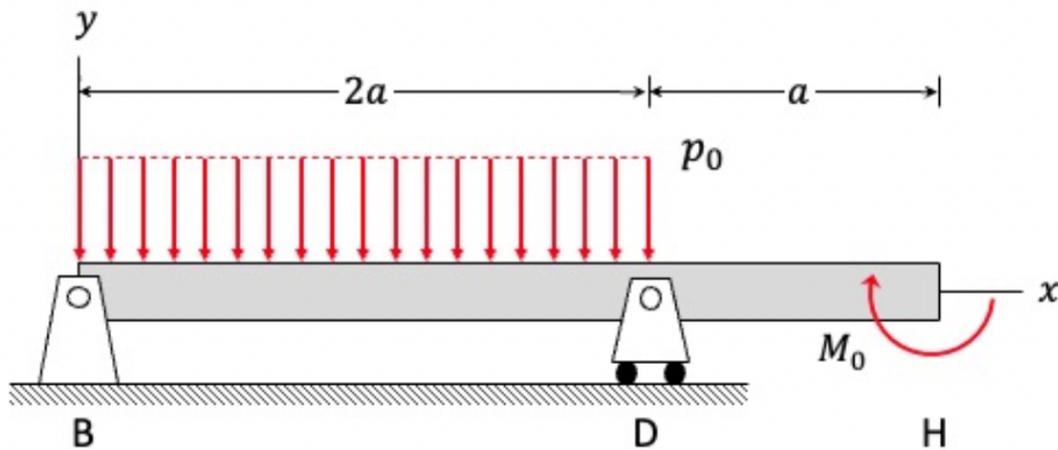


**Problem 1 (10 points):**

The simply-supported beam whose cross-section has a second area moment of  $I$  and is made up of a material with a Young's modulus of  $E$  shown below experiences a constant line load of  $p_0$  along section BD and a concentrated couple  $M_0$  at end H.

1. Draw the free body diagram (FBD) of the beam. Based on this FBD, write down the equilibrium equations for the beam.
  2. State whether the beam is determinate or indeterminate. Solve for the reactions.
  3. Using the second order integration approach, determine the deflection of the beam  $v(x)$  over the range of  $0 \leq x \leq 3a$ . Clearly identify the segments along the beam for which the different segments of the deflection curve is valid.
  4. Determine the rotation (slope) of the beam deflection curve at support D.
- Leave your answers in terms of, at most:  $E$ ,  $I$ ,  $a$ ,  $p_0$  and  $M_0$ .

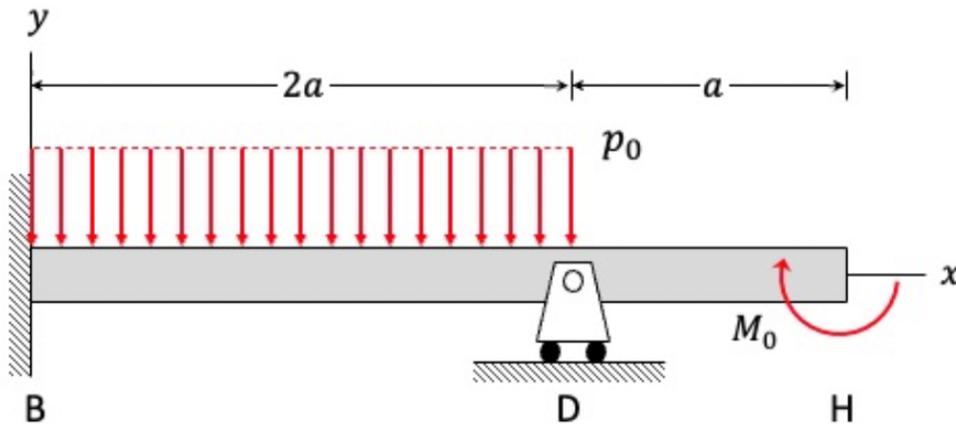


**Problem 2 (10 points):**

The propped cantilevered beam whose cross-section has a second area moment of  $I$  and is made up of a material with a Young's modulus of  $E$  shown below experiences a constant line load of  $p_0$  along section  $BD$  and a concentrated couple  $M_0$  at end  $H$ .

