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Development of a Mobile Probe-Based Traffic Data Fusion and Flow Management Platform for Innovative Public-Private Information-Based Partnerships

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Title
Development of a Mobile Probe-Based Traffic Data Fusion and Flow Management Platform for Innovative Public-Private Information-Based Partnerships

Introduction
Under the aegis of Intelligent Transportation Systems (ITS), real-time traffic information provision strategies are being proposed to manage traffic congestion, alleviate the effects of incidents, enhance response efficiency after disasters, and improve the multimodal/intermodal travel experience of travelers. Currently, most of the real-time traffic information provision and control systems infrastructure is deployed and maintained by public agencies. Given the projected growth and profitability due to the evolution of the information services market in the near future, the potential for new innovations and significant investments from the private sector in emerging technologies and applications related to real-time traffic information can foster new businesses. This study aims to exploit the synergy due to innovative data collection, traffic management, and road pricing/credit mechanisms that can encourage mutually beneficial information-sharing under innovative partnerships (public-private sector, private-private sector, public–public sector partnerships).

There were three major objectives identified to be accomplished by this study: i) development of a unified data mining system that can synthesize different data sources to estimate traffic network states; ii) identification of existing deficiencies in data quality, coverage and reliability in an existing DOT traffic sensor network and development of an information gain theoretic model for optimal sensor location that can take into account uncertainty; iii) measuring and understanding the benefits of real-time traffic information to the commuter by investigating the physical and psychological benefits of real-time traffic information systems.
and development of reliable traveler behavior models that can be used to predict costs and benefits for deployment of such systems to stakeholders.

Findings

To provide effective congestion mitigation strategies, transportation engineers and planners need to systematically measure and identify both recurring and non-recurring traffic patterns through a network of sensors. The collected data is further processed and disseminated for travelers to make smart route and departure decisions. This study proposes a theoretical framework for the heterogeneous sensor network design problem based on successive private-public sector partnerships. In particular, we focus on how to better construct network-wide historical travel time databases, which need to characterize both mean and estimation uncertainty of end-to-end path travel time in a regional network.

A unified travel time estimation and prediction model is first proposed in this research to integrate heterogeneous data sources through different measurement mapping matrices. Specifically, the travel time estimation model starts with the historical travel time database as prior estimates. Point-to-point sensor data and GPS probe data are mapped to a sequence of link travel times along the most likely travelled path. The proposed information quantification model can assist decision-makers to select and integrate different types of sensors, as well as to determine how, when, and where to integrate them in an existing traffic sensor infrastructure.

This study also provides methods for incorporating emerging Automatic Vehicle Identification (AVI) and Global Positioning System (GPS) data to estimate the microscopic states of traffic segments, for the purposes of traffic monitoring and management. Both AVI and GPS samples can be viewed as data “bridges.” In our proposed model, a series of linear measurement equations are developed to dramatically simplify the process of estimating the likelihood of free-flow vs. congested traffic conditions. The value of information (VOI) for the highway traffic state estimation problem systematically investigated for various types of data sources. We then use an information-theoretic approach to quantify the uncertainty of
microscopic traffic state estimation results and further evaluate the effectiveness of various important sensor design scenarios, such as point detector sampling rates, AVI market penetration rates, and GPS market penetration rates.

Finally, we also recognize that various technical and computational barriers still exist for real-time deployment of public-private sector partnerships for traffic information provision. The barriers are mainly present at various stages of the complex data collection and information dissemination process, which include collecting traffic data characterizing the system, transferring the data to various input formats, rapidly predicting traffic under various control strategies, and finally effectively communicating forecasts to travelers without creating driving distractions. All of the above tasks have to occur in a reasonable time frame.

**Recommendations**

This research proposed unified travel time estimation and prediction models to integrate heterogeneous data sources through different measurement mapping matrices. Point-to-point sensor data and GPS probe data are mapped to a sequence of link travel times along the most likely travelled path. The proposed information quantification model can assist traffic agencies (state DOTs and MPOs) to select and integrate different types of sensors, as well as to determine how, when, and where to integrate them in an existing traffic sensor infrastructure. The study also provides methods for incorporating emerging technologies to estimate the microscopic states of traffic segments, for the purposes of traffic monitoring and management.

Further, in order to assess the potential benefits of an advanced traveler information system, there is a need to determine meaningful performance measures beyond just the putative travel time savings. For example, psychological benefits derived from driving experience due to the access to real-time traffic information. The ability to explicitly quantify the human behavior dimension as studied in this research provides a broader set of parameters to public and private sector entities relative to the evolution of the travel information market.
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CHAPTER 1. INTRODUCTION

1.1 Background and motivation

Under the aegis of Intelligent Transportation Systems (ITS), real-time traffic information provision strategies are being proposed to manage traffic congestion, alleviate the effects of incidents, enhance response efficiency after disasters, and improve the multimodal/intermodal travel experience of travelers. Further, through innovations enabled by leveraging technological advances in information and communications technologies, such information provides travelers navigational capabilities and access to location-based services. It enables travelers to enhance the quality and safety of their travel experience through informed decision-making.

Most existing traffic information provision and control systems are deployed and maintained by public agencies, and are built on centralized management architectures. The current technological advances and increased demand for real-time travel information also provides the private sector an emerging domain of opportunities to gainfully participate and shape the evolution of the nascent travel information market. This market is expected to grow from 57 million real-time information users in 2010 to more than 370 million globally by 2015 (Source: ABI Research). Further, the global revenue from real-time traffic information services is projected to increase from $500 million in 2008 to $4.5 billion in 2014 (Source: Cellular News).

The evolution of the travel information market in the United States is occurring at a time when limited revenue streams for federal funding of the transportation sector due to a
sluggish economy are being further exacerbated by the imperatives arising from the need for energy security and to mitigate the negative effects of climate change.

When viewed in conjunction with the need to renew the deteriorating current transportation infrastructure, and the consequences thereof for the economic competitiveness of the U.S. in a global economy, there is an on-going fundamental re-think among policy-makers that suggests the need for a holistic approach to supplement the limited existing funding resources with novel and innovative mechanisms that generate new revenue streams to address the nation’s transportation needs.

In this context, the evolving travel information market represents a key win-win opportunity to generate revenues and resources through innovative partnerships (public-private, private-private, and public-public) to address multiple synergistic goals. First, it enables the limited public sector resources to be supplemented by private sector funding to reduce congestion delays and improve safety. Second, it assures the future economic competitiveness of the U.S. by renewing existing infrastructure using technologies that can significantly increase the efficiency of the utilization of the existing transportation facilities while explicitly enhancing travel safety and enabling the deployment of a new generation of integrated traffic management strategies. Third, it is a holistic approach as it can address multiple national objectives, including safety, mobility, livability, energy security, economic competitiveness, and eco-sensitivity, while reinforcing ongoing national programs such as IntelliDrive. However, for the fruition of the travel information market, there is the need for leadership from both the public and private sectors, through

Figure 1.1 : Global Real-Time Traffic Service Revenue and Subscriber Forecast (Source Cellular News)
integrated policy decisions, development of standards, and the alignment of institutional processes.

1.2 Chapter objectives

Currently, most of the real-time traffic information provision and control systems infrastructure is deployed and maintained by public agencies. Given the projected growth and profitability due to the evolution of the information services market in the near future, the potential for new innovations and significant investments from the private sector in emerging technologies and applications related to real-time traffic information can foster new businesses. For this to happen at a widespread scale, there is need for policy and regulatory decisions at the federal level. This study aims to exploit the synergy due to innovative data collection, traffic management, and road pricing/credit mechanisms that can encourage mutually beneficial information-sharing under innovative partnerships (public-private sector, private-private sector, public–public sector partnerships).

Two major issues will be investigated under different levels of public-private data sharing plan and probe data availability: (1) how to use spatially distributed mobile probe data to identify information gap and deficiency in terms of data quality, coverage and reliability for an existing DOT traffic sensor network; (2) develop information-theoretical sensor network design and management algorithms to determine where and which type of DOT sensor investments should be made. The goal of sensor location optimization is to maximize the expected information gain for the traffic state estimation and problem applications; the sensor design model in this research will explicitly take into account the uncertainty.

Further, the final goal of the proposed research work is to measure and understand the benefits of real-time traffic information to the commuter by investigating the physical and psychological benefits of real-time information by developing reliable traveler behavior models that can be used to predict costs and benefits for real-world deployment.
1.3 *Organization of the research*

The remainder of the research is organized as follows. Chapter 2 is on multi-source traffic state estimation framework and fusion of data from multiple data sources. Chapter 3 investigates sensor location optimization is to maximize the expected information gain for the traffic state estimation. In Chapter 4, we seek to understand the potential benefits of real-time information to travelers beyond mere physical benefits. This chapter is about work-in-progress as this is the first year report of multiple year effort and Chapter 5 draws conclusions from the study as well as discusses future work.
CHAPTER 2. MULTI-SOURCE TRAFFIC STATE ESTIMATION FRAMEWORK

Existing in-pavement and road-side traffic sensors are typically located on a small subset of freeway links and experience perceivable failure rates in the context of traffic management/operations. Hence, while accurate travel time and traffic flow information on ramps and arterial corridors are critically needed, they are expensive to collect on a network-wide basis in addition to the reliability issues. The new generation of GPS-enabled mobile devices presents a data-rich environment for regional traveler information systems to accurately measure route-based travel times and network-wide traffic flow dynamics and evolution. This research focuses on how to use multiple data sources, including loop detector counts, AVI Bluetooth travel time readings and GPS location samples, to estimate microscopic traffic states on a homogeneous freeway segment. A multinomial probit model and an innovative use of Clark’s approximation method were introduced to extend Newell’s method to solve a stochastic three-detector problem. The mean and variance-covariance estimates of cumulative vehicle counts on both ends of a traffic segment were used as probabilistic inputs for the estimation of cell-based flow and density inside the space-time boundary and the construction of a series of linear measurement equations within a Kalman filtering estimation framework. We present an information-theoretic approach to quantify the value of heterogeneous traffic measurements for specific fixed sensor location plans and market penetration rates of Bluetooth or GPS flow car data.

This chapter is organized as follows. After reviewing the highway traffic state estimation problem in Section 2.1, Section 2.2 briefly reviews the deterministic three-detector model, which is based on the triangular relationship and Newell’s method. In Sections 2.3, 2.4 and 2.5, we sequentially discuss stochastic boundary conditions and
propose a generalized least squares estimation framework to solve the stochastic three-detector problem using heterogeneous data sources. In Section 2.6, numerical experiments are used to demonstrate the proposed methodology and illustrate observability improvements under different sensing plans and market penetration rates.

2.1 Literature Review

By reducing traffic system instability and volatility, the transportation system will operate more efficiently, with better end-to-end trip travel time reliability and reduced total emissions. By closely monitoring and reliably estimating the state of the system using heterogeneous data sources, it is possible to apply information provision and control actions in real time to best utilize the available highway capacity. These two realizations have motivated the two main directions of this research: estimating freeway traffic states from heterogeneous measurements and quantifying the uncertainty of traffic state estimations under different sensor network deployment plans.

A majority of modeling methods focus on macroscopic point bottleneck detection and link-level travel time estimation problems (e.g., Ashok and Ben-Akiva, 2000; Zhou and List, 2010; Coifman, 2002). Recently, a number of data-mining methods have been proposed for the purpose of obtaining microscopic traffic states on freeway segments using different sources of data.

A generic microscopic traffic state estimation method consists of a number of key components: an underlying traffic flow model, a state variable representation, and a system process and a measurement equation. Different traffic flow models could lead to various system state representation and process equations. For example, the Cell Transmission Model (CTM), proposed by Daganzo (1994), captures the transfer flow volume between cells as a minimum of sending and receiving flows, while Newell’s simplified kinematic wave model (Newell, 1993), or three-detector method, which has been systematically described by Daganzo (1997), considers cumulative vehicle counts at an intermediate location of a homogeneous freeway segment as a minimization function of the upstream and downstream cumulative arrival and departure counts.
To apply computationally efficient filters (e.g., a Kalman filter or particle filter) to handle large-volume streaming sensor data, one of the major modeling challenges for traffic state estimation is how to extract or construct linear system processes and measurement equations. The widely used Eulerian sensing framework (e.g., Muñoz et al., 2003; Sun et al., 2003; Sumalee et al., 2011) uses linear measurement equations to incorporate flow and speed data from point detectors, while the emerging Lagrangian sensing framework (e.g., Nanthawichit et al., 2003; Work et al., 2010; Herrera and Bayen, 2010) aims to establish linear measurement equations to utilize semi-continuous samples from moving observers or probes.

Muñoz et al. (2003) proposed a novel switching-mode model (SMM), which adapts a Modified Cell Transmission Model (MCTM) to describe traffic dynamics and transforms its nonlinear (minimization) state equations into a set of piecewise linear equations. In particular, each set of linear equations is referred to as a mode, and the SMM switches between different modes according to the detailed congestion status of the cells in a section and the values of the mainline boundary inputs. Along this line, Sun et al. (2003) employed a mixture Kalman filter to approximate the probabilistic state space through a finite number of mode sample sequences, where the weight of each sample is dynamically adjusted to reflect the posterior probability of all state vectors. Sumalee et al. (2011) further introduced stochastic elements to the MCTM framework by Muñoz et al. (2003) and proposed a stochastic cell transmission model.

Based on a second-order traffic flow model, Wang and Papageorgiou (2005) and Wang et al. (2007) presented a comprehensive extended Kalman filter framework for the estimation and prediction of highway traffic states. To construct linear process equations, linearization around the current state (typically segment density) is required to determine the outgoing flows between segments. Mihaylova et al. (2007) developed a CTM-based second-order macroscopic model and adopted an alternative particle-filtering framework to avoid computational intensive linearization operations.

Nanthawichit et al. (2003) conducted an early chapter that used Payne’s traffic flow model and Kalman filtering within a Lagrangian sensing framework. Work et al. (2010) derived a velocity-based partial differential equation (PDE) to construct linear
measurement equations for utilizing Lagrangian data, while an Ensemble Kalman filter was embedded to propagate non-linear state equations through a Monte Carlo simulation approach. Herrera and Bayen (2010) incorporated a correction term to the Lighthill-Whitham-Richards partial differential equation (Lighthill and Whitham, 1955; Richards, 1956) to reduce the discrepancy between the Lagrangian measurements and the estimated states. Treiber and Helbing (2002) proposed an efficient interpolation method by first employing a “kernel function” to build the state equation for forward and backward waves, and then integrating these two equations into a linear state equation through a speed measurement-based weighting scheme. Based on the cumulative flow count and simplified kinematic wave model (Newell, 2003), Coifman (2002) developed methods to reconstruct vehicle trajectories from the measured local speed measures or a partial set of vehicle probe trajectories. While Mehran et al. (2011) further investigated the sensitivity impact of input data uncertainty, their solution framework has not directly taken into account the measurement errors of different data sources.

While significant progress has been made in formulating system process and measurement equations for the freeway traffic state estimation problem, this chapter aims to address several challenging theoretical and practical issues.

