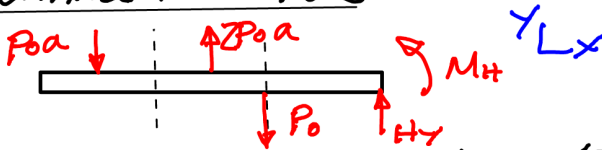


Determine the shear force and bending moment diagrams in the plot axes below for the loaded beam shown. Clearly indicate the values of V and M at the labeled points as well as any maximum/minimum values. Please provide details on your work. Use

$$p_0 = 20 \text{ lb/in}, a = 2 \text{ in} \text{ and } P_0 = 40 \text{ lb}.$$

Determine reactions



$$\sum M_H = M_H + P_0 a - (2P_0 a) \left(\frac{3a}{2}\right) + P_0 a \left(\frac{5a}{2}\right) = 0$$

$$\hookrightarrow M_H = -P_0 a + \frac{1}{2} P_0 a^2 = -40 \text{ lb}\cdot\text{in}$$

$$\sum F_x = -p_0 a + 2p_0 a - P_0 + H_y = 0$$

$$\hookrightarrow H_y = P_0 - p_0 a = 0$$

Shear force

- $V(0) = 0$
- $V(2) = V(0) + (-p_0)(2) = -40 \text{ lb}$
- $V(4^-) = V(2) + (2p_0)(2) = 40 \text{ lb}$
- $V(4^+) = V(4^-) - P_0 = 0$
- $V(6) = V(4^+) + 0 = 0 \checkmark$

Bending moment

- $M(0) = 0$
- $M(2) = M(0) + \frac{1}{2} (-40)(2) = -40$
- Since $V(3) = 0 \Rightarrow \frac{dM}{dx}(3) = 0 \hat{=} M(3) = M(2) + \frac{1}{2} (-40)(1) = -60$
- $M(4) = M(3) + \frac{1}{2} (40)(1) = -40$
- $M(6) = M(4) + 0 = -40 \checkmark$