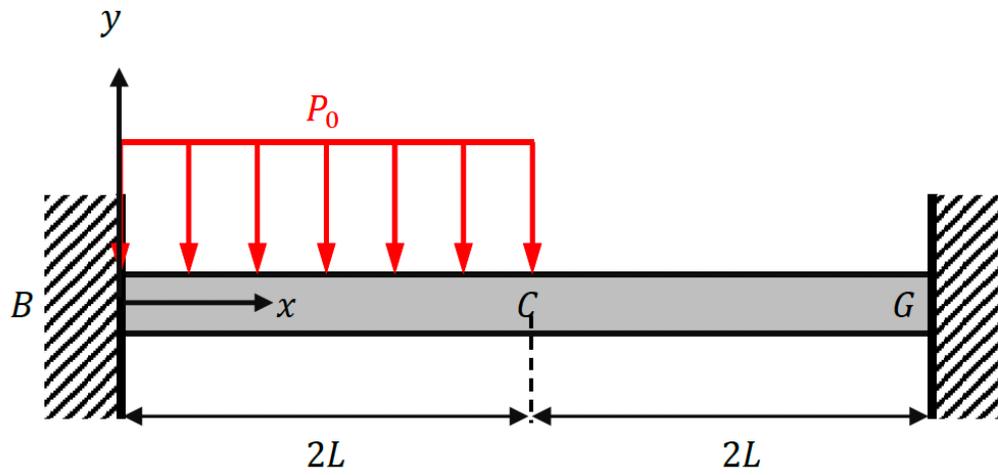
1. Draw the free body diagram (FBD) of the beam. Based on this FBD, write down the equilibrium equations for the beam.
2. State whether the beam is determinate or indeterminate.
3. Using the 2<sup>nd</sup> order integration approach, determine the reactions acting on the beam at  $B$  and  $D$ .
4. Determine the rotation (slope) of the beam deflection curve at support  $D$  and the deflection of the beam at  $H$ .

Leave your answers in terms of, at most:  $E$ ,  $I$ ,  $a$ ,  $p_0$  and  $M_0$ .



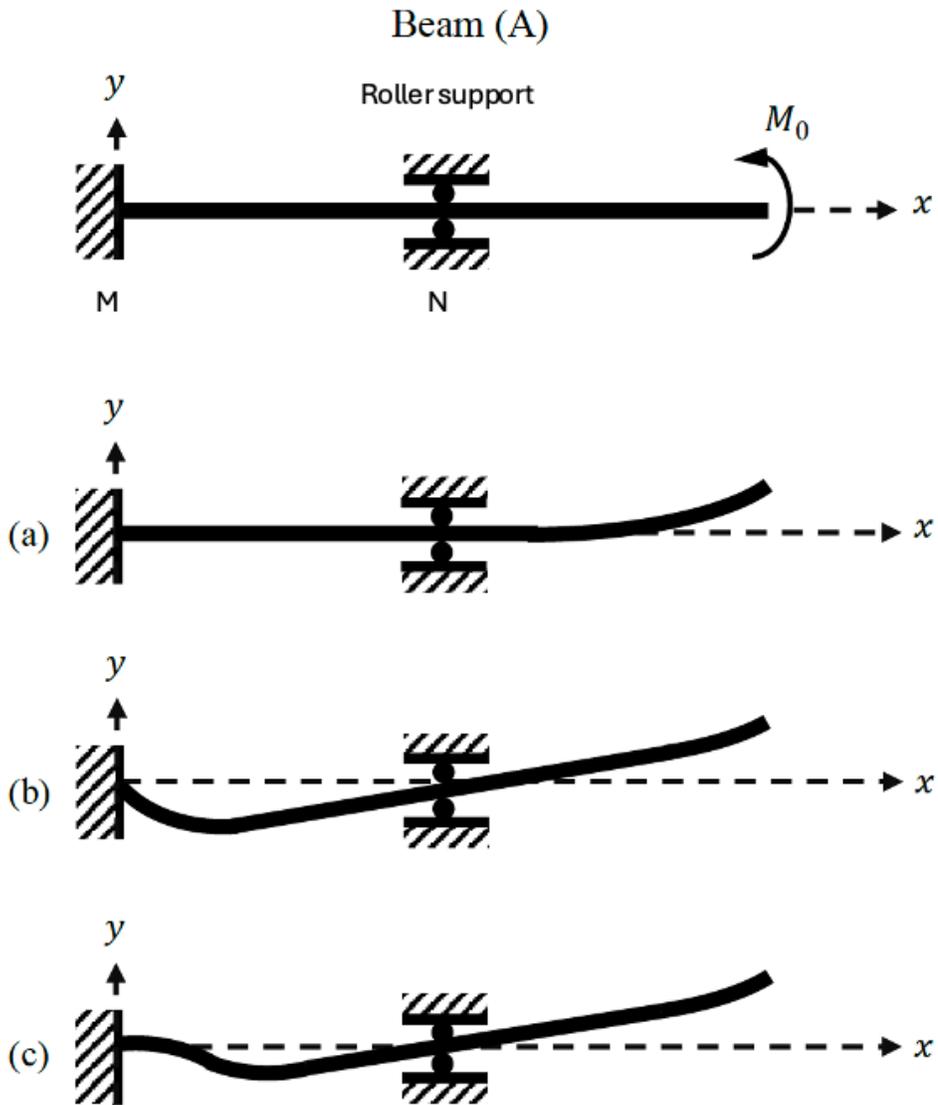
**Problem 3 (10 points):**

The beam shown below has Young's modulus  $E$  and cross-sectional second area moment  $I$ . Determine the reaction forces and moments at ends  $B$  and  $G$  using the second-order integration method.



**Problem 4 (2.5 + 2.5 points)**

Identify the schematic that represents the deflection curve of the following beams. Beam A is fixed at end M and supported by rollers at end N, whereas Beam B is supported by rollers at end M and a hinged support at end N. (each 2.5 points):



Beam (B)