First, we propose a stochastic version of Newell’s three-detector model to utilize multiple data sources to estimate microscopic traffic states for a homogeneous freeway segment. This method provides a new alternative to the existing CTM-based traffic state estimation approach and the interpolation method of Treiber and Helbing (2002). In particular, the traffic state of any intermediate point on a freeway segment can be estimated directly from the boundary conditions through a minimization operation. To handle the upstream and downstream cumulative flow counts as two random variables, we introduce a multinomial probit model and Clark’s approximation (from the field of discrete choice modeling) to approximate the minimization of two random variables as a third random variable with quantifiable mean and variance. By doing so, we could link the accuracy of traffic state estimation for each cell directly with the variability of the boundary conditions.
Second, this chapter aims to incorporate emerging Automatic Vehicle Identification (AVI) and Global Positioning System (GPS) data to estimate the inside microscopic states of a traffic segment. There are a number of surveillance techniques available for the purposes of traffic monitoring and management. Each technique has the ability to collect and process specific types of real-time traffic data. AVI data, which are obtainable from mobile phone Bluetooth samples, represent an emerging data source, but they have been mainly used in link-based travel time estimation applications (e.g., Wasson et al., 2008, Haghani et al., 2010) or origin-destination demand estimation (e.g., Zhou and Mahmassani, 2006) rather than in the estimation of within-link traffic states, such as cell-based density. The existing Lagrangian sensing framework (Nanthawichit et al., 2003; Work et al., 2010; Herrera and Bayen, 2010) can map location-based speed samples to a moving observer-oriented PDE system, but it has difficulties in incorporating end-to-end time-dependent travel time records from AVI readers across a series of cells.

It is practically important but theoretically challenging to utilize AVI data. In our proposed approach, both AVI and GPS samples can be viewed as “bridges” between the upstream and downstream boundaries in terms of cumulative flow counts. Specifically, we develop a series of linear measurement equations within the proposed stochastic three-detector approach that can dramatically simplify the process of estimating the likelihood of free-flow vs. congested traffic conditions for any location inside a traffic segment. Third, the value of information (VOI) for the highway traffic state estimation problem systematically investigated for various types of data sources. We use an information-theoretic approach to quantify the uncertainty of microscopic traffic state estimation results and further evaluate the effectiveness of various important sensor design scenarios, such as point detector sampling rates, AVI market penetration rates, and GPS market penetration rates.

Table 2.1 summarizes the data measurement types and comparative advantages of estimating traffic states at different resolutions. Each of these data sources has strengths and weaknesses, and an effective traffic state monitoring system must be able to fuse multiple data streams to symmetrically capture traffic system instability and volatility.
Moreover, as more sensing technologies become available, the monitoring system must be able to seamlessly incorporate them into a computationally efficient and theoretically rigorous analysis framework.

Table 2.1: The comparative advantages of surveillance techniques

<table>
<thead>
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<th>Measurement Type</th>
<th>Data Quality</th>
<th>Costs and Concerns</th>
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<td>Point Detectors</td>
<td>Vehicle counts and point speed</td>
<td>High accuracy and relatively low reliability</td>
<td>High maintenance cost</td>
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<tr>
<td>Automatic Vehicle Identification</td>
<td>Point to point flow information for tagged vehicles such as travel time and volume</td>
<td>Accuracy depends on market penetration level of tagged vehicles</td>
<td>Relatively high installation costs for automated vehicle ID reader</td>
</tr>
<tr>
<td>Mobile GPS location sensors</td>
<td>Semi-continuous path trajectory for individual equipped vehicles</td>
<td>Accuracy depends on market penetration level of probe vehicles</td>
<td>Public privacy concerns</td>
</tr>
<tr>
<td>Trajectory data from video image processing</td>
<td>Continuous path trajectory for vehicles on different lanes</td>
<td>Accuracy depends on machine vision algorithms</td>
<td>Relatively high installation cost for overhead video camera and communication wires</td>
</tr>
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</table>

2.2 Problem statement and conceptual framework

2.2.1 Parameters of traffic flow model

\(FF\)
\(TT=\) Time for traversing a certain distance by a forward wave with speed.
\(BW\)
\(TT=\) Time for traversing a certain distance by a backward wave with speed.

2.2.2 Subscripts and parameters of space-time representation

\(i\)
\(=\) Unit space increment, i.e., length of one section.
\(i\)
\(=\) Space index of sections.
\(i\)
\(=\) Space position of section, i.e.,.
\(i\)
\(=\) Location of upstream boundary.
\(i\)
\(=\) Location of downstream boundary.
= Distance from a point x to the downstream boundary.
= Unit time increment, i.e., length of one simulation clock time.
= Point sensor sampling time interval, i.e., 1 s, 30 s, 5 min.
= Time index of simulation.
= Time index of sampling point.
= Time, starting from zero.
= Measurement deviation of AVI (e.g., Bluetooth) travel time readers.
= GPS sampling time interval for a semi-continuous vehicle trajectory.

2.2.3 Boundary measurements and variables

, = Measured vehicle counts between time and at location and , respectively.
, = True vehicle counts between time and at location and , respectively.
, ) = Measurement error of vehicle counts and , assumed to be normally distributed.
, = Measured cumulative vehicle counts at location and location , respectively, at timestamp.
, = True cumulative vehicle counts at location and , respectively, at timestamp.
, = Error term of and , to be derived as normally distributed random variables.

2.2.4 Estimation variables

= Cumulative vehicle counts at any intermediate position x at time t.
, = Estimated mean and variance value of cumulative vehicle counts.
= Flow at position x at time t, to be derived from.
, = Estimated mean and variance value of flow.
= Density at position x at time t, to be derived from.
, = Estimated mean and variance value of density.

2.2.5 Variables used in probit model and Clark’s approximation

, = Disutility of the first and the second component of a minimization equation with two random variables.
, = Systematic disutility of disutility and .
, = Noise of disutility and .
= Variance of the difference between systematic disutility and .
= A combined variable, derived from using to divide the difference between systematic disutility and .
= Standard normal distribution of the combined variable.
2.2.6 Vector and matrix forms in measurement models of the Kalman filtering framework

Consider a homogeneous freeway segment without enter or exit ramps in between. The segment is divided into a number of sections of and is the length of a section. The modeling time horizon is discretized into , where denotes the modeling time index, and denotes the length of each simulation time step. We use to denote sampling time stamps, where denotes the sampling time index, and represents the length of each sampling time interval, e.g., 30 s or 5 min.

Two point sensor stations are located at upstream location and downstream location . The measurement equation for the vehicle counts at the upstream sensor can be expressed as

\[
\text{Cumulative normal curve of the combined variable } \mu_n. \\
\text{A variable to denote the equation } \mu_n. \\
\text{A variable to denote the equation } \mu_n.
\]

where denotes the true vehicle counts at upstream sensor, and denotes the measurement error term. is assumed to be normally distributed with zero mean and a variance of .

Generally, the cumulative upstream vehicle counts at each sampling time stamp can be derived from the observed vehicle counts:
where the summation of multiple normal random independent variables is the error of measured cumulative vehicle counts at sampled time. Because the sum of multiple normally distributed independent variables is normally distributed, the cumulative vehicle count follows a normal distribution.

To construct the cumulative vehicle counts at the non-sampled time stamps, we employed a linear interpolation method, shown below. For a time stamp, the corresponding cumulative vehicle counts can be derived as follows:

\[ \text{(3)} \]

Assuming the upstream detector produces unbiased measurements, we can express the mean value of a continuous cumulative arrival flow count as

\[ \text{(4)} \]

We can also derive the related error term, which is the combined error source, including the measurement error and the linear interpolation error.

Likewise, the cumulative departure flow count curve at the downstream station can be constructed.

Given deterministic cumulative departure and arrival flow counts, and at the upstream and downstream detectors, the three-detector problem considered by Newell (1993) aims to determine the traffic state at any intermediate detector location. The traffic state at the third detector location is represented by cumulative flow count value, and cell-based density, flow and speed measures can be derived easily as functions of.

As demonstrated in Fig. 2.1(b), the stochastic three-detector (STD) problem needs to estimate internal traffic states from its stochastic boundary inputs and, which include not only the measurement errors at the time stamps with data but also the possible interpolation errors. For illustration purposes, the measurements with errors are
represented by shaded circle points, and the boundary input between measurements needs
to be approximated through the aforementioned linear interpolation algorithm.

The range of uncertainty at the boundaries is highlighted by the rectangles at the
upstream and downstream locations, while the heights of the rectangles can be viewed as
the overall uncertainty level of the measurement error term. In comparison, the
deterministic three-detector model in Fig. 2.1(a) has error-free measurements and
sufficiently small sampling intervals, so the stochastic boundary at both ends are reduced
to solid lines that represent deterministic values of cumulative flow counts at the
boundaries.

2.2.7 Newell’s deterministic method for solving the three-detector problem

In Newell’s method for solving the deterministic three-detector problem, the
cumulative vehicle counts of any point in the interior of the boundary can be
directly evaluated from the boundary input and . Recognizing two types of
characteristic waves in the triangular shaped flow-density curve, the solution method
includes a forward wave propagation procedure and a backward wave propagation
procedure.

In the forward propagation procedure, a forward wave traverses free-flow travel
time from upstream at time — to a generic point at time . This leads to

\[ t \]
In the backward wave propagation procedure, a backward wave is emitted from the downstream boundary to the generic point \( x \) at time \( t \) inside the boundary. Because the wave pace of the backward wave is equal to \( \frac{v_{tr}}{x} \), and the density along the backward wave is \( \rho \) (according to the triangular shaped flow-density relationship), we have

\[
\text{(6)}
\]

Considering \( C \) as the distance from the downstream boundary to a point \( x \) inside the boundary, Newell’s method selects the smallest value of \( C \) between estimated values from the forward and backward wave propagation procedure:

\[
\text{(7)}
\]

If either procedure leads to a flow \( q \) that exceeded the capacity at \( \theta \), one needs to restrict \( q \) by a straight line with a slope equal to the capacity at \( \theta \).

Hurdle and Son (2001, 2002) and Son (1996) demonstrated the effectiveness and tested the computational efficiency of Newell’s method using field data. Daganzo (2003, 2005) presented an extension to the variational formulation of kinematic waves, where the fundamental diagram is relaxed to a concave flow-density relationship. Furthermore, Daganzo (2006) showed the equivalence between the kinematic wave with a triangular fundamental diagram and a simplified linear car, following a model similar to the one proposed by Newell (2002).

Figure 2.2 illustrates the conceptual framework of the proposed methodology. The conceptual framework starts from prior stochastic boundary estimates, which consists of a prior estimation of cumulative vehicle counts vector \( \mathbf{v} \) in block 1 and a prior estimation of variance-covariance matrix \( \mathbf{V} \) in block 2. These prior estimates of \( \mathbf{v} \) and \( \mathbf{V} \) can be extracted from historical information or available loop detector counts on both ends of a link. A series of linear measurement equations in block 3 are derived from the building blocks at the bottom half of Fig. 2.2.
2.2.8 Conceptual framework

Specifically, we developed a generalized least squares estimation method (i.e., the updating step of the Kalman filter) to update the stochastic boundary in terms of the cumulative vehicle counts vector in block 4 and the posterior estimation variance-covariance matrix in block 5, which further provide the final estimates of cell-based flow and density in blocks 12 and 13. Based on detailed sensor network settings in block 6, we developed linear measurement equations from heterogeneous data sources in block 7, which was constructed from the multinomial probit model and Clark’s approximation in block 8 as well as Newell’s simplified kinematic wave model in block 9. This single set of linear measurement equations provides the key modeling elements of linear
measurement matrix in block 10 and measurement error variance and covariance matrix in block 11.

2.3 Solving stochastic three-detector model using the multinomial probit model and Clark’s approximation

By extending Newell’s deterministic three-detector model as shown in Fig. 1(a), this section presents the model and solution algorithms for an STD problem, which aims to estimate the traffic state at any intermediate location on a homogeneous freeway segment using available measurements with various degrees of measurement errors. Mathematically, the proposed STD problem needs to consider a stochastic version of Eq. (7):

\[ \text{---} \quad \text{---} \quad , \quad (8) \]

where both cumulative arrival and departure flow counts are Normal random variables, as shown previously,

\[ \text{---} \quad \text{---} \quad \text{---} \quad , \quad \text{and} \quad (9) \]

\[ \text{---} \quad \text{---} \quad \text{---} \quad . \quad (10) \]

The key to solving the proposed Eq. (8) is the development of efficient approximation methods to estimate the cumulative vehicle counts at location at time. By assuming that the maximum of two normally distributed random variables can be approximated by a third normally distributed random variable, Clark (1961) proposed an approximation method to calculate the mean and variance (i.e., the first two moments) of the third Normal variable. In the field of discrete choice modeling (Daganzo, 1979), a multinomial probit model has been widely used to calculate the choice probability of an alternative based on a utility-maximization or a disutility-minimization framework, where the unobserved terms of alternative utilities are assumed to be normal distributions with possible correlation and heteroscedasticity structures. Daganzo et al. (1977) and Horowitz
et al. (1982) investigated the numerical accuracy of Clark’s approximation under a small number of alternatives.

By reformulating Eq. (8) within a disutility-minimization framework, the cumulative vehicle count is the minimum of the above two disutilities, corresponding to the forward wave and backward wave alternatives.

\[ \text{cumulative vehicle count} = \min(\text{disutility}_1, \text{disutility}_2) \]

where

\[ \text{disutility}_1 = \text{forward wave} \quad \text{and} \quad \text{disutility}_2 = \text{backward wave} \]  

(12)

It is easy to verify that the systematic disutility — and — , respectively, correspond to the forward or backward wave propagation procedures in Eqs. (5-6). The unobserved terms can be derived as — and — .

In this probit model framework, the choice probability of each alternative is equivalent to the probability of the forward wave vs. the backward wave being selected to determine the traffic state (i.e., free-flow vs. congested) of the current time-space location \((t, x)\). In this chapter, we further adopted Clark’s approximation method to estimate the mean and variance of the estimated cumulative flow count as

\[ \text{mean} = \text{expression} \]

(13)

where the mean

\[ \text{mean} = \text{expression} \]

(14)

and the variance

\[ \text{variance} = \text{expression} \]

(15)

Based on the notation system used in Sheffi (1985), the coefficients and can be further calculated by the following formulas.

\[ \text{formula} \]

(16)

\[ \text{formula} \]

(17)

There are several elements in Eqs. (16-17), including
(i) a parameter describing the standard deviation of the systematic disutility difference
\[ \sigma \]
where \( \sigma \) and \( \sigma^2 \) denote the variance of \( \sigma \) and \( \sigma^2 \), respectively, and \( \rho \) is the correlation coefficient between the error terms \( \epsilon \) and \( \eta \);

(ii) a standardized normal variable
\[ \Phi(\cdot) \]

(iii) a corresponding standard normal distribution function
\[ \Phi(\cdot) \]
and a cumulative normal distribution curve
\[ \Phi(\cdot) \]

In particular, Eq. (16) also show that the relative weights for the systematic disutilities and in the final mean estimate are jointly determined by the cumulative distribution functions and as well as an adjustment factor of that ranges between 0 and 1.

Because the deterministic three-detector model is a special case of the proposed STD model with error-free measurement, we can substitute \( \epsilon = 0 \) and \( \eta = 0 \) into Eqs. (14-20) to obtain the mean and variance of cumulative flow count in the following relationships between \( \mu \) and \( \sigma \):

\[ \mu = \mu_0 \]
\[ \sigma^2 = \sigma_0^2 \]

When solving the deterministic three-detector model by Clark’s approximation method, we obtain an error-free cumulative vehicle count through the simple minimization operation. This derivation confirms that the proposed method using Clark’s approximation can satisfactorily handle the deterministic three-detector model as a special case of the STD model.
2.4 Measurement models for heterogeneous data sources

Corresponding to blocks 8 and 9 of the conceptual framework in Fig. 2.2, the previous session proposed approximation formulas that can connect internal state with the stochastic boundary conditions. This session proceeds to establish a set of linear measurement equations that can map additional sensor measurements to the boundary conditions and . The following discussions detail the modeling components for blocks 3, 10 and 11 in Fig. 2 regarding the linear measurement equations shown below.

\[ \text{, where} \]

\[ \text{(23)} \]

Specifically, measurement vector can include flow counts and occupancy from additional point detectors, Bluetooth reader travel time measurements, and GPS vehicle trajectory data. Matrix provides a linear map between cumulative vehicle counts on the boundary, namely and and observations . The measurement error covariance matrix \( R \) is referred to as the combined error that includes error sources such as sensor measurement errors and approximation errors in the proposed modeling approach.

