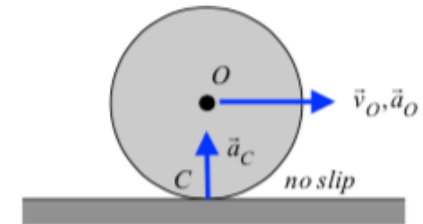


## Summary: Newton/Euler Equations 2

FUNDAMENTAL equations:

- (1)  $\sum \vec{F} = m\vec{a}_G$   
 (2)  $\sum \vec{M}_A = I_A \vec{\alpha}$  ; A = c.m. OR fixed point OR  $\vec{r}_{G/A} \parallel \vec{a}_A$



MASS MOMENT OF INERTIA:  $I_A = \int r^2 dm$ , with  $r$  measured from point A

- circular disk of radius  $R$ , mass  $m$  and c.m. at  $G$ :  $I_G = mR^2 / 2$
- thin bar of length  $L$ , mass  $m$  and c.m. at  $G$ :  $I_G = mL^2 / 12$

PARALLEL AXES THEOREM:  $I_A = I_G + md^2$

- You MUST have  $I_G$  on the right-hand side of the P.A.T. equation.
- The mass moment of inertia about the c.m. is the smallest for all points on the body.
- When do you need to use this? *Useful when a non-centroidal point is used in Euler's equation.*

RADIUS OF GYRATION:  $k_A \triangleq \sqrt{I_A / m}$ . *Dependent only on the "shape", NOT on the mass.*