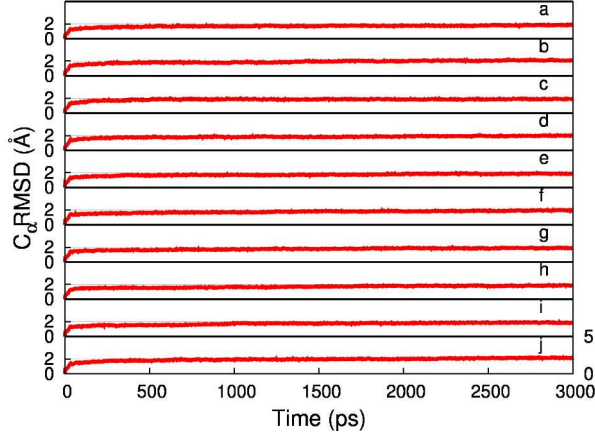


Figure C1: C_α RMSD of coordinates of ten trajectories in T_{nowin} with respect to the initial structures of each trajectory. For last 2 ns time period RMSD value remained around 2 Å.

an explicit shell of water constrained by outside and inside spherical boundaries. Water molecules were constrained within the outer and inner radii by applying spherical quadratic potentials referenced 170 Å and 85 Å, respectively. The spherical quadratic potential was setup with a well depth of -0.25 kcal/mol at 1 Å from the reference distance followed by a smoothly rising repulsion. Solvated pentamer contained $\approx 140,000$ atoms.

Neighboring protomers were generated using icosahedral boundary conditions implemented with the IMAGES facility within CHARMM. The detail implementation of icosahedral boundary condition is explained, in detail elsewhere [6]. Image atoms within 16.0 Å of a primary atom were included in the non-bonded pair list. Updates of image and non-bonded lists were made heuristically. In each of the MD calculations capsid was equilibrated for 1 ns before collecting data for another 2 ns period. During the 2 ns time period root mean square deviation (RMSD) values of the crystallographic coordinates w.r.t. the initial structures remained around 2 Å. RMSD values of trajectories of HRV 14 are shown in Fig C1.

Appendix D: Bootstrap

Bootstrap is a statistical procedure to learn about sampling variation using one set of observations [7]. Given ten independent 2 ns long trajectories, to find the variability in an observable μ , such as $C_R(i, j)$ or betweenness, a new set of ten 2 ns long trajectories is made by randomly choosing ten trajectories from the original pool, where a single trajectory is allowed to appear more than once. A new estimate $\hat{\mu}^*$ is calculated from the mean value of the new set. This procedure is repeated n times to generate the bootstrap distribution containing n values of $\hat{\mu}^*$. The bootstrap distribution is then used to calculate the 95% confidence interval (CI) of the true mean μ from the mean $\hat{\mu}$ of the original ten trajectories and n values of $\hat{\mu}^*$ from bootstrap distribution.

The $\rho\%$ CI of μ , is then given by

Starting from different annealed structures from modeling, ten 3 ns MD trajectories were calculated each for solvated viral capsid of HRV 14 without and with WIN 52084. The last 2 ns of the ten trajectories for HRV 14 and HRV 14-WIN 52084, referred as T_{nowin} and T_{win} respectively, were used for analysis. All MD calculations were performed using the CHARMM program [4] with constant volume and energy (NVE ensemble). A force switching function [5] was used to smoothly truncate electrostatic and van der Waals non-bonded forces with a cut-off of 14.0 Å. The covalent bonds to hydrogen atoms were constrained by the SHAKE algorithm. The equations of motion were integrated using the Verlet leap-frog algorithm with a time step of 1 fs. The unit cell of simulation was a pentamer containing five protomers solvated by

$$2\hat{\mu} - \hat{\mu}_{(n+1)(1-\alpha/2)}^* \leq \mu \leq 2\hat{\mu} - \hat{\mu}_{(n+1)\alpha/2}^* \quad (\text{D1})$$

where α is $(1 - \rho/100)$ and $\hat{\mu}_p^*$ is the p th ordered value of the bootstrap distribution $\hat{\mu}_1^* \leq \hat{\mu}_2^* \leq \dots \leq \hat{\mu}_n^*$ [7]. For 95% CI, α is $(1 - 95/100) = 0.05$. With n being 399 in our case $\hat{\mu}_{(n+1)(1-\alpha/2)}^*$ and $\hat{\mu}_{(n+1)\alpha/2}^*$ are $\hat{\mu}_{390}^*$ and $\hat{\mu}_{10}^*$.