In general, more measurements would lead to less uncertainty in the boundary conditions. Fig. 2.3 illustrates three typical sensing configurations to reduce the estimation errors in the freeway traffic state estimation problem:

(i) deploying an additional point detector at the intermediate location, which can produce vehicle counts and occupancy measurements;
(ii) installing two prevailing AVI (e.g., mobile phone Bluetooth) readers, which can detect passing time stamps of individual vehicles;
(iii) equipping a certain percentage of vehicles with GPS mobile devices, which can produce semi-continuous vehicle trajectories for a short sampling interval, e.g., every 10 seconds.
2.4.1 Measurement equations for vehicle counts and occupancy from additional point detectors

In the analysis time period , an additional point sensor, located at , as shown in Fig. 2.3, produces vehicle count measurements. For simplicity, let us first assume that the counting process starts from an empty segment at time , and then we obtain a cumulative vehicle count at time stamp ,

\[ v(t) = \sum_{k=1}^{t} v_k \]

where is the observed link volume covering time period , denotes the constructed cumulative flow counts, and denotes the measurement error term of .

Within the proposed cumulative flow count-based estimation framework, the key to establishing a linear measurement equation is mapping vehicle count and occupancy measurements to the state value of and . Through Clark’s approximation formula in Eqs. (13-19), we can map the constructed cumulative flow count to the boundary conditions as.

Figure 2.3: Illustration of additional measurements from middle point sensor, AVI and GPS sensors.
where the combined error term includes both the measurement error and the estimation error in Clark’s approximation. Within the linear measurement framework

we can construct a transformed measurement of

the mapping vector and the system state vector

As an extension, if there are vehicles on the segment at time $t=0$, then we can reset $=0$ and adjust cumulative flow counts from the middle sensor to consider the additional number of vehicles that have already passed through but have not reached the end of segment.

A dual loop detector that includes two detectors at location and, where $l$ is the distance of the two detectors yields occupancy measurements that can be converted into local density (Cassidy and Coifman, 1997). By expressing the local density at time at location as a function of the estimated cumulative vehicle count and

we obtain the following linear measurement equations.

where the error term is the combination error term, including the measurement error and estimation error of and.
Unlike the standard linear mapping equation with a constant mapping matrix $H$, the mapping coefficients $a$ and $b$ in Eqs. (23) and (26) are dependent on the prevailing traffic conditions on the boundary, namely, the difference between $D_1$ and $D_2$. Because the true values of cumulative flow counts are unknown, only the estimates of cumulative departure and arrival flow counts are available to calculate $a$ and $b$ when constructing the linear measurement equations. This possible estimation error, associated with the boundary cumulative flow counts, introduces one more source of error that should be included in the combined error terms $a$ and $b$. On the other hand, as demonstrated in Eq. (21), when the standardized difference between $D_1$ and $D_2$, as shown in Eq. (19), is significantly large, the coefficients $a$ and $b$ take extreme values of 0 or 1, indicating that the internal condition at position $(t, x)$ can be estimated directly from one of the forward vs. backward wave propagation procedures with high confidence levels.

2.4.2 Measurement equation for AVI data

In this subsection, we show that the proposed methodology can effectively incorporate the AVI (Bluetooth data) data source.

As illustrated in Fig. 2.3, two Bluetooth readers are separately located at the upstream and downstream locations. For a tagged vehicle, its passing time stamps at the two readers are denoted $t$ and $t'$, respectively. To connect these samples with the cumulative vehicle counts at the both ends (i.e., unknown state variable in the freeway traffic state estimation problem), under a First-In-First-Out (FIFO) assumption for the three-detector model, we can establish the following conditions to ensure that the tagged vehicle has the same cumulative flow count number when passing through both the upstream and downstream stations. Under an error-free environment, we have

$$t = t'$$

while consideration of a combined error term leads to

$$t = t' + e$$

where

$$e$$

(29)

(30)
and where $\Sigma$ is the covariance of error term.

The combined error term includes possible deviation in identifying $\theta_1$ and $\theta_2$. To calculate the error range in identifying $\theta_1$, we first denote $\theta_1$ as a constant value for the likely feasible range of AVI readers’ clock drift errors and as the average flow rate around time $t$. Then, the standard deviation of the flow count deviation during a time duration of possible clock drifts is $\sigma_{\theta_1}$. According to Eq. (15), we can further consider the estimation uncertainty of $\theta_1$ and $\theta_2$ (before incorporating AVI data) as $\sigma_{\theta_1}$ and $\sigma_{\theta_2}$. Thus, the variance of the combined error can be approximated as $\sigma^2_{\theta_1} + \sigma^2_{\theta_2}$. (31)

In this case, a linear measurement equation can be established as follows:

$$\textbf{y} = \textbf{H}\textbf{x} + \textbf{v},$$

where $\textbf{y}$, $\textbf{H}$, and $\textbf{x}$ are the measured vector, measurement matrix, and system state vector, respectively. Note that the measurement term in the above form is expressed as $\textbf{y}$ rather than the original passing time stamp samples. Additionally, the mapping vector $\textbf{z}$, and the system state vector $\textbf{x}$. To consider AVI reader stations that are not located on the boundaries of segments, we can first map the passing time stamp measurements to the cumulative flow counts corresponding to the AVI reader locations, say, $\textbf{z}_1$ and $\textbf{z}_2$, where $\textbf{z}_1$ and $\textbf{z}_2$ are upstream and downstream locations of AVI readers. The second step is to connect $\textbf{z}_1$ and $\textbf{z}_2$ to the cumulative arrival and departure curves $\textbf{a}$ and $\textbf{d}$ at the boundary using the proposed stochastic three-detector model.

### 2.4.3 Measurement equation for GPS probe data

GPS probe data offer a semi-continuous trajectory of a vehicle in a segment. This section first extends the cumulative vehicle count-based approach in the previous section to construct measurement equations for each sample point along the trajectory. Second, we aim to use the local speed profile of the vehicle in our estimation framework.

As shown in Fig. 2.3, a vehicle of number $n$ traverses the segment along semi-continuous trajectory $\textbf{t}$, where $\textbf{t}$ denotes the sampling time
interval of GPS, and \( m \) denotes total number of sampling points for an individual vehicle trajectory.

By applying the proposed STD model, we can map the cumulative vehicle count \( m \) at a sampling point with the following boundary conditions:

\[ m_s = m_e + m_{err} \]  \hspace{1cm} (33)

where the combined error term \( m_{err} \) should include the following: (1) GPS location measurement errors; (2) the estimation error associated with the entry vehicle count \( m_e \); and (3) the estimation error of cumulative vehicle counts through the proposed STD model. The second type of error range can be approximated using a similar formula for AVI data, i.e., . According to Eq. (15), the variance of the third estimation error is

\[ \sigma^2 = \cdots \]  \hspace{1cm} (34)

Similar to the previous analysis, we can establish a linear measurement equation, shown below.

\[ z = Hx + v \]  \hspace{1cm} (35)

and where the transformed measurement term is

\[ \tilde{z} = Hx \]  \hspace{1cm} the system state vector

Typically, the location data of GPS probes are available second by second, and the adjacent locations of two sample points are used to compute the local speed measure. However, to reduce battery consumption and mitigate privacy concerns, some practical systems use a much longer time interval for data reporting, i.e., 30 seconds or 1 minute, while still sending local speed data (calculated from the internal second-by-second location data) to the data server.
To utilize the local speed measurement, we can convert local speed measurements into local density values. Fig. 2.4 shows the speed and density relationship. In the free-flow state, there are multiple density values corresponding to a constant free-flow speed, so one cannot deduce the unique density value in this case. On the other hand, during the congested state, because the vehicle-density relation is a monotonous curve, one can deduce the density from the speed measurement. By extending the measurement equation for local density in Eq. (28), we can incorporate the additional semi-continuous local speed data from GPS sensors.

2.5 **Uncertainty quantification**

2.5.1 Estimation Process using Kalman filtering

By considering the cumulative vehicle counts vector on the boundary as state vector \( N \), we can apply a Kalman filtering framework to use the proposed linear measurement equations for each measurement type and obtain a final estimate of the boundary conditions. Specifically, given the prior estimate vector \( \hat{x} \) and the prior estimate error variance-covariance matrix \( P \), the Kalman filter can derive the posterior estimate error variance-covariance and posterior estimate of using the following updated formula:

\[
(36)
\]
where denotes the optimal Kalman filter gain factor:

When there are two sensors available on a single segment, one can directly use sensor data to construct the prior estimate vectors and through Eqs. (2-4). When there is only one sensor available on a segment, one must provide a rough guess of the unobserved boundary values, which leads to a much larger prior estimation error range for .

The proposed estimation framework uses cumulative flow counts as the state variable, which should be a non-decreasing time series at a certain location. Nevertheless, due to various sources of estimation errors, it is possible but less likely that the non-decreasing property of the estimated cumulative vehicle counts does not hold, and the corresponding derived flow can be negative. A standard Kalman filtering framework, as described in Eqs. (36-38), does not consider inequality constraints. For simplicity, this chapter does not impose additional non-negativity constraints into the Kalman filtering framework to ensure that the derived flow is larger or greater than zero, and the negative flow volume can be easily corrected by a post-processing procedure. This post-processing technique is also used in the general field of vehicle tracking, where a vehicle is typically moving forward, but the instantaneous speed might be estimated as negative due to various estimation errors.

In general, Kalman filtering is used in online recursive estimation and prediction applications. In this chapter, we focused on the offline traffic state estimation problem, and the Kalman filter was used as a generalized least squares estimator. Interested readers are referred to the dissertation by Ashok (1996) on the equivalence between these two estimators.

2.5.2 Quantifying the density estimation uncertainty and the value of information

To evaluate the benefit of a possible sensor deployment strategy, we need to quantify the uncertainty reduction of the internal traffic state , which can be derived from the boundary conditions using the proposed STD model.
Furthermore, the density between intermediate position $i$ and $j$ at time $t$ can be directly calculated from cumulative counts:

$$
(39)
$$

According to Eqs. (14-15) in the proposed STD model, we can derive the mean and variance of the cumulative vehicle count estimates at any given location $i$ and time $t$. Let $\mu$ and $\sigma^2$ denote the mean and variance of density, respectively. First, we obtain:

$$
(40)
$$

For simplicity, we can ignore the possible correlation between estimated adjacent cumulative flow counts and quantify the uncertainty associated with the density estimate as:

$$
(41)
$$

Similarly, we can derive the uncertainty measure for local flow rates. To estimate the uncertainty associated with local speed estimates, one can construct a linear mapping function between speed and density, as shown in the piecewise dashed line in Fig. 4, and then derive the speed estimation uncertainty as a function of the density estimation uncertainty.

To quantify the system-wide estimation uncertainty, one can simply tally the cell-based density estimation uncertainty across all cells on a segment and all simulation/modeling time intervals. Additional discussion on possible value of information measures in a Kalman filtering framework can be found in recent studies by Zhou and List (2010) on the origin-destination demand estimation problem, and Xing and Zhou (2011) on the path travel time estimation/prediction problem. Typically, when the total variance of traffic state estimation errors is smaller, the value of the information that can be obtained from the underlying sensor network is larger.
2.6 **Numerical Experiments**

In this section, we used a set of simulated experiments to investigate the performance of the proposed STD model on a 0.5-mile homogeneous segment with no entry or exit ramps, as shown in Fig. 2.5. The segment is divided into 10 sections, and the time of interest ranges from 0 to 1,200 s. Two loop detectors are installed at the upstream and downstream ends.

![Figure 2.5: A homogeneous segment used for conducting experiments (mile).](image)

The other important parameters include a triangle-shaped flow-density relation, as shown in Fig. 2.6, where the free-flow speed $\nu$, the backward wave speed $\gamma$, and the maximum density $\rho_m$.

![Figure 2.6: Triangular shaped flow-density curve and the shockwave speeds in this experiment](image)

In this experiment, we consider a constant arriving flow rate $u = 1200$ veh/h $t \in [0,1200]$, while the downstream bottleneck discharge rate $\lambda$ is assumed to be time-dependent, i.e., $\lambda(t) = \begin{cases} 600 \text{ veh/h} & t \in [0,450] \\ 1800 \text{ veh/h} & t \in [451,1200] \end{cases}$. 

...
2.6.1 Estimations results of the STD model

Using the deterministic three-detector approach, the first step was to generate the ground truth boundary conditions in terms of deterministic arrival and departure cumulative vehicle count curves, as shown in Fig. 2.7. In particular, there are three shockwaves:

(1) The first shockwave travels at a speed of 4 m/h, resulting in a long queue in the segment. When it finally spills back to the upstream site, the flow detected at the upstream sensor (compared to the actual arrival flow of 1,200 veh/h) is controlled by the bottleneck capacity of 600 veh/h.

(2) The second backward recovery shockwave starts to propagate upstream at a speed of 12 m/h, right after the bottleneck capacity recovers to 1,800 veh/h at a time of 451 s.

(3) The third shockwave is triggered by the transition where the arrival rate of 1,200 veh/h, starting at a time of 701 s, is lower than the normal bottleneck capacity.

The second step is to test the ability to capture the shockwave propagation using the proposed STD model. The corresponding stochastic boundary conditions, in terms of prior estimation cumulative vehicle counts vector $\hat{\mathbf{z}}$ and a prior estimation variance-covariance matrix $\mathbf{H}_{\hat{\mathbf{z}}\hat{\mathbf{z}}}$, were constructed under a sampling time interval $\Delta t = 300$ s, with a +/-10% measurement standard deviation. Based on $\hat{\mathbf{z}}$ and $\mathbf{H}_{\hat{\mathbf{z}}\hat{\mathbf{z}}}$, the STD model is able to produce the cell-based density estimates for all 10 sections inside the segment, shown in Fig. 2.8, and the corresponding uncertainty range for each cell in the space-time diagram, shown in Fig. 2.9.

As expected, Fig. 2.8 clearly shows the transition of the following four regimes: (1) free-flow (FF); (2) severe congestion (SC); (3) mild congestion (MC); and (4) free-flow. The boundaries of those regimes correspond to the underlying shockwaves.

To further demonstrate the computational details of the proposed STD model, let us consider a series of time stamp points at section 8, marked in Fig. 2.8. These seven points are numbered by time from 1 to 7, and each point corresponds to a particular traffic mode. Specifically, four points of interest, 1, 3, 5 and 7, are under the steady traffic.
state mode, and the other three points are in the transition boundaries. Table 2 shows the values of Clark’s approximation for estimating the mean and variance of the cumulative flow count using Eqs. (20-22).

![Figure 2.7: Arrival and departure cumulative vehicle count curves.](image)

![Figure 2.8: The original cell based density estimation profile. Color denotes the density of each cell in veh/mile.](image)
Table 2.2: Values of Clark’s approximation under different traffic mode / transition

<table>
<thead>
<tr>
<th>Point</th>
<th>Traffic Mode/Transition</th>
<th>Time (min)</th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>FF</td>
<td>2</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>33.33</td>
<td>45.83</td>
</tr>
<tr>
<td>2</td>
<td>FF SC</td>
<td>3.3</td>
<td>0.3</td>
<td>0.5</td>
<td>0.5</td>
<td>58.33</td>
<td>58.33</td>
</tr>
<tr>
<td>3</td>
<td>SC</td>
<td>6</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>113.3</td>
<td>85.83</td>
</tr>
<tr>
<td>4</td>
<td>SC MC</td>
<td>8.5</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>163.3</td>
<td>116.5</td>
</tr>
<tr>
<td>5</td>
<td>MC</td>
<td>11</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>205.1</td>
<td>191.5</td>
</tr>
<tr>
<td>6</td>
<td>MC FF</td>
<td>13.2</td>
<td>0.8</td>
<td>0.5</td>
<td>0.5</td>
<td>257.0</td>
<td>257.0</td>
</tr>
<tr>
<td>7</td>
<td>FF</td>
<td>16</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>313.3</td>
<td>328.6</td>
</tr>
</tbody>
</table>

In Eqs. 15-17 for generating the final cumulative flow count estimates, the cumulative normal distribution of the combined variable $\Phi(\gamma)$ and $\Phi(-\gamma)$ is the weights for forward wave vs. backward wave alternatives. Based on the numerical results in Table 2.2, we have the following interesting findings.

