

## Newton Euler

$$\sum \vec{F} = ma_g$$
$$\sum \vec{M}_A = I\vec{\alpha}$$

$A$  is a fixed point or center of gravity

## Power Equation

$$T + U = T_o + U_o + W^{(nc)}$$
$$Power = \frac{dW^{(nc)}}{dt} = \frac{dT}{dt} + \frac{dU}{dt}$$

## Lagrange's Equations

$$\frac{d}{dt} \left( \frac{\partial T}{\partial \dot{q}_i} \right) - \frac{\partial T}{\partial q_i} + \frac{\partial U}{\partial q_i} = Q_i$$

## Linearized Lagrange's Equations

$$[M]\ddot{\vec{z}} + [C]\dot{\vec{z}} + [K]\vec{z} = \vec{0}$$

$$\vec{z}(t) = \vec{q}(t) - \vec{q}_0$$

$$M_{ik} = (m_{ik})_{\vec{q}_0} = M_{ki}$$

$$C_{ik} = \left( \frac{\partial^2 R}{\partial q_i \partial q_k} \right)_{\vec{q}_0} = C_{ki}$$

$$K_{ik} = \left( \frac{\partial^2 U}{\partial q_i \partial q_k} \right)_{\vec{q}_0} = K_{ki}$$

## Log Decrement

$$\delta = \ln \left( \frac{x_j}{x_{j+1}} \right)$$

$$\zeta = \frac{\delta/2\pi}{\sqrt{1 + (\delta/2\pi)^2}}$$

$$\zeta \ll 1 \rightarrow \zeta = \frac{\delta}{2\pi}$$