Appendix E: Distribution of radial correlation coefficients and betweenness

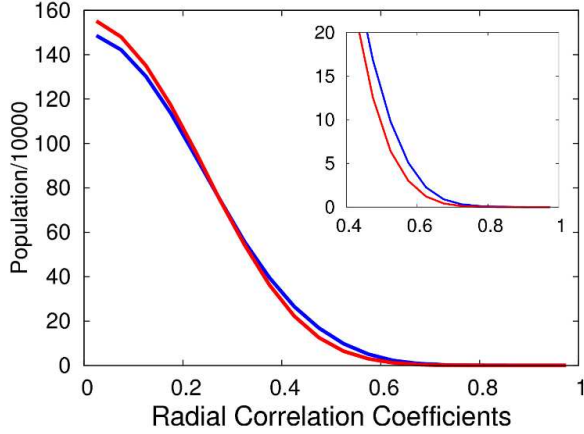


Figure E1: Distribution of C_R values for all possible C_α pairs of T_{nowin} and T_{win} are plotted with blue and red curve respectively. T_{win} has lesser number of pairs with high value of C_R than T_{nowin} . Values $C_R > 0.6$ are clear outliers. Inset shows a zoomed in region of the plot.

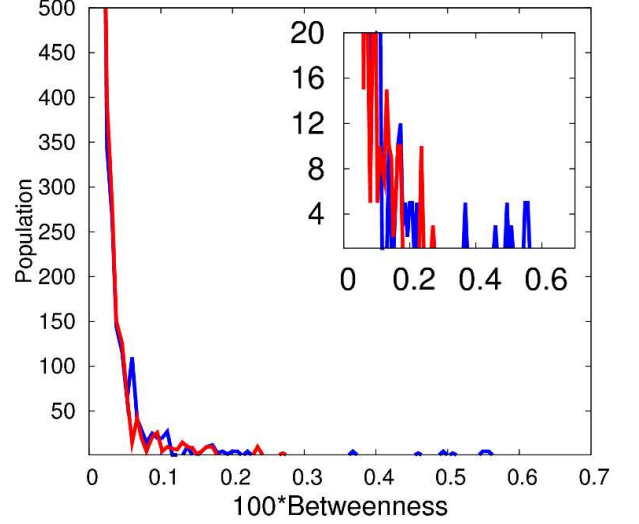


Figure E2: Number of edges as a function of betweenness in T_{nowin} and T_{win} are plotted in red and blue curve respectively. Betweenness of an edge is the number of occurrences of the edge relative to the total number of paths. Inset shows the same distribution with a magnified Y-axis. Edges with betweenness > 0.003 present in T_{nowin} are completely missing in T_{win} .

In this article we investigated radial correlation, C_R , between C_α pairs. Distribution of C_R values for all possible C_α pairs of T_{nowin} and T_{win} are plotted in Fig E1 with blue and red curve respectively. T_{win} has lesser number of pairs with $C_R \geq 0.4$ than T_{nowin} indicating overall loss of correlation with introduction of WIN52084. Values $C_R > 0.6$ are clear outliers in the distribution and indicate unusual highly correlated radial motion. Hence we concentrated our analysis on $C_R > 0.6$ for non-neighboring C_α pairs.

From a network, where the nodes are C_α atoms with edges between i, j neighboring nodes are weighted as $1 - C_R(i, j)$, we calculate the betweenness of each edge. Betweenness is the frequency an edge occurs in all shortest paths between two non-neighboring C_α s. The number of edges as a function of betweenness in T_{nowin} and T_{win} are plotted in Fig E2 with blue and red curve respectively. Edges with betweenness > 0.003 present in T_{nowin} are completely missing in T_{win} .

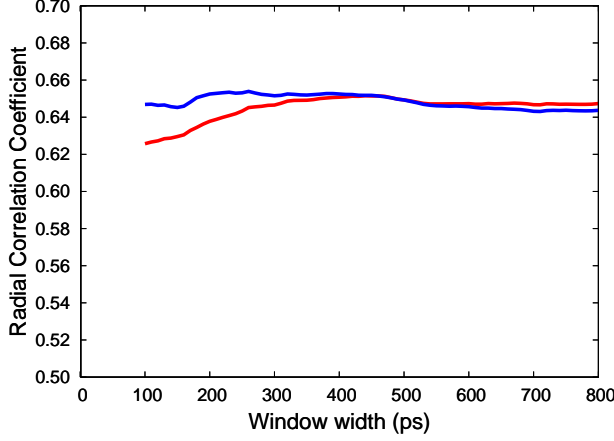


Figure F1: Average C_R , calculated from a window of varying width from the end of T_{nowin} trajectories for C_α pairs with final C_R value between 0.6 and 0.7. Neighboring and non-neighboring pairs are plotted with blue and red curve respectively. The value of C_R is converged for window for widths > 450 ps.