1. When the difference of systematic disutility, $V_u$ and $V_d$, is significantly large, the weight on each alternative, $\Phi(\gamma)$ and $\Phi(-\gamma)$, has an extreme value of zero or one, and the corresponding adjustment factor $\alpha \phi(\gamma)$ is close to zero. It should be noted that, although Table 2.2 shows a value of zero for $\alpha \phi(\gamma)$, it is actually a very small numerical value. By substituting $\alpha \phi(\gamma)=0$ into the mean and variance estimation equation in Eqs. 16-17, we can verify that and for points 1 and 7, indicating that the uncertainty of the final estimate is controlled by the dominating alternative.

2. In cases of state transitions, i.e., free-flow to congested or congested to free-flow, $\Phi(\gamma)$ and $\Phi(-\gamma)$ stay at a level of 0.5, leading to almost equal weights for each alternative, and a positive adjustment factor $\alpha \phi(\gamma)$ is needed. More interestingly, this case results in a large uncertainty or low confidence level about its exact value of the cumulative flow count, and the variance is jointly determined by both alternatives.

The overall uncertainty plot in Fig. 2.9 for each cell confirms our findings; that is, the boundaries of the state transition have large uncertainty. In addition, the estimation generally increases when the time clock advances, as the measurement error in flow counts from the previous time intervals must be included in the cumulative flow count.
variable that appears later. Likewise, in Fig.2.8, the contour of the shockwaves can be captured. Later, we compare this figure with a posterior density uncertainty profile to test the performance of a series of measurements.

2.6.2 VOI for heterogeneous measurements

From this point on, we are interested in the value of information of the following (additional) sensor network enhancement strategies:

(1) providing a higher resolution for the existing boundary sensors by reducing the sampling time interval;

(2) deploying an additional sensor between the original pair of sensors, at $x = 0.3$ miles (using vehicle count measurements, i.e., Eq. 26);

(3) locating a pair of Bluetooth readers at the upstream and downstream boundaries, with a Bluetooth travel time reader measurement standard deviation $\text{sec}$ (using travel time measurements, i.e., Eq. 32);

(4) equipping a certain percentage of vehicles with GPS mobile devices with a sampling time interval $\text{sec}$ along each probe vehicle trajectory (using vehicle number observations, i.e., Eq. 35).

Figure 2.9: The original density uncertainty profile of cell based density estimation. Color denotes the estimated density variance of each cell.
Conceptually, these additional measurements are used to enhance the estimates and reduce the estimation uncertainty of cumulative vehicle counts at the upstream and downstream boundaries.

Here, we adopt the density uncertainty to measure the VOI, which is defined as the inverse of sum of the estimated density variance of all cells. Fig. 2.10 displays the estimation performance improvement for the first two scenarios. Specifically, the VOI of the density estimation increases with a finer sampling time resolution of the existing sensors in the boundary. Keeping the same sampling resolution, the added middle sensor can produce additional VOI by an average of 10%.

We then varied the market penetration rates from 10% to 90% for scenarios 3 and 4. As expected, the results shown in Fig. 2.11 indicate that both AVI and GPS measurements can significantly enhance the confidence level of the microscopic state estimation when the individual market penetration rate increases. Under the same market penetration rate of probe vehicles, the semi-continuous location-based samples from GPS sensors contribute more information than AVI readings, which are available only at the boundaries of the segment.

![Figure 2.10: Value of Information vs. sampling time interval. (a) existing sensors; (b) additional middle sensor.](image-url)
We now consider an integrated case with scenarios 2, 3 and 4 using the following settings: existing loop detectors at boundaries with a 5-min sampling time interval, an additional sensor at $x = 0.3$ miles with a 5-min sampling time interval, and a randomly selected portion of vehicles (10%) that are equipped with AVI Bluetooth and GPS sensors.

![Comparable total uncertainty reduction curve for GPS and AVI in different market penetration rate.](image)

**Figure 2.11:** Comparable total uncertainty reduction curve for GPS and AVI in different market penetration rate.

The proposed information-theoretic approach produces the posterior estimation cumulative vehicle counts vector and variance-covariance matrix. Comparing the

![A posterior estimation density uncertainty profile. Color denotes the estimated density variance of each cell.](image)

**Figure 2.12:** A posterior estimation density uncertainty profile. Color denotes the estimated density variance of each cell.
original estimated density uncertainty profile in Fig. 2.9 and Fig. 2.12 for the above integrated sensor network setting, we find that overall uncertainty has been dramatically reduced, but the cells corresponding to the back of the queue still have large uncertainty due to the inherent difficulty in estimating the exact probability of free-flow and congestion state between those state transition boundaries.

2.6.3 Preliminary discussions of modeling errors

The proposed model provides a theoretically rigorous mechanism for estimating internal traffic states on a freeway segment, but it is important to recognize possible modeling errors pertaining to the perfect triangular flow-density relationship, which is a key underlying assumption for both Newell’s kinematic wave model and the widely used CTM. By carefully examining our estimation results based on an NGSIM data set (FHWA, 2008), which provides detailed trajectory data based on video recordings at 0.1-s intervals, we identified the following possible modeling errors associated with the triangular flow-density relationship for both the deterministic and stochastic three-detector model.

(1) Constant jam density . As an inverse of jam density, critical spacing could be much larger for trucks than for regular passenger vehicles. There are also significant variations in depending on the driving conditions.

(2) Variations in backward wave speed . Many studies (e.g., Kim and Zhang, 2008) have investigated stochasticity in .

(3) Free-flow speed . Preferred free-flow speeds vary among individual drivers.

Particularly under congested conditions, the modeling errors in STD’s key formula can be decomposed into the following elements.

(1) Estimation errors in the boundary cumulative count , which have been systematically addressed in this chapter.
(2) Time index refereeing errors in —. Let us denote as the assumed backward wave speed in calculation and consider as the true backward wave speed. In this case, then the time index referencing error is — —, which can further lead to the counting error of — —.

(3) Uncertainty and variations associated with . The assumed jam density value can lead to an adjustment factor error of , where denotes the true jam density.

Likewise, under the free-flow condition, we can derive the modeling errors associated with variability of in the first component — of the minimization equation. Other error sources include the FIFO principle, which can be violated by complex lane changing behavior.

2.7 Conclusions

While there is a growing body of work on the estimation of traffic states from different sources of surveillance techniques, much of the prior work has focused on single representations, including loop detectors, GPS data, AVI tags, and other forms of vehicle tracking. This chapter investigated cumulative flow count-based system modeling methods that estimate macroscopic and microscopic traffic states with heterogeneous data sources on a freeway segment. Through a novel use of the multinomial probit model and Clark’s approximation method, we developed a stochastic three-detector model to estimate the mean and variance-covariance estimates of cumulative vehicle counts on both ends of a traffic segment, which are used as probabilistic inputs for estimating cell-based flow and density inside the space-time boundary and to construct a series of linear measurement equations within a Kalman filtering estimation framework. This chapter presented an information-theoretic approach to quantify the value of heterogeneous traffic measurements for specific fixed sensor location plans and market penetration rates of Bluetooth or GPS flow car data.
Further research will focus on the following three major aspects. First, the proposed single-segment-oriented methodology will be further extended for a corridor model with merges/diverges for possible medium-scale traffic state estimation applications. Second, the proposed model for the traffic state estimation problem can be further extended to a real-time recursive traffic state estimation and prediction framework involving multiple OD pairs with stochastic demand patterns or road capacities. Third, given the microscopic state estimation results, one can quantify the uncertainty of other quantities in many emerging transportation applications, e.g., fuel consumption and emissions that mainly dependent on cell-based or vehicle-based speed and acceleration measures; and link-based travel times that can be related to the cumulative vehicle counts on the boundary.
CHAPTER 3. SENSOR LOCATION OPTIMIZATION

With a particular emphasis on the end-to-end travel time prediction problem, this chapter proposes an information-theoretic sensor location model that aims to maximize information gains from a set of point, point-to-point and probe sensors in a traffic network. Based on a Kalman filtering structure, the proposed measurement and information quantification models explicitly take into account several important sources of errors in the travel time estimation/prediction process, such as the uncertainty associated with prior travel time estimates, measurement errors and sampling errors. After thoroughly examining a number of possible measures of information gain, this chapter selects a path travel time prediction uncertainty criterion to construct a joint sensor location and travel time estimation/prediction framework. We further discuss how to quantify information gain for steady state historical databases and point-to-point sensors with multiple paths, and a heuristic beam-search algorithm is developed to solve the combinatorial sensor selection problem. A number of illustrative examples are used to demonstrate the effectiveness of the proposed methodology.

3.1 Literature review

Based on the types of measurement data, traffic sensors can be categorized into three groups, namely point sensors, point-to-point sensors, and probe sensors. Point sensors collect vehicle speed (more precisely, time-mean speed), volume and road occupancy data at fixed locations. With point detectors having significant failure rates, existing in-pavement and road-side traffic detectors are typically instrumented on a small
subset of freeway links. Point-to-point sensors can track the identities of vehicles through mounted transponder tags, license plate numbers, or mobile phone Bluetooth signals, as vehicles pass multiple but non-contiguous reader stations. A raw tag read typically records a vehicle ID number, the related time stamp, and the location. If two readers at different locations sequentially identify the same probe vehicle, then the corresponding data reads can be fused to calculate the reader-to-reader travel time and the counts of identified vehicles between instrumented points.

Automatic license plate matching techniques have been used in the traffic surveillance field since the 1970s, and many statistical and heuristic methods have been proposed to reduce reading errors to provide reliable data association (Turner et al., 1998). Many feature-based vision and pattern recognition algorithms (e.g. Coifman et al., 1998) have been developed to track individual vehicle trajectories using camera surveillance data. Radio Frequency Identification (RFID) technologies first appeared in Automated Vehicle Identification (AVI) applications during the 1980s and has become a mature traffic surveillance technology that produces various traffic measures with high accuracy and reliability. Currently, many RFID-based AVI systems are widely deployed in road pricing, parking lot management, as well as real-time travel time information provision. For instance, prior to 2001, around 51 AVI sites were installed and approximately 48,000 tags had been distributed to users in San Antonio, United States, which represents a 5% market penetration rate. Additionally, Houston’s TranStar fully relies on AVI data to provide travel time information currently (Haas et al., 2001). Many recent studies (e.g. Wasson et al., 2008, Haghani et al., 2010) started to use mobile phone Media Access Control (MAC) addresses as unique traveler identifiers to track travel time for vehicles and pedestrians.

Many Automatic Vehicle Location (AVL) technologies, such as Global Positioning System (GPS), and electronic Distance Measuring Instruments (DMI’s) provide new possibilities for traffic monitoring to semi-continuously obtain detailed passing time and location information along individual vehicle trajectories. As the personal navigation market grows rapidly, probe data from in-vehicle Personal Navigation Devices (PND) and cell phones become more readily available for continuous
travel time measurement. On the other hand, privacy concerns and expensive one-time installation costs are two important disadvantages influencing the AVL deployment progress.

Essentially, any application of real-time traffic measurements for supporting Advanced Traveler Information Systems (ATIS) and Advanced Traffic Management Systems (ATMS) functionalities involves the estimation and/or prediction of traffic states. Depending on underlying traffic process assumptions, the existing traffic state estimation and prediction models can be classified into three major approaches: (1) approach purely based on statistical methods, focusing on travel time forecasting, (2) approach based on macroscopic traffic flow models, focusing on traffic flow estimation on successive segments of a freeway corridor, (3) approach based on dynamic traffic assignment models, focusing on wide-area estimation of origin-destination trip demand and route choice probabilities so as to predict traffic network flow patterns for links with and without sensors. In this research, we are interested in how to place different types of sensors to improve information gains for the first statistical method-based travel time prediction applications.

In sensor location models for the second approach, significant attention (e.g., Liu and Danczyk, 2009, Danczyk and Liu, 2011, and Leow et al., 2008) has been devoted to placing point detectors along a freeway corridor to minimize the traffic measurement errors of critical traffic state variables, such as segment density and flow. The traffic origin-destination (OD) matrix estimation problem is also closely related to the travel time estimation problem under consideration. To determine the priority of point detector locations, there are a wide range of selection criteria, to name a few, “traffic flow volume” and “OD coverage” criteria proposed by Lam and Lo (1990), a “maximum possible relative error (MPRE)” criterion proposed by Yang et al. (1991) that aims calculate the greatest possible deviation from an estimated demand table to the unknown true OD trip demand.

Based on the trace of the a posteriori covariance matrix produced in a Kalman filtering model, Zhou and List (2010) proposed an information-theoretic framework for locating fixed sensors in the traffic OD demand estimation problem. Related studies
along this line include an early attempt by Eisenman et al. (2006) that uses a Kalman filtering model to minimize the total demand estimation error in a dynamic traffic simulator and a recent chapter by Fei and Mahmassani (2011) that considers additional criteria, such as OD demand coverage, within a multi-objective decision making structure. Furthermore, in the travel time estimation problem, the Kalman filtering based framework has also been employed by many researchers. For instance, an ensemble Kalman filtering model is proposed by Work et al. (2008) to estimate freeway travel time with probe measurements.

Several recent studies have been conducted on the sensor location problem from different perspectives. Chen et al. (2004) studied the AVI reader location problem for both travel time and OD estimation applications. They presented the following three location section criteria: minimizing the number of AVI readers, maximizing the coverage of OD pairs, and maximizing the number of AVI readings. To maximize the information captured with regard to the network traffic conditions under budget constraints, Lu et al. (2006) formulated the roadside servers locating problem as a two-stage problem. The first stage was a sensitivity analysis to identify a subset of links on which the flows have large variability of travel demand, and more links were gradually selected to maximize the overall sensor network coverage in the second stage. Sherali et al. (2006) proposed a discrete optimization approach for locating AVI readers to estimate corridor travel times. They used a quadratic zero-one optimization model to capture travel time variability along specified trips. In a recent chapter by Ban et al. (2009), link travel time estimation errors are selected as the optimization criterion for point sensor location problems, and a dynamic programming-based solution method is constructed to optimize the location of point sensors on link segments along a corridor. Li and Ouyang (2011) proposed a reliable sensor location method that considers probabilistic sensor failures, and developed a Lagrangian relaxation based solution algorithm.
3.2 Proposed approach

While significant progress has been made in formulating and solving the sensor location problem for travel time estimation and prediction, a number of challenging theoretical and practical issues remain to be addressed.

First, the optimization criteria used in the existing sensor location models typically differ from those used in travel time estimation and prediction. Due to the inconsistency between the two models, the potential of scarce sensor resources might not be fully achieved in terms of maximizing information gain for travel time estimation/prediction. For example, an AVI sensor location plan that maximizes sensor coverage does not necessarily yield the least end-to-end travel time estimation and prediction uncertainty if there are multiple likely paths between pairs of AVI sensors. As a result, a simplified but unified travel time estimation and prediction model for utilizing different data sources is critically required as the underlying building block for the sensor network design problem.

