

1. xyz . Attached to shaft \vec{OA}



Find $\vec{\omega}$, $\vec{\alpha}$ of xyz

$$\vec{\omega} = -\omega_1 \hat{i} = -\omega_1 \hat{i} \quad \text{at this inst.}$$

$$\vec{\alpha} = 0$$

Write \vec{a}_p expression. *eg*

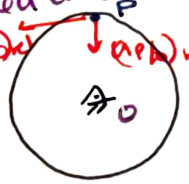
$$\vec{a}_p = \vec{a}_0 + \vec{\alpha} \times \vec{r}_{p/o} + \vec{\omega} \times \vec{\omega} \times \vec{r}_{p/o} + (\vec{a}_p/o)_{rel} + 2\vec{\omega} \times (\vec{v}_{p/o})_{rel}$$

Write \vec{a}_0 expression.

$$\vec{a}_0 = \vec{a}_A + \vec{\alpha}_{OA} \times \vec{r}_0/A + \vec{\omega}_{OA} \times \vec{\omega}_{OA} \times \vec{r}_0/A - \omega_1 \hat{i} \times (-\omega_1 \hat{i} \times d \hat{k}) = -\omega_1^2 d \hat{k} = -\omega_1^2 d \hat{k} \quad \text{at this instant}$$

Find $(\vec{v}_{p/o})_{rel}$ and $(\vec{a}_{p/o})_{rel}$

Like a pinned disc $(\vec{v}_{p/o})_{rel}$



$$(\vec{v}_{p/o})_{rel} = \vec{v}_0 + \vec{\omega}_{disk} \times \vec{r}_{p/o} = \omega_2 \hat{k} \times R \hat{j} = -\omega_2 R \hat{i}$$

$$(\vec{a}_{p/o})_{rel} = \vec{a}_0 + \vec{\alpha}_{disk} \times \vec{r}_{p/o} + \vec{\omega}_{disk} \times \vec{\omega}_{disk} \times \vec{r}_{p/o} = -\omega_2^2 R \hat{j}$$

Solve for \vec{a}_p .

$$\vec{a}_p = -\omega_1^2 d \hat{k} + (-\omega_1 \hat{i}) \times [(-\omega_1 \hat{i}) \times R \hat{j}] - \omega_2^2 R \hat{j} + 2(-\omega_1 \hat{i}) \times (-\omega_2 R \hat{i})$$

$$\vec{a}_p = -(\omega_1^2 R + \omega_2^2 R) \hat{j} - \omega_1^2 d \hat{k}$$

2. xyz Attached to disk

Find $\vec{\omega}$, $\vec{\alpha}$ of xyz

$$\vec{\omega} = -\omega_1 \hat{i} + \omega_2 \hat{k} = -\omega_1 \hat{i} + \omega_2 \hat{k} \quad \text{at this inst.}$$

$$\vec{\alpha} = \frac{d}{dt}(\vec{\omega}) = -\dot{\omega}_1 \hat{i} - \dot{\omega}_2 \hat{k} = \omega_1 \hat{i} + \omega_2 \hat{k} \quad \text{at the inst.}$$

$$= \omega_2 (\vec{\omega} \times \hat{k}) = \omega_2 [(-\omega_1 \hat{i} + \omega_2 \hat{k}) \times \hat{k}] = \omega_2 \omega_1 \hat{j}$$

Write \vec{a}_p expression.

$$\vec{a}_p = \text{same}$$

Write \vec{a}_0 expression.

$$\vec{a}_0 = \text{same}$$

Find $(\vec{v}_{p/o})_{rel}$ and $(\vec{a}_{p/o})_{rel}$

$$(\vec{v}_{p/o})_{rel} = 0$$

$$(\vec{a}_{p/o})_{rel} = 0$$

Solve for \vec{a}_p .

$$\vec{a}_p = -\omega_1^2 d \hat{k} + (\omega_2 \omega_1 \hat{j} \times R \hat{j}) + (-\omega_1 \hat{i} + \omega_2 \hat{k}) \times [(-\omega_1 \hat{i} + \omega_2 \hat{k}) \times R \hat{j}]$$

$$= -\omega_1^2 d \hat{k} - \omega_1^2 R \hat{j} - \omega_2^2 R \hat{j} = -(\omega_1^2 R + \omega_2^2 R) \hat{j} - \omega_1^2 d \hat{k}$$