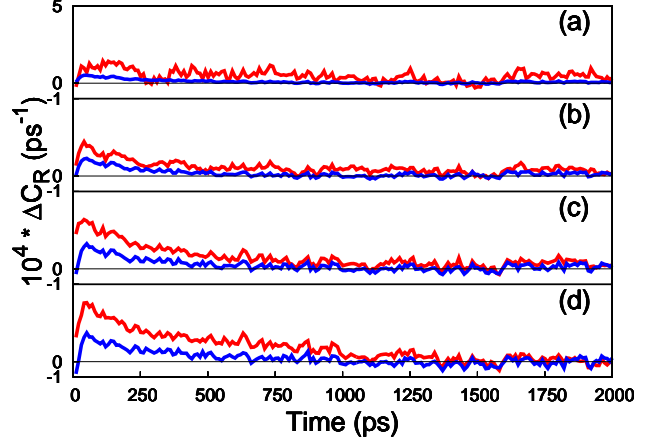


Figure F2: Values of ΔC_R calculated from a 950 ps window of ten HRV 14 trajectories, for non-neighboring (red) and neighboring (blue) pairs belonging to group a to d (see text), as the window being shifted by 10 ps from the beginning of trajectories. We consider C_R values > 0.6 has been converged around 1 ns.

Appendix F: Convergence of radial correlation coefficients

To investigate the convergence of values $C_R > 0.6$, we grouped all C_α pairs in to four groups, group a to d , according to whether their C_R values calculated from T_{nowin} is between interval $(0.9 - 1.0)$, $(0.8 - 0.9)$, $(0.7 - 0.8)$ or $(0.6 - 0.7)$ respectively.

To determine a window size over which the C_R stabilizes, average value of C_R for windows of different width from the end of 10 HRV 14 trajectories for neighboring and non-neighboring C_α pairs of group d are plotted in blue and red curve respectively in Fig F1. The initial increase of C_R in Fig F1 indicates statistical dependence of the data for window width < 450 ps. The C_R value is stabilizes for window width > 450 ps.

With a window of 950 ps we calculated values of C_R from ten trajectories of HRV 14 for a total average time of 9.5 ns for neighboring and non-neighboring C_α pairs. Starting from the initial step of the trajectory, the 950 ps window was shifted by 10 ps to calculate C_R . ΔC_R , changes in average C_R values, is plotted against the initial time of the moving window from 1 ps to 2050 ps, for group a to d in Fig F2a to Fig F2d respectively. ΔC_R for neighboring and non-neighboring C_α pairs are plotted with blue and red curve respectively. Convergence is assumed when ΔC_R values fluctuates around zero.

Non-neighboring residues are correlated via interactions through intermediate residues and as expected C_R between non-neighboring pairs converges slower than C_R between neighboring pairs. Also smaller C_R values require longer averaging time to separate the correlated fluctuation from random thermal fluctuation. ΔC_R for non-neighboring pairs of group d reaches zero around 1000 ps. We conclude the convergence of C_R values of interest has been achieved with 1 ns data from 10 HRV trajectories.

Appendix G: Entropy from vibrational modes

Vibrational frequency spectrum of a protein can be calculated from eigenvalues of mass weighted covariance matrix of the atomic Cartesian coordinates, \mathbf{A} , of the protein calculated from MD simulations.

$$\mathbf{A}\mathbf{V} = \lambda\mathbf{V} \quad (\text{G1})$$

where matrix \mathbf{V} is defined as the eigenvector matrix of \mathbf{A} and $\lambda = \{\lambda_\alpha\}$ is a diagonal matrix of the eigenvalues whose elements represent mean-square fluctuation (MSF) along the direction of the corresponding eigenvectors. Matrix \mathbf{A} is a $3N \times 3N$ dimensional matrix where N is number of atoms present in the protein. An element a_{ij} of matrix \mathbf{A} is defined as [8]

$$a_{ij} = \langle (q_i - \langle q_i \rangle)(q_j - \langle q_j \rangle) \rangle$$

where

$$q_i(t) = \begin{bmatrix} \cdot \\ \cdot \\ \cdot \\ (m_n)^{1/2}x_n(t) \\ (m_n)^{1/2}y_n(t) \\ (m_n)^{1/2}z_n(t) \\ \cdot \\ \cdot \\ \cdot \end{bmatrix} \quad (\text{G2})$$

The eigenvalues λ_α s are related to the frequency of vibrational modes ν_α s as

$$\lambda_\alpha = \frac{k_B T}{4\pi^2 \nu_\alpha^2} \quad (\text{G3})$$

The contribution of a vibrational mode, S_α^{vib} to the entropy of the protein is

$$S_\alpha^{vib} = -R \ln(1 - e^{-\frac{h\nu_\alpha}{k_B T}}) + \frac{N_A h \nu_\alpha}{T(e^{\frac{h\nu_\alpha}{k_B T}} - 1)} \quad (\text{G4})$$

where h is Planck's constant, N_A is Avogadro's number, R is gas constant and T is temperature of the protein. Vibrational entropy of a protein is then $S^{vib} = \sum_\alpha S_\alpha^{vib}$. See Ref.[9] for short review on the topic.