Second, most of the existing studies typically focus on real-time speed estimation errors (when using measured speed from point sensors to approximate speed on adjacent segments without sensors), they do not explicitly take into account uncertainty reduction and propagation in a heterogeneous sensor network with both point and point-to-point travel time measurements, as well as possible error correlation between new and existing sensors.

Third, how to quantify the information loss in an integrated travel time and prediction process, especially under non-recurring traffic conditions, has not received sufficient attention. Under recurring conditions, the traffic is more likely to be estimated and predicted accurately for links with sensor measurements. For locations without sensors, one can resort to historical information (e.g. through limited floating car studies) or adjacent sensors to approximate traffic conditions. However, under non-recurring traffic conditions due to incidents or special events, without real-time measurements from impacted locations, traffic management centers or traffic information provision
companies might still offer biased traffic information, based on outdated historical estimates or incorrect approximation from unimpacted neighboring detectors.

By extending a Kalman filtering-based information theoretic approach proposed by Zhou and List (2010) for OD demand estimation applications, this research focuses on how to analyze the information gain for real-time travel time estimation and prediction problem with heterogeneous data sources. Since the classical information theory proposed by Shannon (1948) on measuring information gain related to signal communications, the sensor location problem has been an important and active research area in the fields of electrical engineering and information science. Various measures have been used to quantify the value of sensor information in different sensor network applications, where the unknown system states (e.g. the position and velocity of targets studied by Hintz and McVey, 1991) can typically be directly measured by sensors. In comparison, sensing network-wide travel time patterns is difficult in its own right because point sensors only provides a partial coverage of the entire traffic state. Using AVI data involves complex spatial and temporal mapping from raw measurements, and AVL data are not always available on a fixed set of links, especially under an early sensor network deployment stage.

There are a wide range of time series-based methods for traffic state estimation, and many studies (e.g. Okutani and Stephanedes (1984); Zhang and Rice, 2003; Stathopoulos and Karlaftis, 2003) have been devoted to travel time prediction using Kalman filtering and Bayesian learning approaches. To extract related statistics from complex spatial and temporal travel time correlations, a recent chapter by Fei et al. (2011) extends the structure state space model proposed by Zhou and Mahmassani (2007) to detect the structural deviations between the current and historical travel times and apply a polynomial trend filter to construct the transition matrix and predict future travel time. In this chapter, we aim to present a unified Kalman filtering-based framework under both recurring and non-recurring traffic conditions. More importantly, a spatial queue-based cumulative flow count diagram is introduced to derive the important transition matrix for modelling traffic evolution under non-recurring congestions. Different from existing data-driven or time-series-based methods, this chapter derives a series of point-queue-
model-based analytical travel time transition equations, which lay out a core modeling building block for quantifying prediction uncertainty. In addition, a steady-state uncertainty formula is presented to fully capture day-to-day uncertainty evolution and convergence of the sensor network in a long-term horizon.

We first introduce the notation used in the travel time prediction and sensor network design problems.

### Notation and problem statement

#### 3.3 Sets and Subscripts:

- **$N$** = set of nodes.
- **$A$** = set of links.
- $m = \text{number of links in set } A$.
- **$A'$** = set of links with point sensors (e.g. loop detectors), $A' \subseteq A$.
- **$N^*$** = set of nodes with point-to-point sensors, $N^* \subseteq N$.
- **$A^*$** = set of links with reliable probe sensor data, $A^* \subseteq A$.
- **$\bar{A}'$** = sets of links that have been equipped with point sensors, $\bar{A}' \subseteq A'$.
- **$\bar{N}^*$** = sets of nodes that have been equipped with AVI sensors, $\bar{N}^* \subseteq N'$.
- $n', n'', n''' = \text{numbers of measurements, respectively, from point sensors, point-to-point sensors and probe sensors.}$
- $n = \text{number of total measurements, } n = n'+n''+n'''$.
- **$t$** = time index for state variables.
- **$h$** = travel time prediction horizon.
- **$d$** = subscript for day index.
- **$o$** = subscript for origin index, $o \in O$, $O = \text{set of origin zones.}$
- **$s$** = subscript for destination index, $s \in S$, $S = \text{set of destination zones.}$
- **$a, b$** = subscript for link index, $a, b \in A$.
- **$i, j$** = subscript for node index, $i, j \in N$.
- **$k, \lambda$** = subscript for path.
- **$p(i, j, k)$** = set of links belong to path $k$ from node $i$ to node $j$. 
3.3.2 Estimation variables

\( t_{d,a} = \) travel time of link \( a \) on day \( d \).

\( t_{d,o,s,k} = \) travel time on path \( k \) from origin \( o \) to destination \( s \), on day \( d \),

\[
t_{d,o,s,k} = \sum_{a \in p(o,s,k)} t_{d,a}.
\]

3.3.3 Measurements

\( y'_{d,a} = \) single travel time measurement from a point sensor on link \( a \), on day \( d \).

\( y''_{d,i,j,k} = \) single travel time measurement from a pair of AVI readers on path \( k \) and day \( d \)
from node \( i \) to node \( j \), where the first and second AVI sensors are located at nodes \( i \) and
node \( j \), respectively.

\( y'''_{d,a} = \) a set of travel time measurements from a probe sensor that contain map-matched
travel time records on links \( a \) on path \( k \) and day \( d \) from node \( i \) to node \( j \), where
\( a \in p(i,j,k) \).

3.3.4 Vector and matrix forms in Kalman filtering framework

\( Y_d = \) sensor measurement vector on day \( d \), consisting of \( n \) elements.

\( T_d = \) travel time vector on day \( d \), consisting of \( m \) elements \( t_{d,a} \).

\( T_d^a = \) a priori estimate of the mean values in the travel time vector on day \( d \), consisting of
\( m \) elements.

\( T_d^p = \) a posteriori estimate of the mean values in the travel time vector on day \( d \),
consisting of \( m \) elements.

\( T_d^h = \) historical regular travel time estimates using data up to day \( d \).

\( V_d = \) structural deviation on day \( d \).

\( P_d^a = \) a priori variance covariance matrix of travel time estimate, consisting of \((m \times m)\)
elements.

\( P_d^p = \) a posteriori error covariance matrix, i.e. conditional covariance matrix of estimation
errors after including measurements.

\( \Sigma = \) a priori variance covariance matrix of structure deviation, consisting of \((m \times m)\)
elements.
\( \Sigma^* \) = a posteriori variance covariance matrix of structure deviation.
\( \overline{\mathbf{r}} \) = vector of regular historical mean travel time estimates, consisting of \( m \) elements, \( \overline{\mathbf{r}} = \mathbf{T}_h^r \).
\( \overline{\mathbf{P}} \) = error covariance matrix of historical travel time estimate, consisting of \((m \times m)\) elements, \( \overline{\mathbf{P}} = \mathbf{P}_0^- \).
\( H_d \) = sensor matrix that maps unknown travel times \( T_d \) to measurements \( Y_d \), consisting of \((n \times m)\) elements.
\( K_d \) = updating gain matrix, consisting of \((n \times m)\) elements, on day \( d \).
\( K_{d}^{NR} \) = updating matrix for non-recurring traffic estimations on day \( d \).
\( L_d(t, t+h) \) = non-recurring traffic transition matrix from time \( t \) to \( t+h \) on day \( d \).
\( w_d \) = system evolution noise vector for link travel times, \( w_d \sim N(0, \mathbf{Q}_d) \).
\( Q_d \) = system evolution noise variance-covariance matrix, on day \( d \).
\( \mu_d \) = non-recurring derivation evolution noise vector for link travel times, \( \mu_d \sim N(0, \mathbf{Q}_d^{\mu}) \).
\( Q_d^{\mu} \) = non-recurring derivation evolution noise variance-covariance matrix, on day \( d \).
\( q_{d,a} \) = systematic travel time variance on link \( a \).
\( \varepsilon_d \) = combined measurement error term, \( \varepsilon_d \sim N(0, \mathbf{R}_d) \), on day \( d \).
\( \mathbf{R}_d \) = variance-covariance matrix for measurement errors, on day \( d \).

3.3.5 Parameters and variables used in measurement and sensor design models

\( \phi_{i,j,k,a} \) = path-link incidence coefficient, \( \phi_{i,j,k,a} = 1 \) if path \( k \) from node \( i \) to node \( j \) passes through link \( a \), and 0 otherwise.
\( \tilde{\gamma}^m_{d,a} \) = stochastic link traversing coefficient for GPS probe vehicles, \( \tilde{\gamma}^m_{d,a} = 1 \) if GPS probe vehicles pass through link \( a \) on day \( d \), and 0 otherwise.
\( e_{d,o,s,k} \) = path travel time estimation error on path \( k \) from origin \( o \) to destination \( s \).
\( f_{o,s,k} \) = traffic flow volume on path \( k \) from origin \( o \) to destination \( s \).
\( TU_d \) = total path travel time estimation uncertainty on day \( d \).
\( \alpha \) = market penetration rate for vehicles equipped with AVI sensors/tags.
\( \beta \) = market penetration rate for vehicles equipped with AVL sensors.
\( l \) = subscript of sensor design solution index.

\( X_i = \) \( i^{th} \) sensor design solution, represented by \( X_i = [A', N^*, A'^*, \alpha, \beta] \).

\( X^* \) = optimal sensor design solution.

\( z(X_i) \) = overall information gain (i.e. performance function) for a given sensor design scenario \( X_i \).

Consider a traffic network with multiple origins \( o \in O \) and destinations \( s \in S \), as well as a set of nodes connected by a set of directed links. We assume the following input data are available:

1. The prior information on historical travel time estimates, including a vector of historical mean travel time estimates \( \bar{T} \) and the corresponding variance-covariance matrix \( \bar{P} \).
2. The link sets with point sensor and point-to-point AVI sensor data, specified by \( \bar{A} \) and \( \bar{N} \).
3. Estimated market penetration rate \( \alpha \) for point-to-point AVI sensors.
4. Estimated market penetration rate \( \beta \) for probe sensors, and set of links with accurate probe data \( A^* \).

The sensor network to be designed and deployed will include additional point sensors and point-to-point detectors that lead to sensor location sets of \( A' \) and \( N^* \), where \( \bar{A}' \subseteq A' \), \( \bar{N}^* \subseteq N^* \). In the new sensor network, through GPS map-matching algorithms, GPS probe data can be converted from raw longitude/latitude location readings to link travel time records on a set of links \( A^* \). In this chapter, we assume that probe data will be available through a certain data sharing program, (e.g. Herrera and Bayen, 2010), from vehicles equipped with Internet-connected GPS navigation systems or GPS-enabled mobile phones. It should be noticed that, depending on the underlying map-matching algorithm and data collection mechanism, only a subset of links in a network, denoted by \( A^* \) can produce reliable GPS map-matching results. For example, it is very difficult to distinguish driving vs. walking mode on arterial streets through data from GPS-equipped mobile phones, so typically only travel time estimates on freeway links are considered to be reliable in this case.
One of the key assumptions in our chapter is that the historical travel time information can be characterized by the \textit{a priori} mean vector $\overline{T}$ and the estimation error variance matrix $\overline{P}$. If point sensor or point-to-point data are available from sets $\overline{A}$ and $\overline{N}$, then we can construct the mean travel time vector $\overline{T}$, and estimate the variance of estimates in the diagonal elements of corresponding variance-covariance matrix $\overline{P}$. For links without historical sensor measurements, the travel time mean estimate can be approximated by using national or regional travel time index (e.g. 1.2) and set the corresponding variance to a sufficient large value or infinity. One can assume zero for the correlation of initial travel time estimates. In the case of a complete lack of historical demand information, we can set $(\overline{P})^{-1} = 0$.

It should be remarked that, measurements from a point sensor are typically instantaneous speed values observed at the exact location of the detector. Using a section-level travel time modeling framework (e.g., Lindveld et al., 2000), a homogenous physical link can be decomposed into multiple cells or sections, with the speed measurement directly reflecting only the section where the sensor is located. In some previous studies, the link or corridor speed can be estimated using the section based speed, while cells without sensors using approximated values from adjacent instrumented sections. As shown in Fig. 3.1, the travel times on section A and D are directly measured using sensors 1 and 2, respectively. Meanwhile, the travel times for sections B, C and E, as well as the entire corridor, are estimated using upstream and downstream sensors. There are a number of travel time reconstruction approaches, such as constant speed based methods and trajectory methods (Van Lint and Van der Zijpp, 2003).

Figure 3.1: Section-level travel time estimation
In this chapter, for sections without point sensors, the above mentioned approximation error is modeled as prior estimation errors, which can be obtained through a historical travel time database by considering other related links such as adjacent links or links with similar characteristics. Furthermore, our proposed framework can be also easily generalized to a section-based representation scheme, where a section in Fig. 3.1 can be viewed as a link in our link-to-path-oriented modeling structure.

3.3.6 Generic state transition and measurement models

By adapting a structure state model for dynamic OD demand estimation by Zhou and Mahmassani (2007), this chapter decomposes a true travel time pattern into three modeling components:

\[ \text{true travel time} = \text{regular recurring pattern} + \text{structural deviations} + \text{random fluctuations}. \]

Under this assumption, travel time estimation/prediction can be studied in two categories: recurring traffic conditions and non-recurring conditions. For travel time prediction under recurring conditions, structural deviation is considered as zero, and the regular travel time patterns/profiles can be constructed based on historical data for recurring traffic. On the other hand, for travel time prediction under non-recurring conditions, the structural deviation is further modelled in this chapter as a function of time-dependent capacity and time-dependent demand. Without loss of generality, this chapter mainly focuses on time-dependent capacity reductions due to incidents, a major source of non-recurring congestion.

To further jointly consider both recurring and non-recurring traffic conditions in the sensor location problem, the overall system uncertainty under a certain sensor design is modeled as a probabilistic combination of recurring and non-recurring uncertainty measures:

\[ \text{overall system prediction uncertainty} = (1 - \rho_{\text{NR}}) \times \text{uncertainty under recurring conditions} + \rho_{\text{NR}} \times \text{uncertainty under non-recurring conditions}, \]

where \( \rho_{\text{NR}} \) represents the given probability of non-recurring events.
(i) State transition model

The state transition model of the travel time is written as

\[ T_d(t) = T_d^h(t) + V_d(t) + w_d, \quad w_d \sim N(0, Q_d) \]  \hspace{1cm} (1)

In Eq. (1), the travel time for each link is represented as a combination of three components: regular pattern, structural deviation and random fluctuation. The regular pattern \( T_d^h(t) \) is the time-dependent historical travel time average which is determined by the day-to-day regular traffic demand and capacity. For non-recurring traffic conditions, a structural deviation \( V_d(t) \) exists due to non-recurring congestion sources such as incidents, work zones and severe weathers. Considering a stationary congestion pattern, this chapter assumes that \( w_d \) follows a normal distribution with zero-mean and a variance-covariance matrix \( Q_d \). \( Q_d \) corresponds to random travel time variation magnitude, which is further determined by dynamics and stochasticity in the underlying traffic demand and road capacity supply. For example, the travel time variations are more significant on a congested freeway link with close-to-capacity demand flow volume, compared to a rural highway segment with low traffic volume and sufficient capacity where the speed limit could yield a good estimate most of the time. More specifically, \( q_{d,a} \), the (diagonal) variance elements of the matrix \( Q_d \), exhibit the travel time variability/uncertainty of each individual link, while the covariance elements should reveal the spatial correlation relationship (mostly due to queue spillbacks) between adjacent links in a network. We refer readers to a chapter by Min and Wynter (2011) for calibrating spatial correlations of link travel times.

