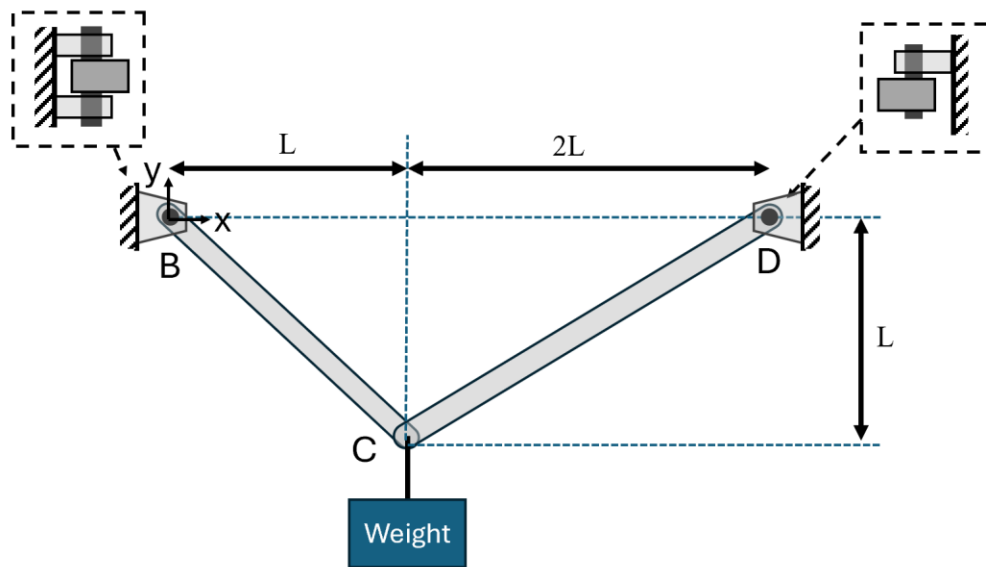


**Problem 1 (10 points):**

Structure BCD is composed of two axial members BC and CD. BC and CD both have a cross-sectional area of  $10 \text{ mm}^2$  and are made of a material with a yield stress ( $\sigma_Y$ ) of 180 MPa. The pin at B is double sided and has a diameter of 3.5 mm and a shear yield stress ( $\tau_y$ ) of 75 MPa. The pin at D is single sided and has a diameter of 5 mm and a shear yield stress ( $\tau_y$ ) of 75 MPa.

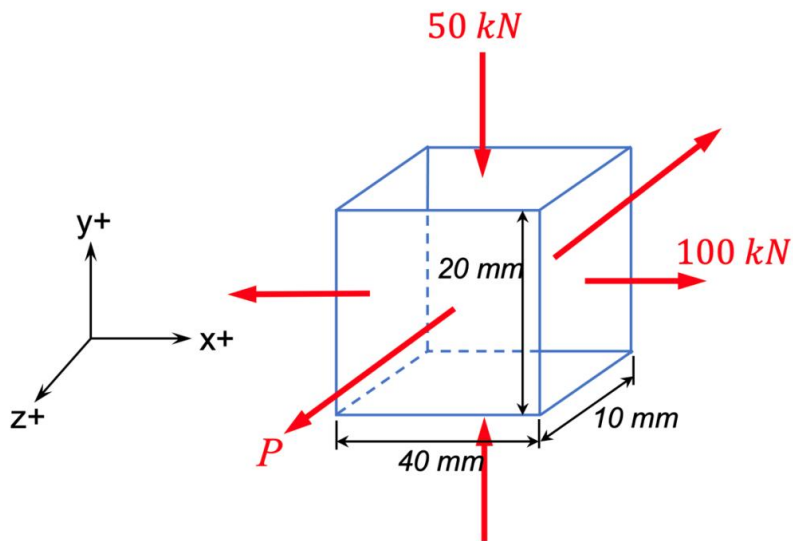


- Draw the free body diagram of the node C and write the equilibrium equations.
- Determine the normal stress in members BC and CD as a function of the weight W.
- Determine the shear stresses in the pins at B and D as a function of the weight W.
- What is the maximum value of weight (W) that can be applied to achieve an overall factor of safety of 3. What component (member BC, member CD, pin at B, or pin at D) is the limiting factor for the safety of the structure?
- What are the factors of safety for the other components at the value of W found in part (d)?