To estimate change of entropy, upon binding of WIN to the capsid, from vibrations of tertiary structures we included only the Cartesian coordinates of C_α atom of protein residues and one central carbon atom of WIN compounds in the covariance matrix \mathbf{A} . We found change in entropy upon binding of WIN, $\Delta S^{vib} = S_{win}^{vib} - S_{nowin}^{vib}$, is 75.64 cal/K/mol. Fig G1 shows contribution vibrational modes to S^{vib} as a function of frequency ν of the modes. Fig G2 shows distribution of vibrational mode frequencies calculated from covariance matrix defined from the Cartesian coordinates of C_α atoms. Most of the vibrational frequencies are less than 20 ps⁻¹ which is a lower frequency than vibrational modes estimated for secondary structures of proteins [10]. Accordingly, the modes from HRV14 are more collective and related to tertiary structures of the capsid.

Experimental results show WIN like drug stabilizes poliovirus capsid, structurally similar to rhinovirus capsid, entropically by ~ 320 cal/K/mol[11]. From fluctuations of C_α atoms we find

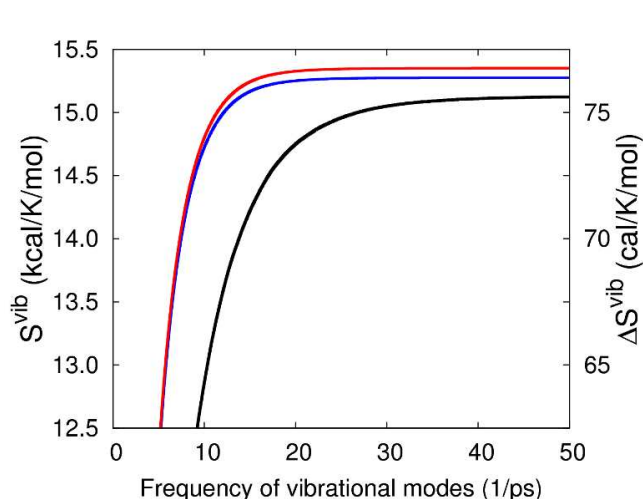


Figure G1: Vibrational entropies S_{nowin}^{vib} (blue), calculated from fluctuations of C_{α} atoms in T_{nowin} , and S_{win}^{vib} (red), calculated similarly from T_{win} , are plotted as a function frequency of fluctuations. Difference in vibrational entropy, $\Delta S^{vib} = S_{win}^{vib} - S_{nowin}^{vib}$ is plotted as a function of frequency in black. Final value of ΔS^{vib} is 75.64 cal/K/mol.

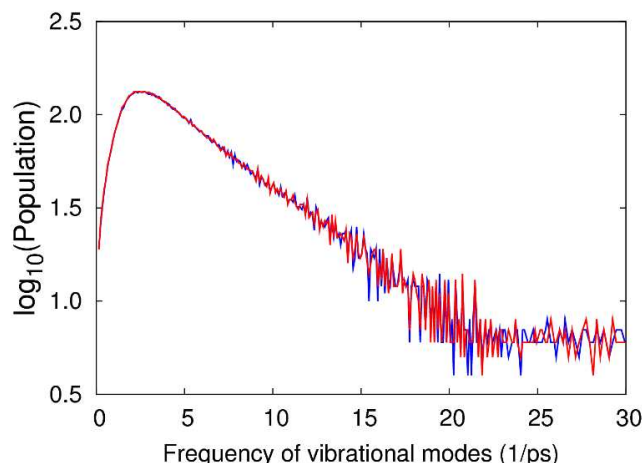


Figure G2: Number of vibrational modes as a function of frequency of the modes calculated from fluctuations of C_{α} atoms in T_{nowin} and T_{win} are plotted in blue and red curve respectively. Most of the modes have frequencies less than 20 ps^{-1} indicating that the observed difference in vibrational entropy is coming from vibrations of tertiary structures of capsid proteins.

ΔS^{vib} has a value of same order of magnitude. It leads us to speculate that vibrational modes contributing to ΔS^{vib} form part of the reaction coordinates of conformational change leading to the “breathing” motions.

The quasi-harmonic normal modes are also a useful approach to examine concerted motion, and therefore could be considered as a means to determine differences in long-distance correlated motions of HRV14 and HRV14-WIN capsids. While this information must be present in A, it exists in some combination of modes that is not readily apparent. How to extract a meaningful difference from the large set of normal modes for HRV14 and HRV14-WIN is unclear.

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