(ii) General measurement model

In order to estimate the regular pattern \( T_d^h(t) \) and structural deviation \( V_d(t) \), a linear measurement model is constructed as:

\[ Y_d(t) = H_d(t) \times T_d(t) + \varepsilon_d, \quad \text{where} \quad \varepsilon_d \sim N(0, R_d) \]  \hspace{1cm} (2)

With the measurement model in Eq. (2), the travel times are estimated using the latest measurements \( Y_d(t) \). Measurement vector \( Y_d \) is composed of travel time observations from point sensors, point-to-point sensors and probe sensors. The mapping matrix \( H_d \), with \((n \times m)\) elements, connects unknown link travel time \( T_d \) to measurement
data $Y_d$. Particularly, each row in the mapping matrix $H_d$ corresponds to a measurement and each column corresponds to a physical link in the network. For an element at $u^{th}$ row and $v^{th}$ column of the matrix $H_d$, a value of 1 indicates that the $u^{th}$ measurement covers or includes the travel time on the $v^{th}$ link of the network, otherwise it is 0. With the measurement equation, the historical recurring travel time pattern is then updated through the Kalman filtering process.

3.3.7 Uncertainty analysis under recurring and non-recurring conditions

We now focus on the conceptual analysis of the uncertainty reduction and propagation. By assuming independence between different components in the structure state model (1), the total variance of the predicted travel time can be obtained by

$$\text{var}(T_d(t)) = \text{var}(T^h_d(t)) + \text{var}(V_d(t)) + Q_d$$

Under recurring congestion conditions, the structural deviation $V_d(t) = 0$, which leads to

$$\text{var}(T_d(t)) = \text{var}(T^h_d(t)) + Q_d.$$  (4)

To reduce prediction error under recurring conditions, (e.g. at the beginning of each day $d$ for pre-trip routing applications), we need to reduce the variance of the historical travel time estimates, $\text{var}(T^h_d(t))$, while the variance of inherent traffic process noises $Q_d$ (due to traffic demand and supply variations) cannot be reduced and sets a limit for travel time prediction accuracy. Along this line, this article will first focus on updating the historical travel time pattern and the uncertainty reduction due to added sensors under recurring conditions. Under non-recurring conditions, in addition to the above mentioned uncertainty elements $\text{var}(T^h_d(t))$ and $Q_d$, the total prediction variance is mainly determined by the structural travel time deviation $V_d(t)$.

3.4 Conceptual framework and data flow

Focusing on predicting end-to-end path travel time applications and considering future availability of GPS probe data on links $A^\infty$, the goal of the sensor location problem is to maximize the overall information gain $X^* = \arg\min_{X_1} z(X)$ by locating point and point-
to-point sensors in sets $A'$ and $N^*$, subject to budget constraints for installation and maintenance. To systematically present our key modeling components in the proposed sensor design model, we will sequentially describe the following three modules.

3.4.1 Link travel time estimation and prediction module

Given prior travel time information $T_d$ and $P_d$, with traffic measurement vector $Y_d$ that includes $y_{d,a}$, $y_{d,i,j,k}$ and $y_{d,a}$ from sensor location sets $A'$, $N^*$ and $A^*$, the link travel time estimation and prediction module seeks to update current link travel times $T_d$ and their variance-covariance matrix $P_d$.

Information quantification module:

With prior knowledge on the link travel time estimates $T$ and $P$, the information quantification module aims to find the single-valued information gain $z(X_i)$ for the critical path travel times for a sensor design scenario $X_i$, represented by location sets $A'$, $N^*$, $A^*$, as well as AVI and AVL market penetration rates $\alpha$ and $\beta$.

3.4.2 Sensor network design module

The sensor design module aims to find the optimal solution $X^* = \arg\min_z z(X_i)$, subject to budget constraints for installation and maintenance. For each candidate solution $X_i$, this module needs to call the information quantification module to calculate $z(X_i)$. The optimal solution $X^*$ produces optimal location sets $A'$ and $N^*$, for a predicted AVI and AVL market penetration rates $\alpha$ and $\beta$, and predicted location set $A^*$ with reliable travel time map-match results.

Fig. 3.2 illustrates the conceptual framework and data flow for the proposed modules. From sensor network design plans in block 1, we need to extract three groups of critical input parameters: AVI/AVL market penetration rates $\alpha$ and $\beta$ at block 2, measurement error variance-covariance $R$ in block 3, and sensor location mapping matrix $H$ in block 4. Location mapping matrix $H$ is derived from the sensor location sets $A'$, $N^*$ and $A^*$. 
The link travel time estimation module uses a Kalman filtering model to iteratively update the travel time (blocks 9 and 10) and the corresponding error variance matrix (blocks 7 and 8), where the critical Kalman gain matrix $K$, calculated in block 6, is applied to the above two mean and variance propagation processes. Based on the estimation or prediction error variance statistics in blocks 7 and 8, the information quantification module derives the measure of information in block 11 by representing the path travel time estimation/prediction quality as a function of $P^+$ and $P^-$. By minimizing the network-wide path travel time estimation uncertainty, the sensor network design module finally selects and implements an optimized sensor plan so that point sensor, AVI, and AVL measurement data in block 13 can be produced from the actual sensor network illustrated by block 12.

One of the key features offered by the Kalman Filtering model is that although updating the travel time mean estimates from $T^-$ in block 9 to $T^+$ in block 10 requires sensor measurements $Y$, the uncertainty propagation calculation from block 7 to 8 (i.e. updating $P^+$ from $P^-$) does not rely on the actual sensor data, as the uncertainty reduction formula in block 8 is a function of three major inputs: a priori uncertainty matrix $P^-$, measurement error range $R$, and sensor mapping matrix $H$. In other words, if a transportation analyst can reasonably prepare the above three input parameters, then he/she can apply the proposed analytical model to compute the information gain for a sensor design scenario and further assist the decision-maker to determine where and with what technologies sensor investments should be made in a traffic network.

3.5 **Measure of information for historical traffic patterns**

One of the fundamental questions in sensor location problems is which criteria should be selected to drive the underlying optimization processes. Above travel time estimation and prediction model offer an analytical model for quantifying the estimation/prediction error reduction due to additional measurements provided by new sensors. As the process variance-covariance matrix is assumed to be constant, the travel time uncertainty measure in this section uses the *a posterior* estimation error covariance
$P^+$ as the basis to evaluate the information gain. A challenging question then is how to select single-value information measures for a sensor design plan. To this end, we first examine two commonly used estimation criteria, namely, the mean-square error and entropy. We then propose total path travel time estimation variance as a new measure of information for end-to-end trip time prediction applications.

Figure 3.2: Conceptual framework and data flow
3.5.1 Trace and entropy

The classic Kalman filter aims to minimize the mean-square error, i.e., the trace of $P_d^*$. The trace of the variance covariance matrix $tr(P_d^*)$ is the sum of the diagonals of the matrix, which is equivalent to the total variance of link travel time estimates for all links:

$$tr(P_d^*) = \sum_{a=1}^{m} \text{cov}(t_{d,a}, t_{d,a}) = \sum_{a=1}^{m} \text{var}(t_{d,a})$$

While the trace does not consider the effects of correlation between travel times of adjacent links, an alternative measure of information is entropy which is commonly used in information theory applications. For a discrete variable, Shannon’s original entropy is defined as the number of ways in which the solution could have arisen. For a continuously distributed random vector $T$, on the other hand, the entropy is measured by $-E(\ln f(T))$, where $f$ is the joint density function for vector $T$. If travel time $T$ in our chapter is assumed to follow a normal distribution, then its entropy is computed as $\theta + \frac{1}{2} \ln(\det(P_d^*))$, where $\theta$ is a constant that depends on the size of $T$, the total number of links in our chapter network. The entropy measure is proportional to the log of the determinant of the covariance matrix. By ignoring the constant $\theta$ and the monotonic logarithm function, we can simplify the entropy-based information measure for the a posteriori travel time estimate as $\det(P_d^*)$. The determinant of the variance covariance matrix, as a measure of information, is also known as the generalized variance. Mathematically, the trace and determinant of the variance covariance matrix $P_d^*$ can be calculated from the sum and product, respectively, of the eigenvalues of $P_d^*$. Since the determinant considers the variance and covariance in the matrix, a smaller determinant is desirable because this indicates a more accurate estimate.

3.5.2 Total path travel time estimation uncertainty

This chapter proposes a new measure of information to quantify the network-wide value of information, based on the travel time estimation quality of critical OD/paths.
The travel time estimation uncertainty of path \( k \) from origin \( o \) to destination \( s \) can be calculated from the posterior travel time estimate variance-covariance matrix \( P_{d}^{+} \):

\[
e_{d,o,s,k} = \sum_{a \in \mathcal{P}(o,s,k)} \text{var}(t_{d,a}) + 2 \times \sum_{a \prec b, a, b \in \mathcal{P}(o,s,k)} \text{cov}(t_{d,a}, t_{d,b})
\]

(6)

where \( \text{var}() \) and \( \text{cov}() \) are variance and covariance coefficients in the link travel time uncertainty matrix, respectively. Compared to trace or entropy based information measures, the proposed path travel time based measure can better capture the possible correlation between traffic estimates along a path, with the covariance portion of the estimation error matrix.

A similar equation can be derived for travel time prediction based uncertainty measure, using the travel time estimate variance-covariance \( P_{d}^{-} \) matrix. For sensor location decisions that jointly consider recurring and non-recurring conditions, an integrated uncertainty matrix can be generated from recurring travel time uncertainty \( P_{-}^{r} \) and non-recurring structure derivation uncertainty \( \Sigma_{-} \):

\[
P_{-}^{d} = (1 - \rho_{\text{incident}} - \rho_{\text{workzone}} - \rho_{\text{weather}}) \times P_{\text{recurrent}}^{-} + \rho_{\text{incident}} \Sigma_{\text{incident}}^{-} + \rho_{\text{workzone}} \Sigma_{\text{workzone}}^{-} + \rho_{\text{weather}} \Sigma_{\text{weather}}^{-}
\]

Weighted by the path flow volume of different origin-destination pairs \( f_{o,s,k} \), the overall estimation uncertainty of the network-wide traffic conditions on day \( d \) can be determined from the following equation:

\[
TU_{d} = \sum_{a,o,s,k} \left( e_{d,o,s,k} \times f_{o,s,k} \right)
\]

(7)

The above total path travel time estimation uncertainty measure includes three important components: (1) the sum of elements in the variance covariance matrix for link travel time estimates; (2) the sum of the travel time variance for each feasible or critical path in the network; and (3) weights of path flow volume for different paths. As the path travel time estimation accuracy (as opposed to individual link travel times) is the ultimate information quality requirement by commuters traveling on various routes, this measure of information can capture the high-level monitoring performance of a sensor network. In relation to the trace and entropy measures, the total path travel time estimation
uncertainty can be viewed as a more appropriate indicator for system-wide information gains.

3.6 Sensor design model and beam search algorithm

The proposed sensor network design model is essentially a special case of the discrete network design problem, so an integer programming model, shown below, can be constructed to find the optimal sensor location solution.

**Min** $TU$

**Subject to**

Budget constraint:

\[ \pi \sum_a x'_a + \pi' \sum_i x''_i \leq \pi \]  

Sensor mapping matrix constraint:

\[ H_d = function\left( A'=[x'_{a}], N''=[x''_{i}], \gamma^m_{d,a}, \alpha, \beta \right) \quad d = 0,1,...,D \]  

$D$ = a sufficiently large day number for measure of information to reach convergence.

- $x'_{a} = 1$ if a point sensor is installed on link $a$, 0 otherwise.
- $x''_{i} = 1$ if an AVI sensor (point-to-point sensor) is installed on node $i$, 0 otherwise.
- $\pi'$, $\pi''$ = installation and maintenance costs for point sensors and point-to-point sensors.
- $\pi$ = total available budget for building or extending the sensor network.

In the above objective function, the overall system uncertainty matrix $P_u$ is calculated as a probabilistic combination of recurring and non-recurring traffic variances. Structure derivations from different non-recurring traffic conditions are considered in the total system uncertainty with corresponding probabilities. For links with sensors, the structure derivation uncertainty is aggregated and averaged from historical measurements (e.g. 95% or $2\sigma$ for normal distribution). For links without sensor, we will take the maximum of the structure derivation from limited historical database.
$H_t$ is determined by the sensor location set $A'=\left[ x'_i \right]$ and $N''=\left[ x''_i \right]$, randomly generated link traversing coefficient for GPS probe vehicles $\hat{\gamma}_d$, and AVI and AVL market penetration rates $\alpha$ and $\beta$.

Essentially, the goal of the above sensor location model is to add sensor information from spatially distributed measurements to minimize the weighted uncertainty associated with the path travel time estimates. In this chapter, a branch-and-bound search procedure can be used to solve the integer programming problem. To reduce the computational complexity, a beam search heuristic algorithm is implemented in this chapter.

Given prior information on the link travel time vector and its estimation error covariance from historical database, the proposed algorithm tries to find the best sensor location scenario from a set of candidates under particular budget constraints. Based on a breadth-first node selection mechanism, the beam search algorithm branches from the nodes level by level. At each level, it keeps only $\varphi$ promising nodes, and prunes the other nodes permanently to limit the total number of nodes to be examined. $\varphi$ is typically referred to as the beam width, and the total computational time of the beam search algorithm is proportional to the selected beam width.

3.6.1 Beam search algorithm

Step 1: Initialization

Generate candidate link set $LC$ and candidate node set $NC$ for point and point-to-point sensors, respectively.

Set the active node list $ANL = \emptyset$. Create the root node $u$ with $A'(u) = \emptyset, N''(u) = \emptyset$, search level $sl(u) = 0$, where $u$ is search node index. Insert the root node into $ANL$.

Step 2: Stopping criterion

Terminate and output the best-feasible solution under one of the following conditions:

(1) If all of the active nodes in $ANL$ have been visited,
(2) The number of active nodes in memory is exceeded.
Step 3: Node generation and evaluation

For each node \( u \) at search level \( sl \) in ANL, remove it from ANL, and generate child nodes;

Scan through the candidate sets LC, if a link \( a \) is not in \( A'(u) \), generate a new child node \( v' \) where \( A'(v') = A'(u) \cup a, N''(v') = N''(u), sl(v') = sl(u) + 1 \).

Scan through the candidate sets NC, if a node \( i \) is not in \( N''(u) \), generate a new child node \( v'' \) where \( N''(v'') = N''(u) \cup i, A'(v'') = A'(u), sl(v'') = sl(u) + 1 \).

For each newly generated node \( v \), calculate the objective function through \( P_D \). If the budget constraint is satisfied for a newly generated node, add it into the ANL.

Step 4: Node filtering

Select \( \varphi \) best nodes from the ANL in the search tree, and go back to Step 2.

In the above beam search algorithm, the total computational time is determined by the number of nodes to be evaluated, which depends on the beam width \( \varphi \) and the size of the candidate sensor links/nodes. For each node in the tree search process, the complexity is determined by the evaluation of the objective function, which can be decomposed into three major steps: (1) calculating \( P^r \) from \( H^TR^{-1}H \), (2) calculating the inverse of the covariance matrix \( (P^r)^{-1} \), and (3) calculating the path travel time uncertainty as a function of \( P_D^r \). The first step involves two matrix multiplications: \( H^TR^{-1} \) and \( (H^TR^{-1})H \). Because \( H \) is an \((n \times m)\) matrix and \( R \) is an \((n \times n)\) matrix, the first step has a worst-case complexity of \( O(m^2n) \), and calculating the inverse of matrix \( P^r \) leads to an \( O(m^3) \) operation if the Gaussian elimination method is used.

