

Problem 1 (10 points):

While walking through the streets of Osaka, you come across a unique design of a streetlamp (*figure 1*). In this design, a streetlamp of weight W is suspended from the post OABC. A load $4P$ is also applied at point C in the X direction.

- Calculate the reaction forces and moments developed at points O and D of the structure.
- In words, suggest how the reaction forces vary as you move along the length of the post i.e. from O to C.

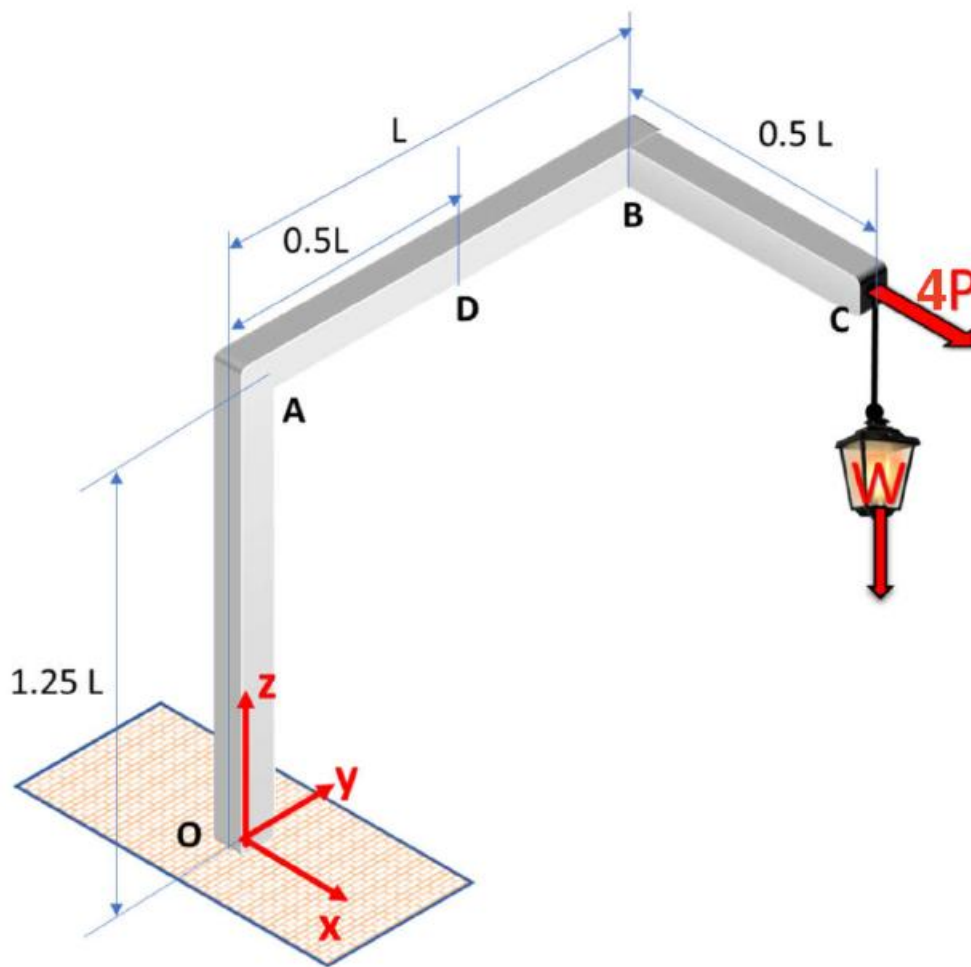


Figure 1: Streetlamp design for Problem 1

Problem 2 (10 points):

Your toddler nephew glues together two wooden blocks of identical square cross section (10 mm x 10 mm) along the plane AC as shown in *figure 2*. The dimension of the entire setup is 10 mm x 10 mm x 100 mm.

- If the glue can withstand a maximum shear stress of 10 kPa, calculate the maximum force P that can be applied at the end of the wooden blocks so that the blocks stay together (or the minimum force to take them apart).
- If the glue can withstand a maximum normal stress of 5 kPa and shear stress of 3.5 kPa. What is the maximum load that can be applied?

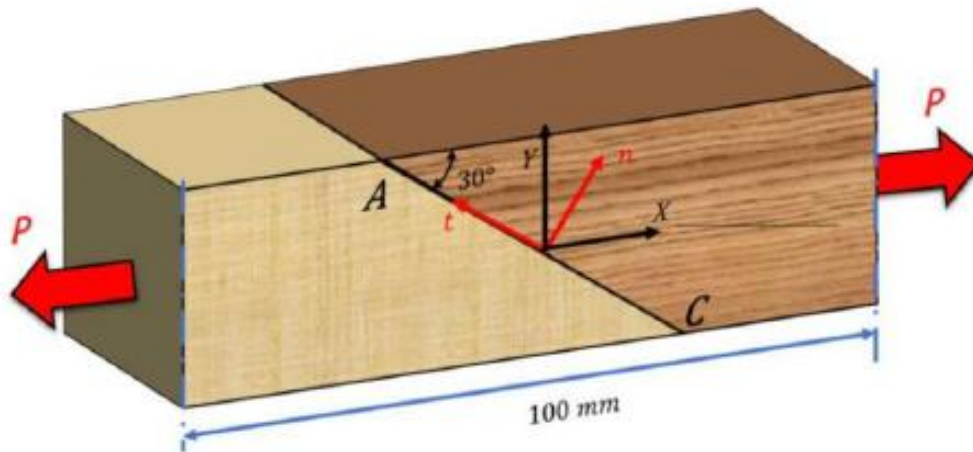


Figure 2: Structure for Problem 2

Problem 3 (10 points):