**Problem 2 (10 points):**

An elastic cuboid made of steel ( $E = 90 \text{ GPa}$ ,  $\nu = 0.15$ ), is subjected to uniformly distributed net axial forces  $100 \text{ kN}$ ,  $50 \text{ kN}$ , and an unknown force  $P \text{ (kN)}$  on the  $x$ ,  $y$ , and  $z$  faces respectively, as shown in Fig 1. The loads are applied such that uniform axial stresses are induced throughout the volume of the cuboid.

1. Calculate the unknown force  $P$  such that length of the cube along the  $x$  axis remains unchanged.
2. Calculate the corresponding deformed lengths along  $y$  and  $z$  axes due to the applied loads.

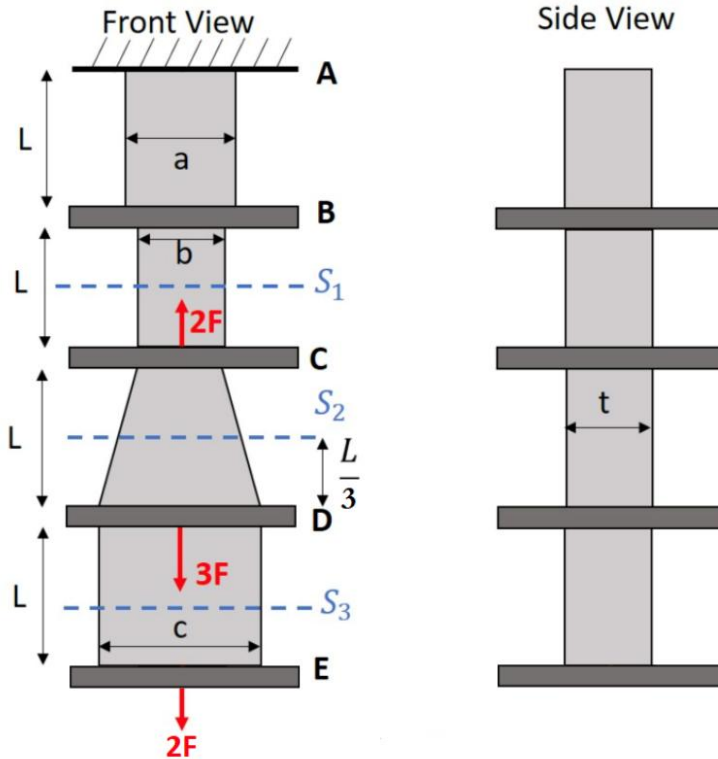


**Problem 3 (10 points):**

The axial bar shown in Figure 3 has four sections. Each section is connected to the neighbouring sections by rigid connectors (at B, C and D). The size and weight of the rigid connectors are negligible. The first section AB, second section BC and the last section DE have uniform rectangular cross sections with widths  $a$ ,  $b$  and  $c$ , respectively. The section CD has width varying linearly from  $b$  to  $c$ . The length of each section is  $L$ . All the sections have same thickness  $t$ . Three loads  $2F$ ,  $3F$  and  $2F$  are applied to the bar as shown in the figure. Assume the Young's Modulus of all the sections is  $E$ .

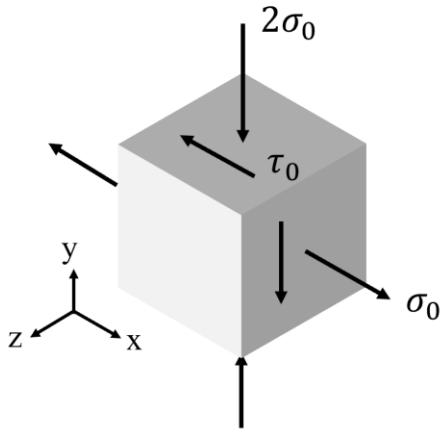
(a) Find expressions for the stresses at sections  $S_1$ ,  $S_2$  and  $S_3$ . ( $S_2$  is  $L/3$  above D as shown)

(b) Find expressions for the displacements at points B, C, and D.



#### Problem 4 (5 points)

**Conceptual:** You do not need to give an explanation for the answers. The state of stress at a given point on a structure is shown above in terms of its xyz components. The material has a Young's modulus of  $E$  and a Poisson's ratio of  $\nu$ , where  $0 < \nu < 0.5$ . State whether each of the xyz components of strain ( $\epsilon_x, \epsilon_y, \epsilon_z, \gamma_{xy}, \gamma_{xz}, \gamma_{yz}$ ) is  $<0$ ,  $=0$ , or  $>0$ .



	$<0, =0, \text{ or } >0$
$\epsilon_x$	
$\epsilon_y$	
$\epsilon_z$	
$\gamma_{xy}$	
$\gamma_{xz}$	
$\gamma_{yz}$	