For a large-scale sensor network design application, we can adopt three strategies to reduce the size of the problem and therefore the computational time. First, one can focus on critical OD pairs with significant volumes. Second, one can aggregate original OD demand zones into a set of super zones within a manageable size, with this strategy being especially suitable for a subarea analysis where many OD zones outside the chapter area can be consolidated together. Third, we can reduce the size of candidate AVL sensor nodes and point sensor links in order to decrease the number of search nodes to be evaluated.
3.7 Complex cases for updating historical traffic patterns

To consider long-term information gains of a sensor network in monitoring the travel time dynamics, the following discussion aims to derive the steady-state results of uncertainty reduction associated with a fixed sensor network design plan. Considering both point and AVL sensors, we first assume constant \( Q, R \) and \( H \) across different days, the travel time estimation error covariance updating equation as seen in Eq. (10).

\[
P_d^- = (I - K_{d-1} H)P_{d-1}^- + Q
\]

Under steady state conditions, the travel time estimation error covariance will achieve a constant state as \( P = P_d^- = P_{d-1}^- \) after a number of updates. By applying the optimal formulation of Kalman gain \( K \), the steady estimation error covariance \( P \) is rewritten as

\[
PH^T (HPH^T + R)^{-1} HP = Q
\]

or \( P = (I - PH^T (HPH^T + R)^{-1} H)P + Q \) (12)

Eq. (12) is known as Algebraic Riccati Equation. When numerically solving this equation, the steady-state travel time estimation error covariance matrix for a long-term sensor location problem is obtained.

Fig. 3.3 illustrates a day-by-day time series of the travel time estimation variance. Due to the presence of system evolution noise \( Q \), the estimation variance always increases when we make a travel time prediction from day \( d \) to day \( d+1 \), that is, \( P_d^- = P_d^+ + Q_d \). After receiving traffic measurement available every day, the uncertainty associated travel time estimates is reduced through \( P_d^+ = (I - K_d H)P_d^- \). The uncertainty reduction and the resulting information gain are very dramatic after the first few days of sensor deployment. After 5 or 6 days, this zig-zag pattern reaches a stable state when \( P_d^- = P_{d-1}^- \) (corresponding to the upper portion of the time series) and \( P_d^+ = P_{d-1}^+ \) (corresponding to the lower portion of the time series).
Due to the stochastic coverage characteristic of AVL sensor data, we can use a sample-based iterative computation scheme to compute the stable-state posterior estimation covariance matrix $P^+$. In particular, representative samples of $\tilde{\gamma}^{m}_{d,a}$ can be first generated for each day, and then applied into the update equations (16) and (19) over multiple days to check if $\det(P^+)$ converges to a constant value.

### 3.8 Illustrative example and numerical experiments

#### 3.8.1 Illustrative example for locating AVI sensors

In this section, we present an illustrative example with a 6-node hypothetical transportation network to demonstrate how the proposed measures of information can systematically evaluate the trade-offs between the accuracy and placement of individual AVI sensors for path travel time estimation reliability. In Fig. 10, subscript day $d$ is omitted for simplicity. As shown in the base case, there are three traffic analysis zones at nodes $a$, $d$ and $b$, and three major origin-to-destination trips: (1) $a$ to $b$, (2) $a$ to $d$ and (3) $d$ to $b$, each with a unit of flow volume. $P^-$ (e.g. obtainable from a historical travel time database with point detectors) leads to a trace of 12 and a determinant of 48. Among the 5 links in the corridor, link 5 from node $f$ to $b$ has the highest uncertainty in terms of link travel time estimation variance. We can view node $b$ as a downtown area, and the incoming flow from the other two zones creates dramatic traffic congestion and travel...
time uncertainty, first on link 5 and then on link 4. For the base case, we can calculate the variance of path travel time estimates for these three OD pairs, respectively, as 12, 3 and 9, leading to a total path travel time estimation uncertainty ($TU$) as $TU = 24$.

In both cases (I) and (II), two AVI sensors are first installed at nodes $a$ and $b$. In case (I), an additional AVI sensor is located at node $f$ so that we can obtain two pairs of end-to-end travel time measurements: from node $a$ to node $f$, and from node $f$ to node $d$. The second measurement directly monitors travel time dynamics on link 5. In this particular example along the linear corridor, the end-to-end travel time statistics from $a$ to $b$ can be explicitly determined from the above two mutually exclusive observations. In order to avoid double-counting the information gain for the same data sources, the information quantification module in this chapter only considers two raw measurements: from $a$ to $f$, and from $f$ to $d$, to update the link travel time variance covariance matrix from $P^-$ to $P^+$. To do so, the measurement error matrix is assumed to be $R = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$, and the mapping matrix $H = \begin{bmatrix} 1 & 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$, where the first measurement from $a$ to $f$ covers links 1, 2, 3 and 4, and the second measurement from $f$ to $b$ covers link 5. As link 5, with the highest travel time uncertainty, is directly measured from AVI readings, its link travel time estimate variance is reduced from 4 to 0.8, but the resulting $P^+$ contains a large amount of correlation in its link travel time estimates for links 1 to 4. All the path travel time uncertainties for the three OD pairs have been reduced, and $TU = 8.5$. In case (II), the third AVI sensor is installed at node $d$ to match the nature OD trip demand pattern, which produces sensor mapping matrix $H = \begin{bmatrix} 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 1 \end{bmatrix}$. The resulting $P^+$ still contains two clusters of correlations corresponding to two individual measurements from $a$ to $d$ and from $d$ to $b$. The path travel time estimate variances for the
(I) Locate additional AVI reader to reduce highest link travel time uncertainty

\[ P^r = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 2 & 0 & 0 & 0 \\ 0 & 0 & 2 & 0 & 0 \\ 0 & 0 & 0 & 3 & 0 \\ 0 & 0 & 0 & 0 & 4 \end{bmatrix} \]

\[ Tr = 12 \quad Det = 48 \quad TU = 12 + 3 + 9 = 24 \]

Base case

(II) Locate additional AVI reader to match origin-to-destination trip pairs

\[ P^r = \begin{bmatrix} 0.89 & -0.22 & -0.22 & -0.33 & 0 \\ -0.22 & 1.56 & -0.44 & -0.67 & 0 \\ -0.22 & -0.44 & 1.56 & -0.67 & 0 \\ -0.33 & -0.67 & -0.67 & 2 & 0 \\ 0 & 0 & 0 & 0 & 0.8 \end{bmatrix} \]

\[ Tr = 6.8 \quad Det = 1.07 \quad TU = 3.47 + 2.01 + 3.02 = 8.5 \]

Figure 3.4: Example of locating AVI sensors on a linear corridor
OD pairs from $a$ to $d$ and from $d$ to $b$ are dramatically reduced to 0.75 and 0.9. Although link 5 still has a relatively large estimate variance of 2.4, its overall estimation error measure, total travel time estimation uncertainty $TU$ is now 3.3, which is much lower than $TU = 8.5$ in case (I).

In comparison, by locating and spacing AVI sensors to naturally match the spatial trip patterns of commuters, case (II) is able to systematically balance the trade-off between the needs for monitoring local traffic variations and end-to-end trip time dynamics. It is also important to notice that, both cases (I) and (II) have the same network coverage and generate the same number of measurements every day, but they provide different information gains from a commuter/road user perspective. Thus, simple measures of information, such as traffic network coverage and the number of measurements, might not be able to quantify the system-wide uncertainty reduction and information gain for traveler information provision applications.

3.8.2 Sensor location design for traffic estimation with recurring conditions

In this chapter, we examine the performance of the proposed modeling approach through a set of experiments on a simplified Irvine, California network, which is comprised of 16 zones, 31 nodes and 80 directed link. This chapter considers a single path between each OD pair in this simple network.

All the experiments are performed on a computer system equipped with an Intel Core Duo 1.8GHz CPU and 2 GB memory. Shown in Table 3.1, a set of critical OD pairs with large flow is selected to estimate the network-wide path travel time based uncertainty. Additionally, a beam search width of 10 is used in the beam search algorithm to reduce the computational complexity. The total number of nodes in the search tree is the number of additional sensors times the beam search width. In our experiments, with standard Matlab matrix calculation functions, it takes about 30 min to compute 160 nodes in the beam search tree for this small-scale network.

In this section, we examine the proposed information measure model and sensor location algorithm for the estimation of recurring traffic conditions. With given OD flow
and prior uncertainty information, three scenarios of sensor location plan are designed to compare with current sensor network.

We first conduct experiments to compare the existing point sensor network (Fig. 3.5a) and an optimized point sensor network plan (Fig. 3.5b), both with the same number (i.e. 16) of point sensors. Table 3 shows the critical path travel time estimation errors under those two scenarios. The results show that the proposed optimization model can reduce the path travel time estimation variance by an average of 34.3%, while the existing sensor plan only reduces the same measure by about 16.5%. By factoring in the OD demand volume (shown in the third column), we can compute the proposed measure of information: the total path travel time estimation variance. The base case with zero sensor produces $TU_{\text{zero_sensor}}=114855$, the existing locations reduce $TU$ to 88878 (77.3% of $TU_{\text{zero_sensor}}$), and the optimized sensor location scenario using the proposed model further decreases the system-wide uncertainty to $TU= 63586$ (55.3% of $TU_{\text{zero_sensor}}$). This clearly demonstrates the advantage of the proposed model in terms of improving end-to-end travel time estimation accuracy.

Table 3.1: Critical Path Travel Time Estimation Error under Existing and Optimized Sensor Location Strategies

<table>
<thead>
<tr>
<th>Origin</th>
<th>Destination</th>
<th>Hourly volume</th>
<th>Prior path travel time estimation variance without sensor</th>
<th>Prior path travel time estimation variance with existing sensors</th>
<th>% reduction in variance due to exiting sensors</th>
<th>Posterior path travel time estimation variance with optimized sensor locations</th>
<th>% reduction in variance due to optimized sensor locations</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>16</td>
<td>4000</td>
<td>5.87</td>
<td>5.14</td>
<td>12.44%</td>
<td>3</td>
<td>48.89%</td>
</tr>
<tr>
<td>16</td>
<td>4</td>
<td>6820</td>
<td>5.24</td>
<td>3.94</td>
<td>24.81%</td>
<td>2.8</td>
<td>46.56%</td>
</tr>
<tr>
<td>12</td>
<td>4</td>
<td>1152</td>
<td>1.85</td>
<td>1.85</td>
<td>0</td>
<td>1.32</td>
<td>28.65%</td>
</tr>
<tr>
<td>4</td>
<td>16</td>
<td>2480</td>
<td>5.23</td>
<td>3.54</td>
<td>32.31%</td>
<td>3.19</td>
<td>39.01%</td>
</tr>
<tr>
<td>16</td>
<td>12</td>
<td>832</td>
<td>4.91</td>
<td>3.61</td>
<td>26.48%</td>
<td>3</td>
<td>38.90%</td>
</tr>
<tr>
<td>15</td>
<td>4</td>
<td>880</td>
<td>2.81</td>
<td>2.6</td>
<td>7.47%</td>
<td>2.07</td>
<td>26.33%</td>
</tr>
<tr>
<td>12</td>
<td>16</td>
<td>680</td>
<td>4.9</td>
<td>3.21</td>
<td>34.49%</td>
<td>3.21</td>
<td>34.49%</td>
</tr>
<tr>
<td>16</td>
<td>1</td>
<td>4800</td>
<td>5.86</td>
<td>4.28</td>
<td>26.96%</td>
<td>3</td>
<td>48.81%</td>
</tr>
<tr>
<td>4</td>
<td>15</td>
<td>604</td>
<td>2.81</td>
<td>2.81</td>
<td>0</td>
<td>2.47</td>
<td>12.10%</td>
</tr>
<tr>
<td>4</td>
<td>12</td>
<td>444</td>
<td>1.85</td>
<td>1.85</td>
<td>0</td>
<td>1.5</td>
<td>18.92%</td>
</tr>
</tbody>
</table>
(a) Existing point sensor locations

(b) Optimized sensor network locations
(start from a zero-sensor case)

(c) Sensor network with 4 point sensors in addition to exiting 16 point sensors
Figure 3.5: Numerical experiment results for regular traffic pattern estimation.

In the next set of numerical experiments, we compare two scenarios with additional sensors on top of the existing sensors.

1) Add 4 point sensors on uncovered links still with large travel time variance, leading to a total 16+4=20 point sensors, shown in Fig. 3.5(c);

2) Add 6 AVI readers on major zones with large volume, leading to a network with 16 point sensors and 6 AVI readers, shown in Fig. 3.5(d).

Fig. 3.6 further compares the measure of uncertainty at different stages. It is interesting to observe that compared to the optimized scenario (from the scratch) with 16 sensors, this “additional point sensors” scenario (with 20 sensors) does not offer a superior uncertainty reduction performance for different OD pairs. On the other hand, compared to adding 4 point sensors to cover highly dynamic links, installing additional 6 AVI sensors does not further improve the path travel time estimation performance dramatically.
3.8.3 Sensor location design for traffic prediction with recurring and non-recurring conditions

Now we perform the proposed algorithm by considering both regular and non-recurring traffic conditions. As discussed in Section 7, the total traffic prediction uncertainty is computed as a probabilistic combination of recurring and non-recurring uncertainties. In this numerical experiment, we take the incident as a demonstration example, with the link based incident rates shown in Fig. 3.7(a). The proposed sensor location algorithm is applied in three scenarios: (1) optimized sensor network with 16 point sensors, (2) current network with additional 4 point sensors, and (3) current network with additional 6 AVI sensors. Consequentially, these three sensor network design results are plotted in Figs.3.7(b-d). It is interesting to note that when considering non-recurring traffic conditions (incidents), the optimized sensor locations (Fig. 13b) are more focused on links with higher incident rates, compared to the regular pattern estimation based planning result in Fig. 11(b).
(a) Annual incident rate

(b) Optimized sensor network locations
   (start from a zero-sensor case)

(c) Sensor network with 4 point sensors in addition to exiting 16 point sensors
3.9. Conclusions

To provide effective congestion mitigation strategies, transportation engineers and planners need to systematically measure and identify both recurring and non-recurring traffic patterns through a network of sensors. The collected data are further processed and disseminated for travelers to make smart route and departure decisions. There are a variety of traditional and emerging traffic monitoring techniques, each with ability to collect real-time traffic data in different spatial and temporal resolutions. This chapter proposes a theoretical framework for the heterogeneous sensor network design problem. In particular, we focus on how to better construct network-wide historical travel time databases, which need to characterize both mean and estimation uncertainty of end-to-end path travel time in a regional network.

A unified Kalman filtering based travel time estimation and prediction model is first proposed in this research to integrate heterogeneous data sources through different measurement mapping matrices. Specifically, the travel time estimation model starts with the historical travel time database as prior estimates. Point-to-point sensor data and GPS probe data are mapped to a sequence of link travel times along the most likely travelled path. Through an analytical information updating equation derived from Kalman filtering, the variances of travel times on different links are estimated for possible sensor design.

Figure 3.7: Numerical experiment results under recurring and non-recurring traffic conditions
solutions with different degree of sampling or measurement errors. The variance of travel time estimates for spatially distributed links are further assembled to calculate the overall path travel time estimation uncertainty for the entire network as the single-valued information measure. The proposed information quantification model and beam search solution algorithm can assist decision-makers to select and integrate different types of sensors, as well as to determine how, when, where to integrate them in an existing traffic sensor infrastructure.