The truss shown below (*figure 3*) is supported by pin joints at B and D. Each member of the truss is made of the same material but has different cross-sectional areas: Member (1) - A, Member (2) - 2A, Member (3) - 2A, and Member (4) - A. If a force P acts downward at H,

- (a) Determine the load carried by each member of the truss.
- (b) Determine the stress developed in each member of the truss. State whether it is in tension or compression.

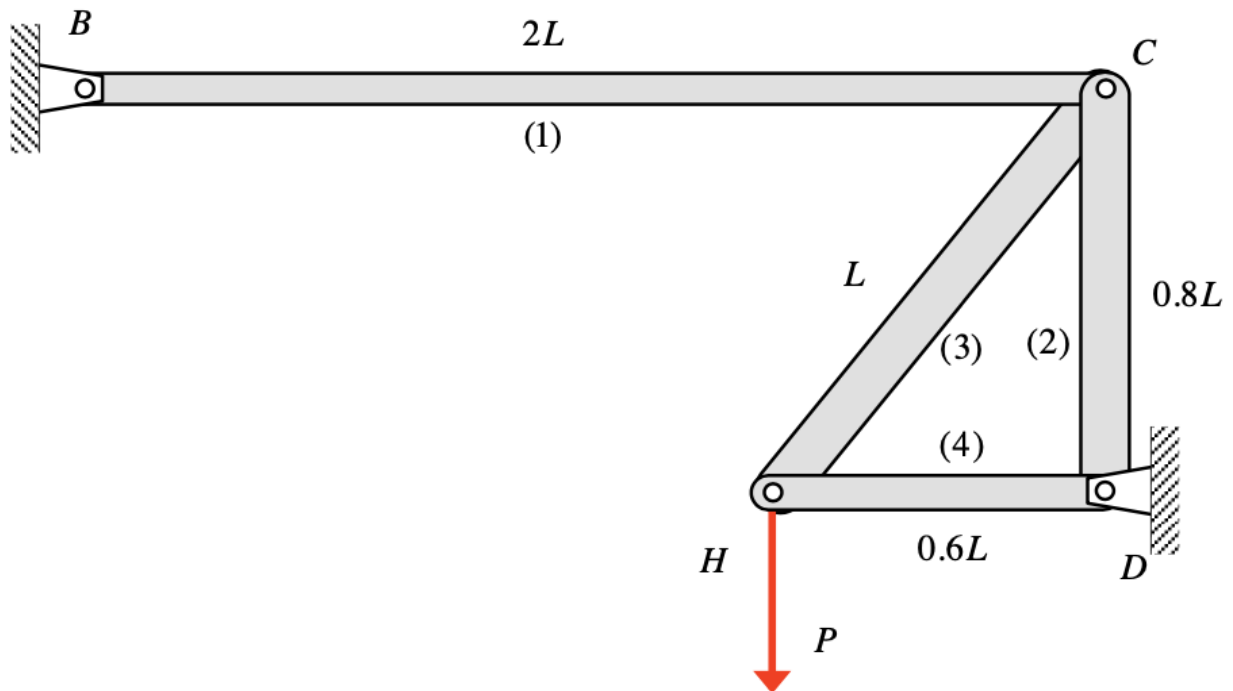


Figure 3: Truss for Problem 3

Problem 4 (2.5 points + 2.5 points):

A component is known to be in a state of plane stress ($\sigma_z = 0$). The following values are also known for stresses and strains:

$$\sigma_x = 20 \times 10^6 \text{ N/m}^2$$

$$\sigma_y = 120 \times 10^6 \text{ N/m}^2$$

$$\varepsilon_x = -1 \times 10^{-3}$$

$$\varepsilon_y = 6 \times 10^{-3}$$

4.1 The numerical value for Poisson's ratio of the material is:

(a) $\nu = -0.2956$

(b) $\nu = 0.1853$

(c) $\nu = 0.5722$

(d) $\nu = 0.3243$

4.2 The numerical value for Young's Modulus of the material is:

(a) $E = 1.89 \times 10^{10} \text{ Pa}$

(b) $E = 2.39 \times 10^{15} \text{ Pa}$

(c) $E = 5.45 \times 10^8 \text{ Pa}$

(d) $E = 6.07 \times 10^5 \text{ Pa}$