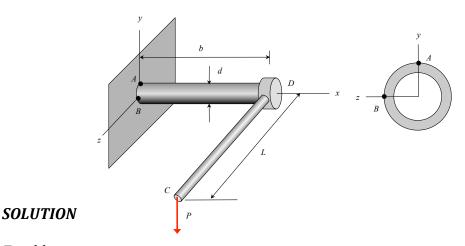
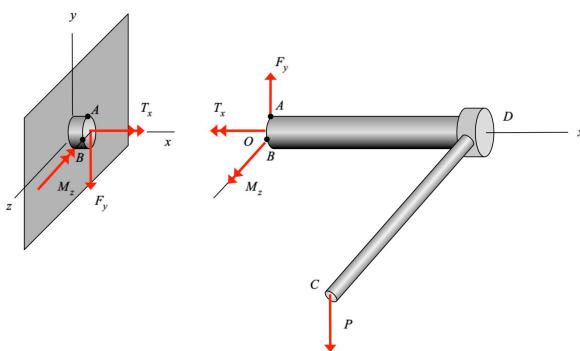
### Example 14.4 - SOLUTION

A vertical force of P is applied to the end of a pipe wrench CD, whose handle is parallel to the z-axis. The pipe has an outer diameter of d and wall thickness of t. Determine the principal stresses at points A and B on the cross section of the pipe.



# **Equilibrium**

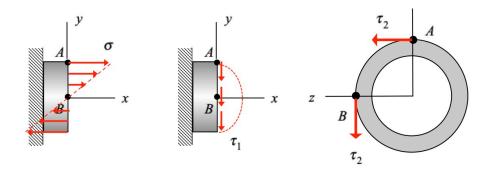


$$\begin{split} \sum F_y &= -P + F_y = 0 \quad \Rightarrow \quad F_y = P \\ \sum M_O &= -T_x \hat{i} + M_z \hat{k} + \vec{r}_{C/O} \times \vec{P} = \vec{0} \\ &= -T_x \hat{i} + M_z \hat{k} + \left(b\hat{i} + L\hat{k}\right) \times \left(-P\hat{j}\right) \\ &= \left(-T_x + PL\right) \hat{i} + \left(M_z - Pb\right) \hat{k} \quad \Rightarrow \end{split}$$

$$\hat{i}: T_{_X} = PL$$

$$\hat{k}: M_z = Pb$$

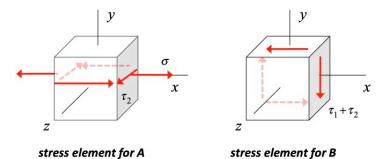
#### Stress distributions



#### Stresses at A and B

internal resultant	stress @ A	stress @ B
$F_y$	0	$\tau_1 = \frac{F_y Q}{It} = \frac{PQ}{It}$
$T_x$	$\tau_2 = \frac{T_x \left( d/2 \right)}{2I_P} = \frac{PLd}{2I_P}$	$\tau_2 = \frac{T_x \left( d / 2 \right)}{2I_P} = \frac{PLd}{2I_P}$
$M_z$	$\sigma = \frac{M_z (d/2)}{I} = \frac{Pbd}{2I}$	0

## Stress elements for A and B



**Principal stresses**