In our on-going research, we plan to expand the research in the following ways. First, this chapter only focuses on the sensor design problem for estimating the mean of path travel time, and a natural extension is to assist sensor design decisions for other network-wide traffic state estimation domains, such as measuring and forecasting point-to-point travel time reliability, and incident detection probability. Second, under assumptions of normal distributions for most error terms, the proposed sensor location model is specifically designed for the minimum path travel time estimation variance criterion, and our future work should consider other crucial factors for real-world sensor network design, such as allowing log-normally distributed error terms and minimizing maximum estimation errors. Furthermore, the offline model developed in this chapter could be extended to a real-time traffic state estimation and prediction framework with mobile and agile sensors. The numerical experimental results (for a small-scale network) in this chapter also demonstrate computational challenges (due to heavy-duty matrix operations) in applying the proposed information-theoretic sensor location strategy in large-scale real-world networks, and these challenges call for more future research for developing efficient heuristic and approximation methods.
CHAPTER 4. QUANTIFYING VALUE OF TRAFFIC INFORMATION

Over the past two decades, real-time information systems have been proposed as a mechanism to generate system-wide and individual travel time savings in congested vehicular traffic networks. Ideally, a traveler/driver would fully comply with such information. However, more likely, he/she would use it to partly modify the existing trip route or completely ignore the information based on inherent behavioral tendencies, past experience, situational factors (such as time-of-day, weather conditions, and trip purpose), and the ambient traffic conditions encountered (Peeta and Yu, 2006). Hence, the complexities associated with driver behavior may impact the reliable prediction of traffic network states unfolding over time as well as the potential benefits derived from information provision. Traditionally, the prediction of system performance under real-time information provision has been studied using dynamic traffic assignment (DTA) models (Ben-Akiva, et al., 1998; Mahmassani, et al., 1998) in which individuals are assigned to time-dependent routes from their origins or en-route locations to their destinations so as to satisfy some system-wide objective and/or individual user level constraints. However, these models primarily focus on modeling the traffic flow propagation robustly, while the role of traveler behavior on the evolution of the network dynamics has largely been subsumed by making potentially restrictive a priori assumptions on behavior (Peeta and Yu, 2006). For example, such assumptions include one or more of the following: (i) travel time is the only basis for route choice decision-making, (ii) users are behaviorally homogeneous, and/or (iii) pre-specified behavior classes are available whose fractions are known in the ambient traffic stream. Further, they do not consider learning that takes place over longer timescales.

Several simulation-based studies have been conducted over the past two decades to analyze the evolution of the traffic network under real-time information provision to drivers. Some of them assume specific driver behavior models and seek to understand the effect of real-time information on the unfolding network states. Others combine an underlying traffic simulator with laboratory-based interactive experiments where the
participants are provided real-time routing information on the traffic conditions related to their origin-destination (O-D) trip. Thereby, their real-time decisions are simulated along with that of the ambient traffic for the test network (Adler, et al., 1993; Pel, 2011; Kwan et. al., 2006; Adler and McNally, 1994). However, the various simulation studies are typically limited by one or more of the following: (i) the need to pre-specify behavior models, (ii) the small number of participants, and (iii) the type of network topology considered (such as parallel route corridors). More importantly, and of fundamental relevance to the proposed work, there is a presumption of the type of information available, how and when it can be delivered to the individual travelers, and how it is processed by the travelers. In simulations models, all of these are seamless and the focus is purely on the estimating the potential benefits of real-time information provision. Unfortunately, this is where there is an underlying disconnect with the real-world, beyond the key issues related to restrictive behavioral assumptions. First, travelers can process only limited information while driving. Hence, it is important to characterize the effects of real-time information based on providing only information that can be realistically processed by individuals in real-time (as opposed to unstated assumptions in simulation models of the ability to process any information provided). Second, due to safety concerns and the inability of individuals to multitask safely while driving, how the information is provided to them (for example, voice, visual, or text) becomes a key issue. Again, this is presumed as seamless in simulation models. Third, there are technological issues related to when information is provided to travelers. This would imply the continuous tracking of each traveler or mechanisms for two-way communication with an automated server. That is, how would the information system operator ensure the timeliness of the information provided to a traveler relative to his/her current location in the network? In simulation models, there is an implicit assumption that a traveler can be accessed anywhere, or possibly at discrete points, in the network to provide such information. Hence, even if we were to discount issues related to the adequacy of representing traveler behavior, the three issues mentioned heretofore would lead to gaps between the benefits predicted by a simulation model and those of actual field experiments.
To provide a better understanding of the potential value of real-time traffic information to travelers, we propose carefully designed field experiments that additionally seek to explicitly capture the behavioral aspects of travelers. That is, we seek to analyze the effect of the actual information provided to a traveler on that traveler’s response after each instance of such information provision. The collected data will be used to develop more reliable models of traveler response behavior by identifying the various factors that affect decision-making under information provision. Further the experiments will help in identifying additional performance measures beyond the traditionally used benchmark of travel time savings that leads to better understanding of the potential benefits of a real-time information system to both the user and the operator.

4.1 **Field Experiment**

The proposed chapter seeks to determine the value of real-time information for travelers through carefully designed field experiments that circumvent the limitations of computer simulations as well as the methodological challenges. The experiments will be conducted using a sample of 500 participants in Indianapolis city by tracking their daily morning commute (from home to work) under pre-trip and en-route real-time information provided via the Internet and GPS-enabled cell phones. The chapter will first create a diverse pool of volunteer participants for the experiment. They will be chosen so as to represent the general driving population, and will be additionally filtered based on their access to the relevant technology (GPS-enabled cell phones or Smartphones and Internet). As a participant’s home-to-work commute will be tracked for each day of the experiment, they will be provided a privacy compliance letter. Once the participants have qualified for the survey, they will be given login information to the chapter website and an app to install on their cellphones. Each participant will have a separate database which will be stored in the server.

As a pre-processing step, the participants will be required to provide their usual routes from home to work, familiarity with routes, attitude towards information, and other socio-economic characteristics in a one-time online survey. Next, for each day of
the duration of the experiment, each participant fills a daily trip diary about their actions related to the real-time information provided after the trip; these will be supplemented using GPS-based tracking data for that participant. The experiments will be conducted only for the home-to-work commute so as to maintain data consistency and enhance the ability of participants to retain memory while filling the daily trip diary. The one-time online survey and the daily trip diary will provide data to capture the qualitative behavioral aspects of the response towards the supplied real-time information. The quantifiable aspects will be in form of the potential travel time savings obtained by changing the current route at each instance. A combination of the stated and revealed preference data will be used to derive the quantitative and qualitative value of the real-time information to the customers.

4.2 Data Availability

The advent of modern real-time traffic information dissemination technologies and potential future levels of market penetration make it technologically viable to send personalized information in both pre-trip and en-route contexts (to smart phones through websites like traffic.com, GPS Navigation system through traffic receivers), as well as generic information en-route (through variable message signs (VMS)) and pre-trip (through traffic information websites and radio FM). Further, technologically, it is possible to track the compliance, non-compliance or partial compliance related to the information provided using devices such as GPS (Lawson et al., 2008), supplemented further manually by travelers’ daily trip diaries (Asakura and Hato, 2004; Itsubo and Hato, 2006). Nevertheless, significant methodological challenges exist beyond privacy concerns in enabling related field studies. First, to understand an individual traveler’s response, there is the need to obtain data on his/her inherent behavioral tendencies (for example, the level of willingness to take risks) as well as attitude towards information provided. Second, the ability to understand whether information provision at any point in time caused the traveler to shift from his/her current route requires the knowledge of the current route at each information provision time instance as well as the commonly-used routes by that traveler for the daily commute. Third, ideally, the decision of the traveler is
captured immediately after each instance of information provision, as memory retention of the cause of the response may diminish with time, in addition to the response itself, especially if information is provided several times.

A promising start in using the aforementioned technologies is the field experiment conducted by Demers et al. (2006). Using GPS-equipped vehicles, they share real-time data on network travel times and route choices are updated based on the GPS tracking. The primary objectives were to illustrate the feasibility of this system architecture and the ability to track the user routes. However, the experiment does not focus on a detailed characterization of individual user behavior attitudes to information, which is essential to infer the value of real-time information to travelers and to address the methodological challenges identified in the previous paragraph.

4.3 Survey Design

Table 1 shows list of variables and attributes that can impact benefits derived from real-time traffic information. The objectives of the survey are as given below:

- To know traveler’s inherent attitude of real-time information and preference (one-time online survey)
- To capture traveler’s attitude, preference change and learning behavior (daily trip diary)
- To obtain traveler’s behavioral response to real-time information and evaluation of their satisfaction from commute trip over days (daily trip diary)

Table 4.1: List of variables and attributes that may impact traveler’s benefits from real-time traffic information

<table>
<thead>
<tr>
<th>Variable</th>
<th>Attributes</th>
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<tbody>
<tr>
<td>Socio-Economic</td>
<td>• Gender</td>
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<td>• Age</td>
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<td>• Income</td>
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<td></td>
<td>• Education</td>
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<td></td>
<td>• Dependency</td>
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<tr>
<td>Familiarity</td>
<td>• Familiarity with alternative routes</td>
</tr>
<tr>
<td></td>
<td>• Familiarity with real-time traffic information</td>
</tr>
</tbody>
</table>

Situational

- Congestion
- Incident
- Adverse Weather
- Construction
- Time of the day

4.4 **Experimental Design**

For each day of the field experiment, before leaving for their commute, participants access the study website or customized app installed on their cell phones to obtain: (i) current traffic conditions, and (ii) projected traffic conditions on their routes. The current traffic conditions will be based on the real-time traffic information available from the traffic feed from NAVTEQ (owner of traffic.com). NAVTEQ provides real-time traffic information from four types of sources: digital traffic sensors, GPS/probe devices, commercial and government partners, and its own traffic operations center staff members. Also, a dedicated staff at traffic operations centers for each of the cities consistently monitors traffic conditions. NAVTEQ also maintains historical traffic patterns (a database with information about the average traffic speed for specific sections of roadways, geo-referenced to the NAVTEQ map). The projected traffic conditions will be based on the expected traffic at different time intervals on the routes based on traffic history and real-time information using advanced predictive algorithms.

The participant will choose the route he/she wishes to follow for that day and records it on the study website or cell phone app. Once the participant starts his/her trip, his/her location will be tracked using the GPS-enabled cell phone by two way communication from the server. The app installed in a cell phone tracks real-time locations, speeds, and headings of participants in the vehicle, and communicate this information to the server. If required, he/she can disable the app after each trip. During the home-to-work trip, the participant will be provided en-route traffic updates based on the changes in the traffic conditions on the chosen route and their response is tracked. After finishing the trip on a specific day, the participant fills the daily trip diary which will have queries regarding the information provided and their experience with the information in qualitative terms (type of information received, reliability of the information, the reason for the choosing/not
choosing the prescribed route, and level of satisfaction based on information (on Likert scale)). This process is repeated for each day of the planned field experiment i.e. at least 30 days.

After finishing the field experiment, the next step is to check for the consistency of the recorded trip diaries. If the trip route data is inconsistent with the tracked information, the tracked information is used for analysis. The next step is to analyze whether a participant followed the usual route or the route suggested by the real-time information. The stored data in the server will be used for analysis. The quantitative benefits will be calculated as the difference between the actual travel time had the participant followed the pre-trip/current route and the travel time if he/she followed the suggested route. The qualitative benefits will be measured using user feedback on the perceived usefulness of traffic information, level of satisfaction, and reduction in anxiety. Using a large portion of the finalized study data, econometric and statistical analysis will be performed to characterize the quantifiable and qualitative benefits of real-time information. The analyses will be used to construct reliable models of traveler response behavior under real-time information.

4.5 Concluding comments

The goal of this study is to measure and understand the benefits of real-time traffic information to the commuter by investigating the physical and psychological benefits of real-time information by developing reliable traveler behavior models that can be used to predict costs and benefits for real-world deployment. Two key aspects of this study are: (i) the proposed field experiments seek to develop robust behavior models related to real-time information provision that can be used reliably in practice, and (ii) the study seeks to identify performance measures beyond just the travel time savings to understand the value of a real-time information system for the user and operator. The expected results are better understanding of psychological benefits to users from real-time traffic information beyond travel time savings. We will also be able to explore if mere availability of information gives assurance to the user irrespective of quality of information in an unfamiliar location.
CHAPTER 5. CONCLUSIONS AND FUTURE RESEARCH

5.1 Summary

In this study three major objectives were identified to be accomplished to exploit innovative data collection, traffic management, and road pricing/crediting mechanisms that can encourage mutually beneficial information-sharing under innovative partnerships for real-time traffic information systems. The first objective was to develop a unified data mining system that can synthesize different data sources to estimate traffic network states. Second, we identified existing deficiencies in data quality, coverage and reliability in an existing DOT traffic sensor network and develop an information gain theoretic model for optimal sensor location that can take into account uncertainty. The third objective was to measure and understand the physical and psychological benefits of real-time traffic information to the commuters and develop reliable traveler behavior models that can be used to predict costs and benefits for deployment of such systems to stakeholders. Each of these objectives has been studied in separate chapters in the study.

In the second chapter we investigated cumulative flow count-based system modeling methods that estimate macroscopic and microscopic traffic states with heterogeneous data sources on a freeway segment. A novel approach of use of the multinomial probit model and Clark’s approximation method is used to develop a stochastic three-detector model. The model estimates the mean and variance-covariance of cumulative vehicle counts on both ends of a traffic segment, which are used as probabilistic inputs for estimating cell-based flow and density inside the space-time boundary and to construct a series of linear measurement equations within a Kalman
filtering estimation framework. This research presented an information-theoretic approach to quantify the value of heterogeneous traffic measurements for specific fixed sensor location plans and market penetration rates of Bluetooth or GPS flow car data.

In the next chapter, we study the second objective, where an information-theoretic sensor location model that aims to maximize information gains from a set of point, point-to-point and probe sensors in a traffic network is proposed. This model gives a particular emphasis on the end-to-end travel time prediction problem. Based on a Kalman filtering structure, the proposed measurement and information quantification models explicitly take into account several important sources of errors in the travel time estimation/prediction process, such as the uncertainty associated with prior travel time estimates, measurement errors and sampling errors. Further, a discussion on quantifying information gain for steady state historical databases and point-to-point sensors with multiple paths is provided. A heuristic beam-search algorithm is developed to solve the proposed combinatorial sensor selection problem. A number of illustrative examples are used to demonstrate the effectiveness of the proposed methodology.

The fourth chapter aims to study the benefits of real-time traffic information systems to the commuter by investigating the physical and psychological benefits of real-time information by developing reliable traveler behavior models that can be used to predict costs and benefits for real-world deployment of these systems. The study proposes field experiments to develop robust behavior models related to real-time information provision that can be used reliably in practice. Further, the study seeks to identify performance measures beyond just the travel time savings to understand the value of a real-time information system for the user and operator. The proposed experiment is yet to be performed, but the survey design and experiment plan has been discussed in detail in the chapter.

5.2 Future research directions

There are several potential future research directions. As mentioned earlier, this is the first year report of a multiple year effort. Future research will focus on the following major aspects:
The proposed single-segment-oriented methodology will be further extended for a corridor model with merges/diverges for possible medium-scale traffic state estimation applications.

The proposed model for the traffic state estimation problem will be further extended to a real-time recursive traffic state estimation and prediction framework involving multiple O-D pairs with stochastic demand patterns or road capacities.

Given the microscopic state estimation results, one can quantify the uncertainty of other quantities in many emerging transportation applications, e.g., fuel consumption and emissions that mainly dependent on cell-based or vehicle-based speed and acceleration measures, and link-based travel times that can be related to the cumulative vehicle counts on the boundary.

This study only focuses on the sensor design problem for estimating the mean of path travel time, and a natural extension is to assist sensor design decisions for other network-wide traffic state estimation domains, such as measuring and forecasting point-to-point travel time reliability, and incident detection probability.

The proposed sensor location model is specifically designed for the minimum path travel time estimation variance criterion with assumptions of normal distributions for most error terms. The future work should consider other crucial factors for real-world sensor network design, such as allowing log-normally distributed error terms and minimizing maximum estimation errors.

Furthermore, the offline model developed in this study could be extended to a real-time traffic state estimation and prediction framework with mobile and agile sensors.

The proposed field experiments for real-time traffic information need to be performed to gain insights into the quantification of real-time traffic information benefits.
REFERENCES


